

# Optical Manipulation of Magnetism in a Correlated Electron System

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Tohoku University  
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Sumio Ishihara



New Frontier of Strongly Correlated Electron Material,  
August 6-24, 2018 Kavli ITS Beijing, China

# Outline

## [1] Excitonic insulating state in a correlated material as an orbital physics



J. Nasu (Tokyo Tech.), M. Naka (Waseda Univ.)  
T. Tatsuno (Tohoku Univ.), T. Watanabe (Chiba Tech.)

Phys. Rev. B **93**, 205136 (2016)  
J. Phys. Soc. Jpn. 85, 083706 (2016)

## [2] Double exchange interaction in non-equilibrium state

A. Ono (Tohoku Univ.) J. Ohara (Hokkaido Univ.),  
Y Kanamori (Tohoku Univ.)

Phys. Rev. Lett. 119, 207202 (2017) (Editors' suggestion)  
Phys. Rev. B 88, 085107 (2013)

# Band insulator v.s. Mott insulator

Band Insulator

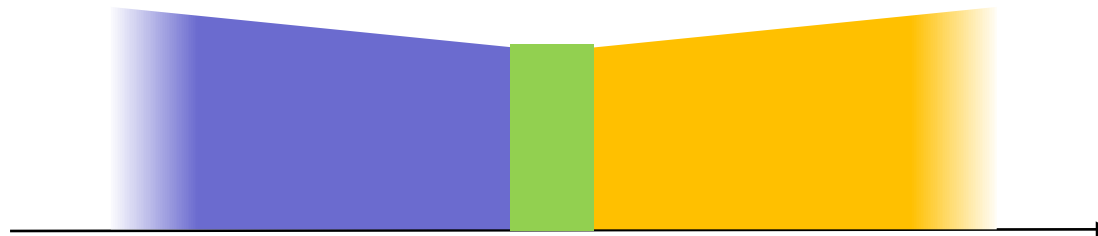
Mott Insulator



Band Insulator

Mott Insulator

Another type  
of insulator

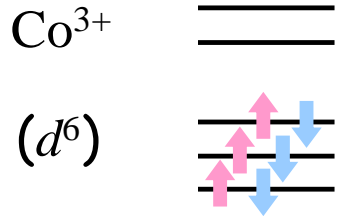


Excitonic insulator (EI)

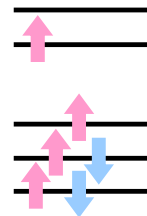
# Perovskite cobaltites

LaCoO<sub>3</sub>

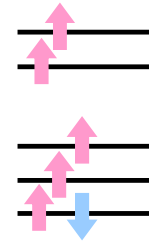
Spin state degree of freedom in Co ion



Low spin  
LS  
(S=0)

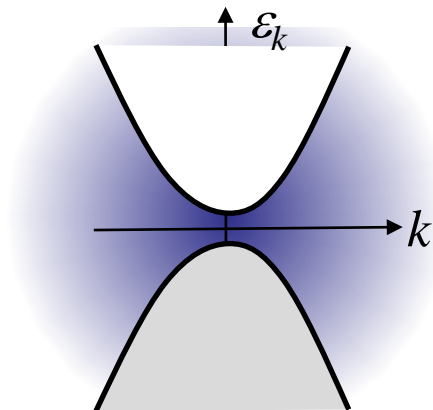


Intermediate  
spin  
(IS) (S=1)



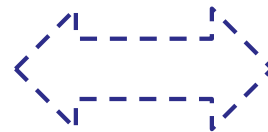
High spin  
(HS)  
(S=2)

Band Insulator

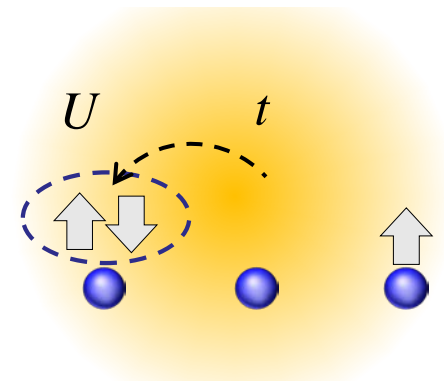


Level splitting  
 $\Delta$

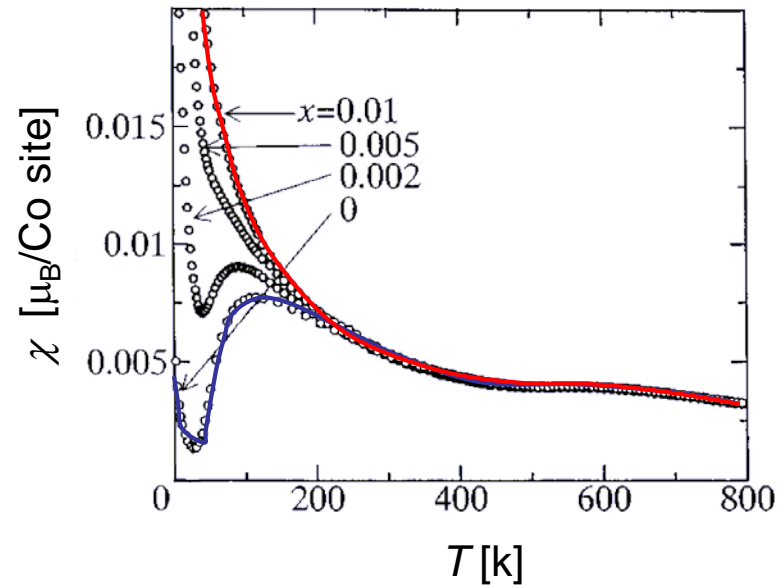
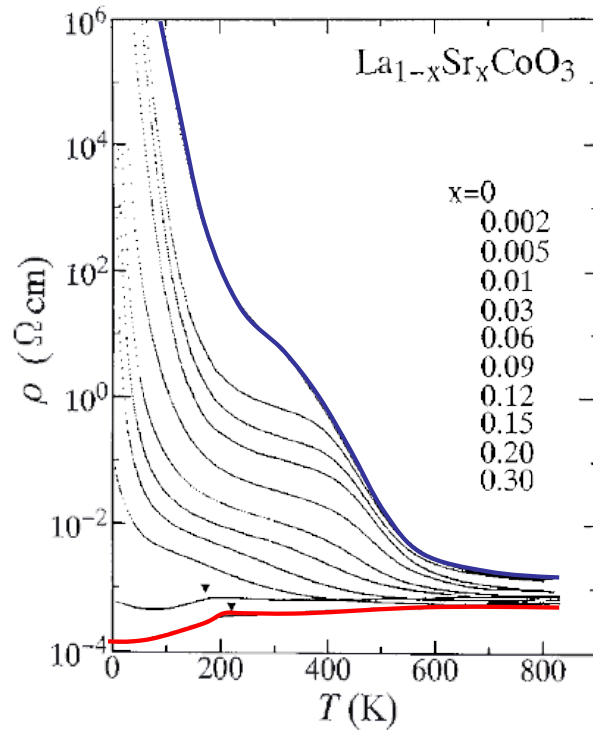
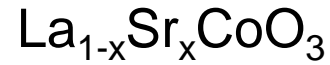
Hund coupling  
 $J$



Mott Insulator



# Perovskite cobaltites

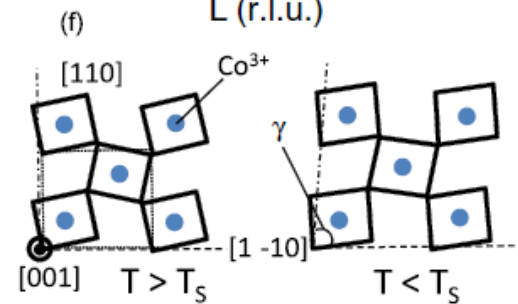
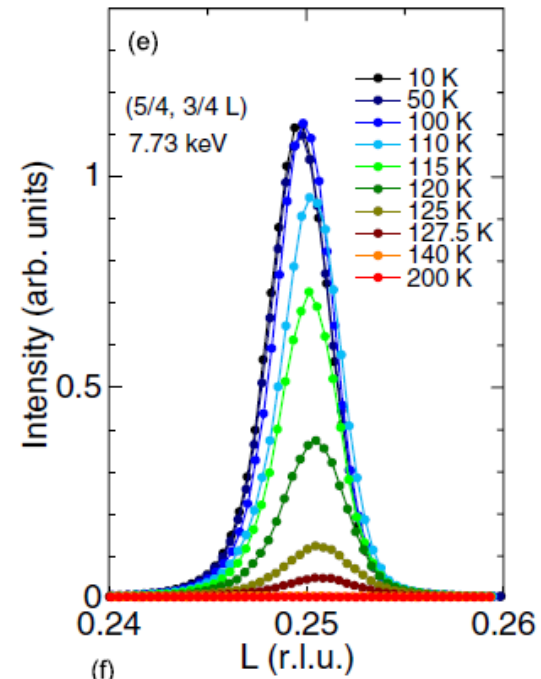
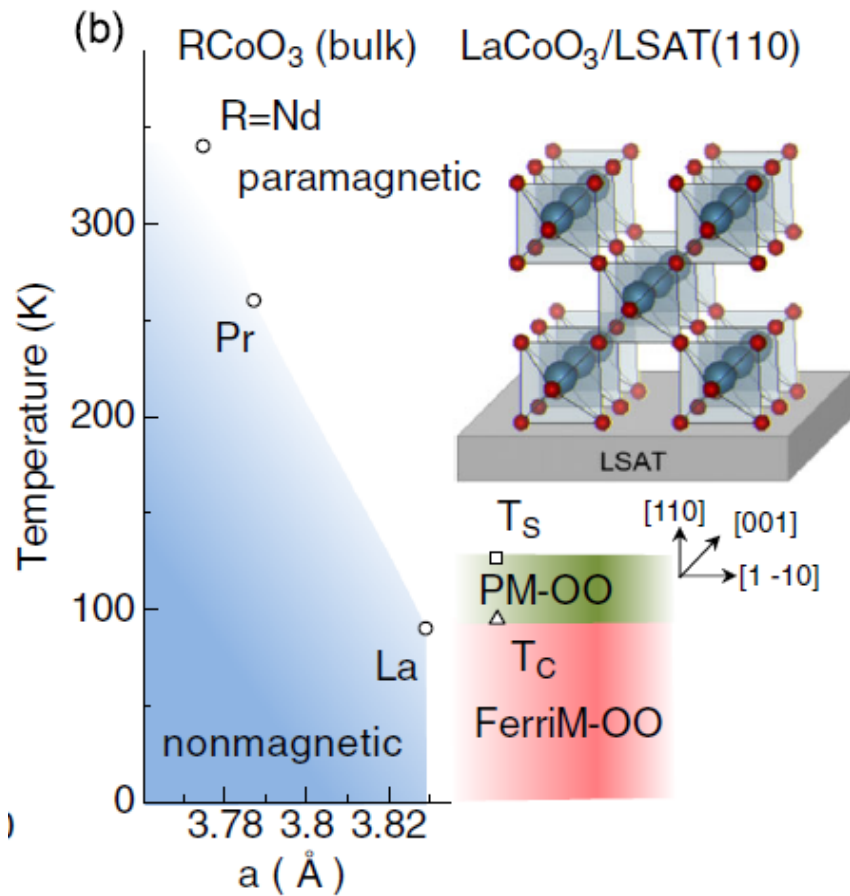
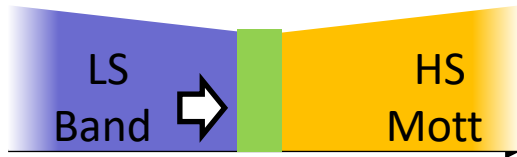


Tokura *et al.* PRB **58** R1699 (1998)

- $\text{LaCoO}_3$  : LS Insulator to HS (IS) metal with increasing T
- LS Insulator to FM metal with x

# Strain on thin film

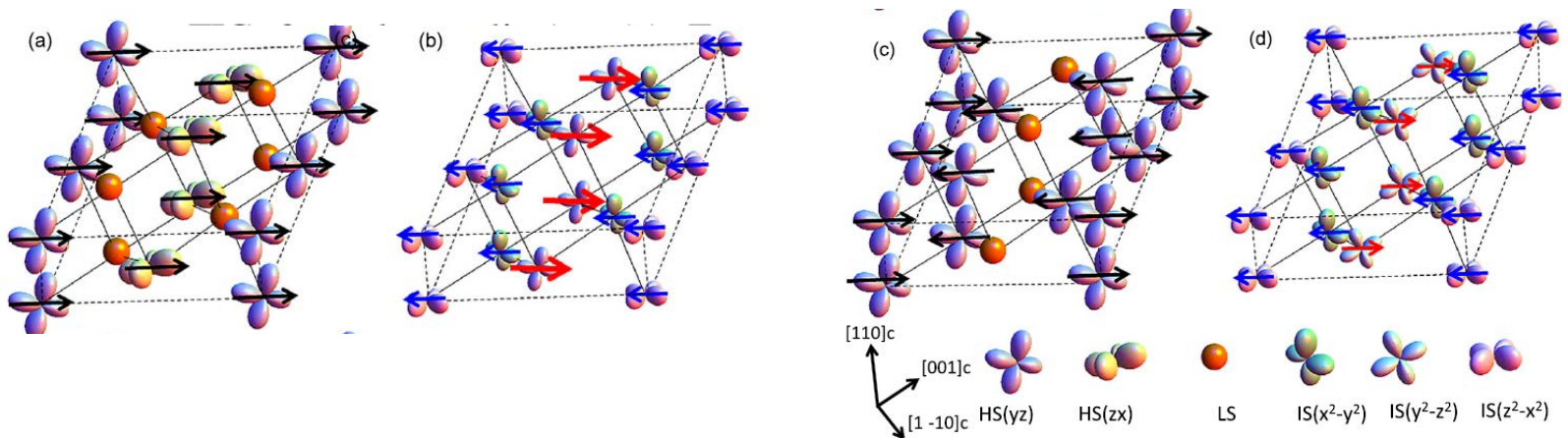
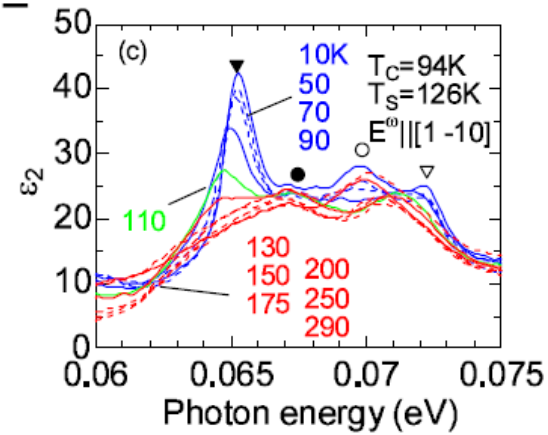
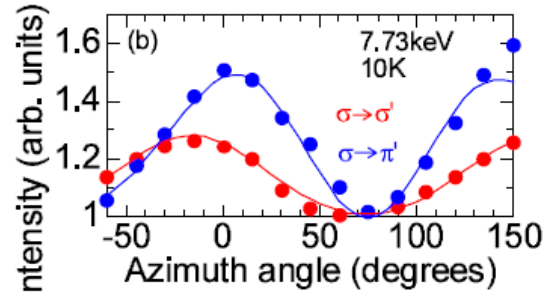
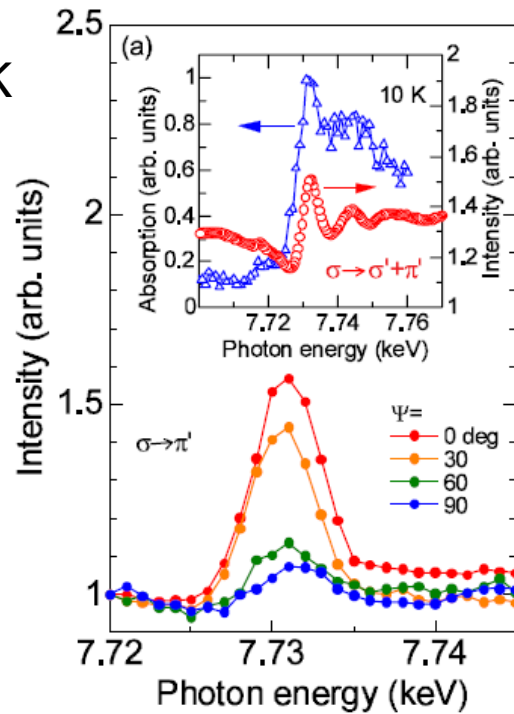
J. Fujioka et al.  
PRL 111, 027206 (2013)



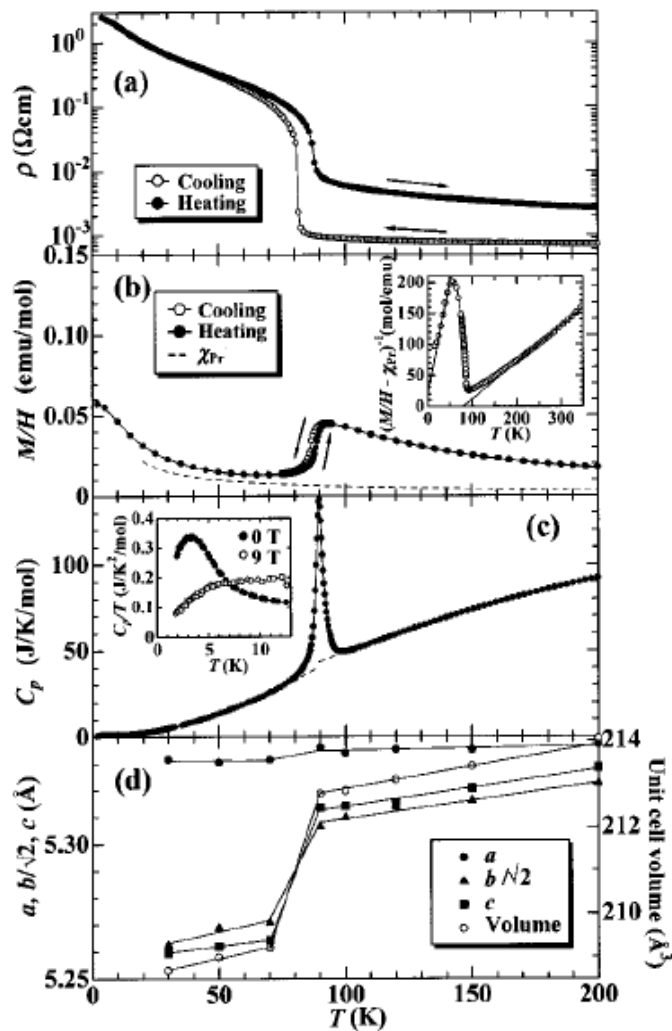
# Strain on thin film

RXS @ Co K

J. Fujioka et al.  
PRL 111, 027206 (2013)



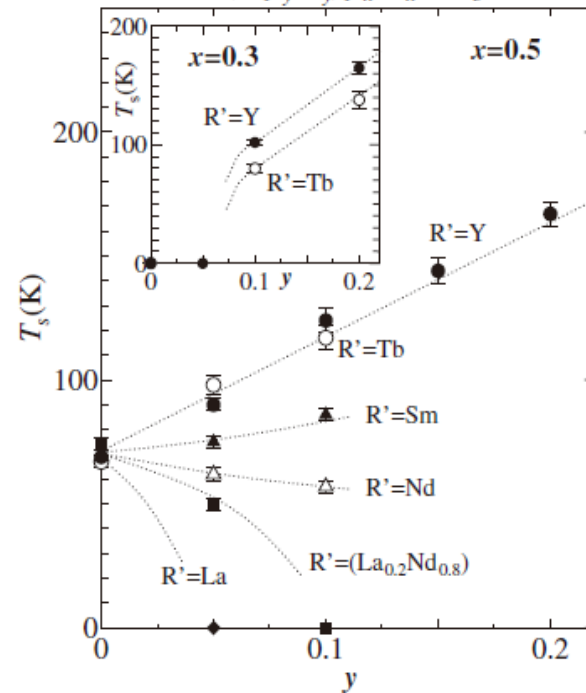
# Ion substitution (II)



Tsubouchi-Itoh et al. Phys. Rev. B **66**, 052418 (2002)



Fujita-Satoh et al. J. Phys. Soc. Jpn. **73**, 1987(2004)  
 $(\text{Pr}_{1-y}\text{R}'_y)_{1-x}\text{Ca}_x\text{CoO}_3$



Probably

$\text{Pr}^{4+}$

$\text{Co}^{3+}$

J. Kuneš and P. Augustinský PRB **89**, 115134 (2014)

J. Kuneš and P. Augustinský PRB **90**, 235112 (2014)

a candidate of **excitonic insulator (EI)**



# Excitonic Insulators

Semiconductor, Semimetal

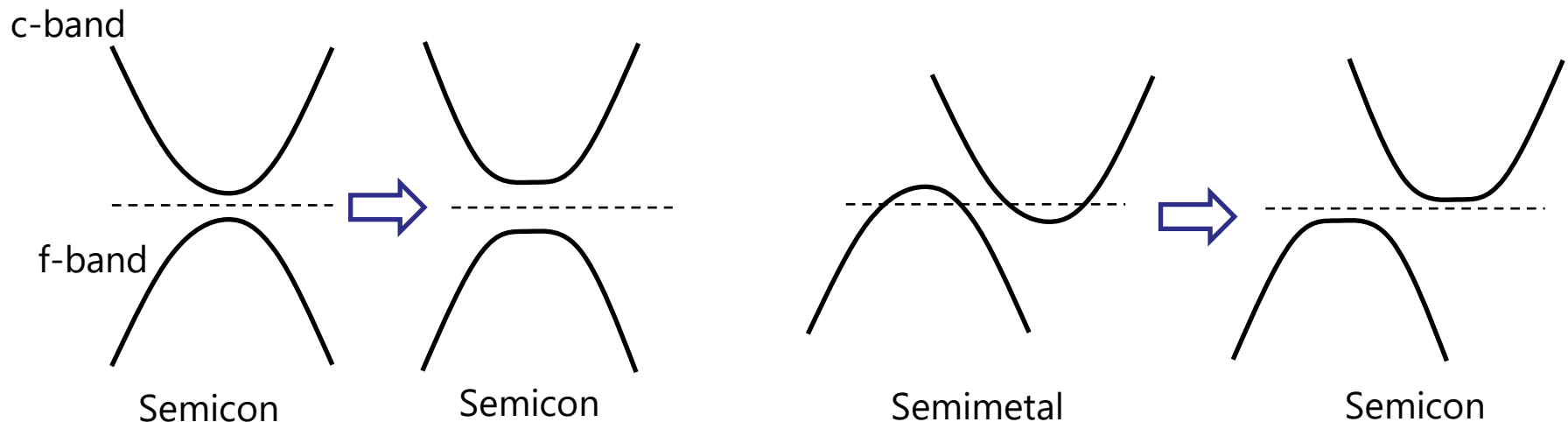
Electron-Hole binding energy  $>$  band gap

Condensation of macroscopic number of excitons

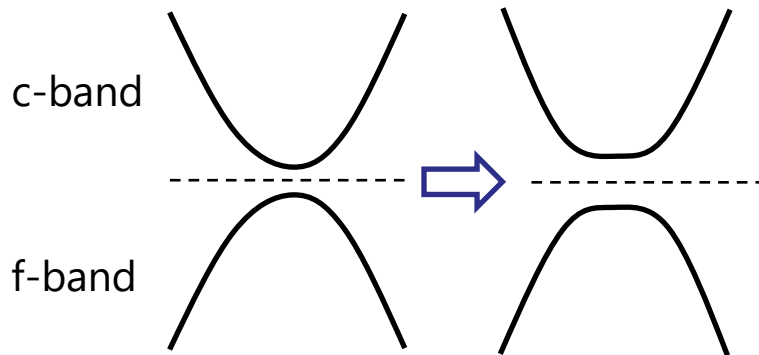
Mott(61) Knox (63) Keldysh(65), Jerome-Rice-Khon (1967)

Halperin, Rice, Solid State Physics, 21 (1968)

Fukuyama (1971), Kuramoto(1978)



# Excitonic Insulators



Different symmetries in c & f bands  
No direct hybridization

~~$$\mathcal{H}_t = - \sum_{\langle ij \rangle \sigma} t \left( c_{i\sigma}^\dagger f_{j\sigma} + H.c. \right)$$~~

Spontaneous symmetry  
breaking

$$c^\dagger c f^\dagger f \rightarrow -c^\dagger f \langle f^\dagger c \rangle$$

Order parameter

$$|EI\rangle \sim N^{-1} \sum_i \left( u + v c_i^\dagger f_i \right) |0\rangle$$

Analogy with Superconductivity

Non-conserved

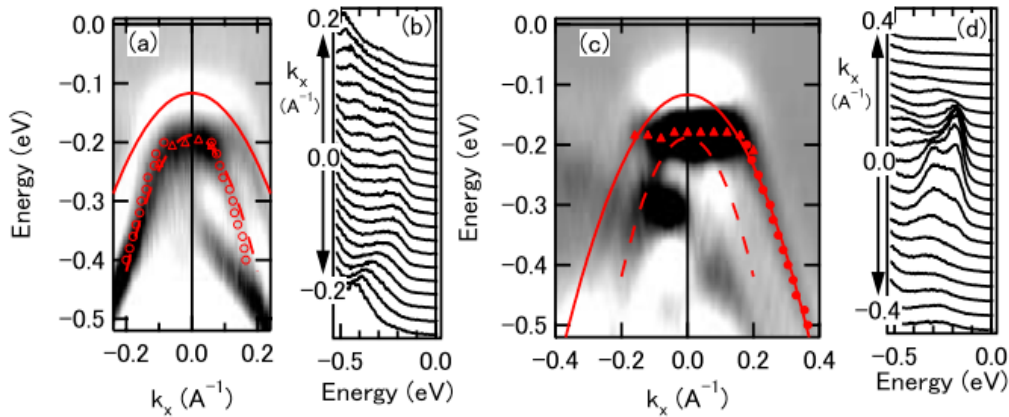
$$\langle f^\dagger f \rangle - \langle c^\dagger c \rangle \quad (EI)$$

$$\langle f^\dagger f \rangle + \langle c^\dagger c \rangle \quad (SC)$$

# Excitonic Insulators

## Ta<sub>2</sub>NiSe<sub>5</sub>

- Flat dispersion observed in ARPES

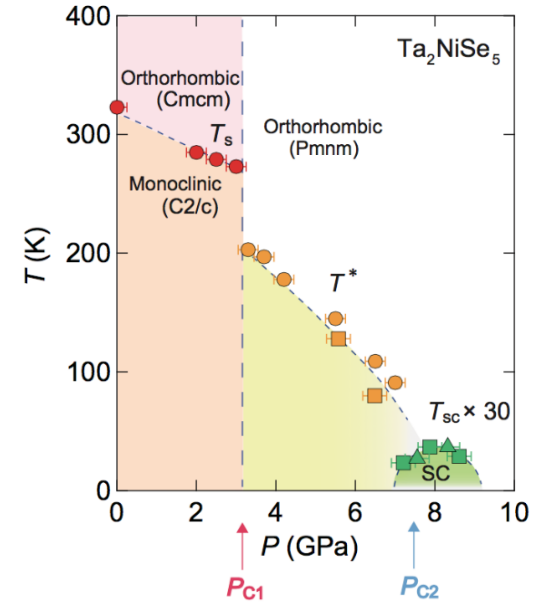


Y. Wakisaka et al., PRL 103, 026402 (2009).

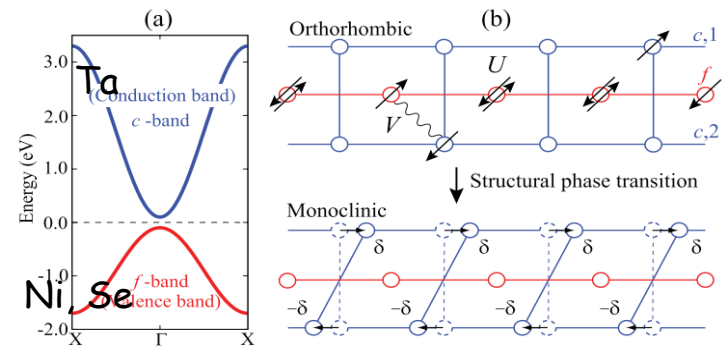
Y. Wakisaka et al., J. Supercond. Nov. Magn. 25, 1231 (2012).

T. Kaneko, T. Toriyama, T. Konishi, and Y. Ohta, PRB 87, 035121 (2013).

T. Kaneko and Y. Ohta, PRB 90, 245144 (2014).



図：Ta<sub>2</sub>NiSe<sub>5</sub>の圧力-温度相図



Approach from Band Ins.

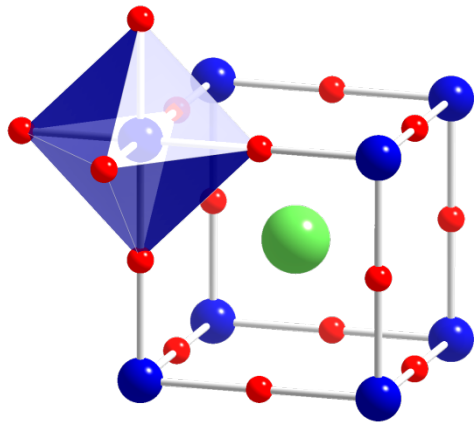
Mott physics / Mottness (?)

## 1T-TiSe<sub>2</sub>

J. Ishioka et al, PRL. 105, 176401 (2010).

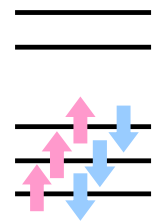
H. Watanabe, K. Seki, and S. Yunoki, PRB 91, 205135 (2015).

# Perovskite cobaltites

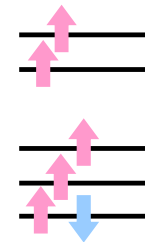


Spin state degree of freedom

$\text{Co}^{3+}$   
( $d^6$ )



Low spin  
LS  
( $S=0$ )

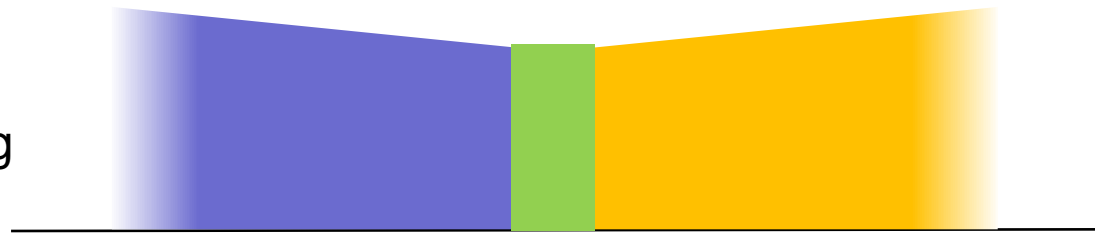


High spin  
(HS)  
( $S=2$ )

Band Insulator

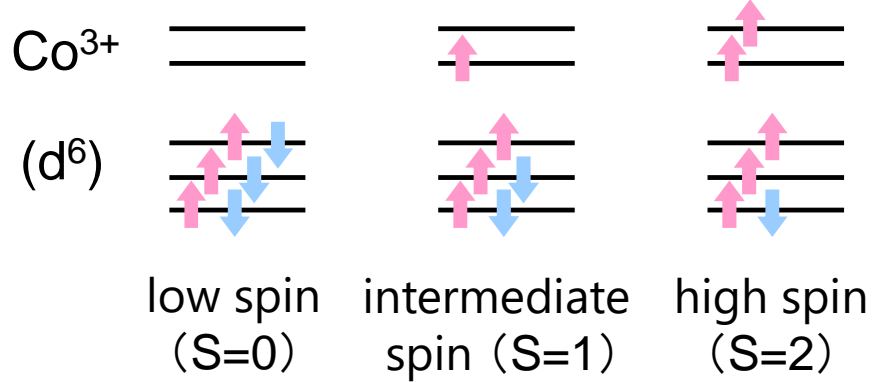
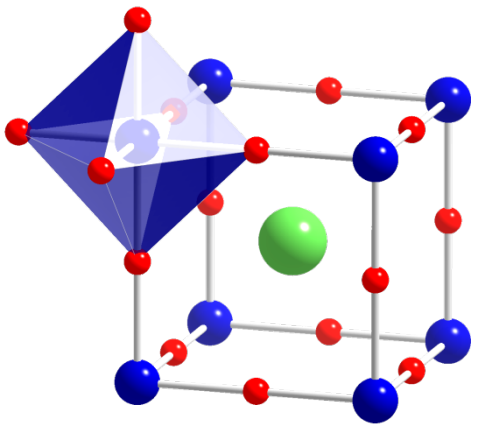
Mott Insulator

Level splitting  
 $\Delta$



Hund coupling  
 $J$

# Theoretical approaches



5 orbital Hubbard model

Weak coupling approach



Hartree-Fock  
Phase diagram  
Collective mode

2 orbital Hubbard model

Strong coupling approach



Low energy effective model

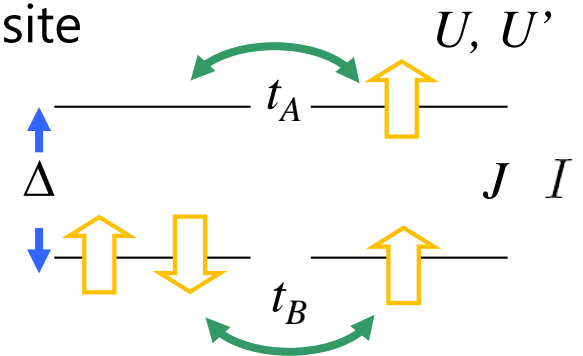


Phase diagram  
Collective mode

# Two band Hubbard with energy difference

$$\mathcal{H} = \mathcal{H}_1 + \mathcal{H}_2$$

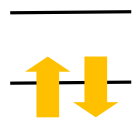
2 electrons/ site



Energy difference

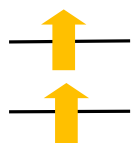
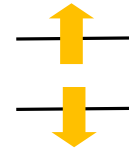
Transfer

$$\mathcal{H}_1 = \Delta \sum_{i,m=\{e_g\}\sigma} c_{im\sigma}^\dagger c_{im\sigma} + \sum_{\langle i,j \rangle, m, \sigma} t_{mm'} \left( c_{im'\sigma}^\dagger c_{jm\sigma} + \text{H.c.} \right)$$



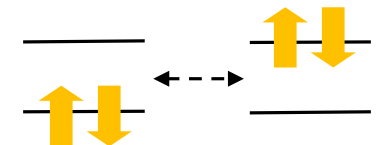
Intra/inter band Coulomb

$$\mathcal{H}_2 = U \sum_{i,m} c_{im\uparrow}^\dagger c_{im\uparrow} c_{im\downarrow}^\dagger c_{im\downarrow} + U' \sum_{i,m \neq m', \sigma \sigma'} c_{im\sigma}^\dagger c_{im\sigma} c_{im'\sigma'}^\dagger c_{im'\sigma'} + J \sum_{i,m \neq m', \sigma \sigma'} c_{im\sigma}^\dagger c_{im'\sigma} c_{im'\sigma'}^\dagger c_{im\sigma'} + I \sum_{i,m \neq m'} c_{im\uparrow}^\dagger c_{im'\uparrow} c_{im\downarrow}^\dagger c_{im'\downarrow}$$



Hund coupling

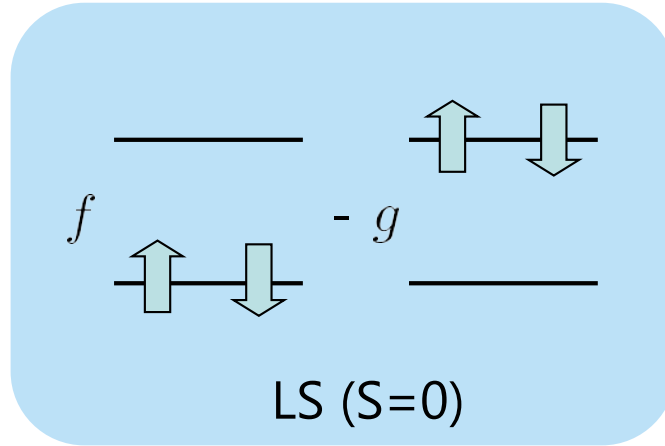
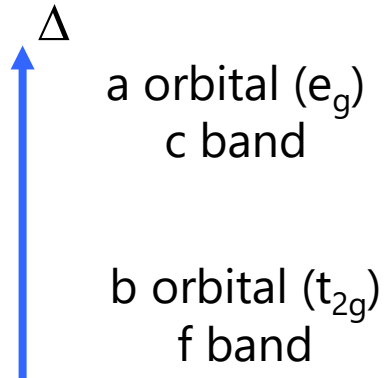
Pair hopping



(sama order of magnitudes)

# Local states

Level splitting



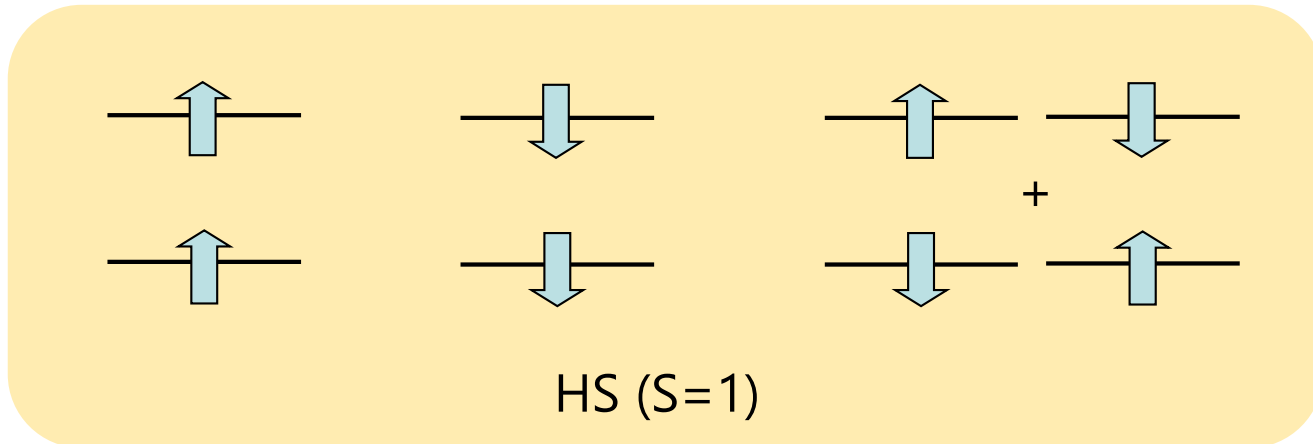
Strong coupling approach

$$\Delta E \sim \Delta, J \gg t$$

$$f \sim 1 \quad g \sim I/\Delta$$

If (pair hopping)  $I=0$ ,  
then  $g=0$

Hund coupling  
 $J$



c.f. C. D. Batista, PRL 89, 166403 (2002)

L. Balents, PRB 62 2346 (2000)

# Pseudo-spins for excitonic state

## Pseudo-spin operator

orbital  
spin

$$\tau_{S_z}^x = (|HS(S_z)\rangle\langle LS| + |LS\rangle\langle HS(S_z)|)$$

$$\tau_{S_z}^y = -i (|HS(S_z)\rangle\langle LS| - |LS\rangle\langle HS(S_z)|)$$

$$\tau_{S_z}^z = |HS(S_z)\rangle\langle HS(S_z)| - |LS\rangle\langle LS|$$

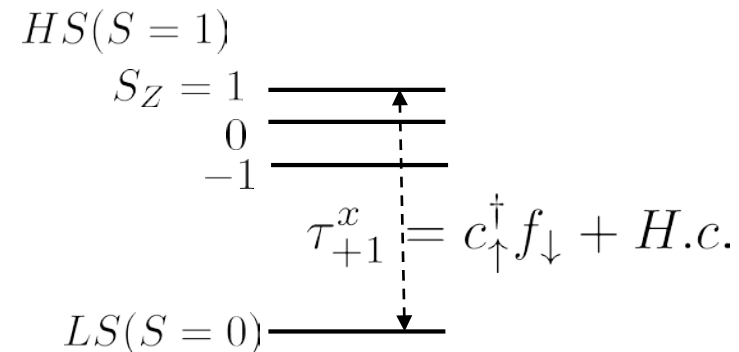
## EI order parameter

$$\sim f^\dagger c + c^\dagger f$$

$$\sim f^\dagger c - c^\dagger f$$

$$\sim f^\dagger f - c^\dagger c$$

$$\tau_{-1}^x = \frac{1}{\sqrt{2}} \begin{array}{c|c} \begin{array}{cc} HS & LS \\ S_z = 1 & 0 & -1 \end{array} & \\ \hline \begin{array}{c} 1 \\ 1 \end{array} \end{array} \quad \tau_X^y = \frac{1}{\sqrt{2}} \begin{array}{c|c} & i \\ \hline -i & i \end{array}$$





# Low energy model

$$\mathcal{H}_{eff} = E_0 - h_z \sum_i \tau_i^z + J_s \sum_{\langle ij \rangle} \vec{S}_i \cdot \vec{S}_j + J_z \sum_{\langle ij \rangle} \tau_i^z \tau_j^z$$

Band gap LS-HS int.

$$+ J_x \sum_{\langle ij \rangle \Gamma} \tau_{i\Gamma}^x \tau_{j\Gamma}^x + J_y \sum_{\langle ij \rangle \Gamma} \tau_{i\Gamma}^y \tau_{j\Gamma}^y$$

Exciton-exciton interaction

$$\tau^x = \sum_{\Gamma} \tau_{\Gamma}^x$$

XYZ-like model with transverse field

If no pair-hopping, then  $J_x = J_y$  XXZ-like model with transverse field

Y. Kanamori, H. Matsueda and S. Ishihara  
Phys. Rev. Lett. 107, 167403 (2011), Phys. Rev. B 86, 045137 (2012)

C. D. Batista, PRL 89, 166403 (2002)  
L. Balents, PRB 62 2346 (2000)

G. Khaliulline, PRL 111 197201(2013)

J. Kuneš and P. Augustinský PRB 89, 115134 (2014), PRB 90, 235112 (2014)

# Symmetry

$$\mathcal{H}_{eff} = E_0 - h_z \sum_i \tau_i^z + J_s \sum_{\langle ij \rangle} \vec{S}_i \cdot \vec{S}_j + J_z \sum_{\langle ij \rangle} \tau_i^z \tau_j^z$$

$$+ J_x \sum_{\langle ij \rangle \Gamma} \tau_{i\Gamma}^x \tau_{j\Gamma}^x + J_y \sum_{\langle ij \rangle \Gamma} \tau_{i\Gamma}^y \tau_{j\Gamma}^y$$

## Symmetry & Conservation

□  $S^x, S^y, S^z$  Total spin angular momentum  $O(3)$

□  $\sum_i (n_i^a + n_i^b)$  Total electron number  $U(1)$

□ If no pair-hopping  $J_x = J_y$  Electron number difference  $U(1)$   
 $\sum_i \tau_i^z \sim \sum_i (n_i^a - n_i^b)$  between c/f bands  
 Relative phase  $a|HS\rangle + e^{i\theta}b|LS\rangle$

□  $\tau_{\Gamma}^x \rightarrow -\tau_{\Gamma}^x$   $\tau_{\Gamma}^y \rightarrow -\tau_{\Gamma}^y$   $Z_2$  Relative sign  $a|HS\rangle \pm b|LS\rangle$

Symmetry of EI order parameter

# Collective mode and symmetry

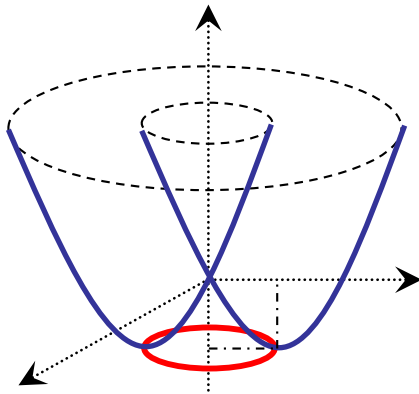
□ If no pair-hopping

$$J_x = J_y$$

Electron number difference  $U(1)$   
between c/f bands

$$\sum_i \tau_i^z \sim \sum_i (n_i^a - n_i^b)$$

Relative phase  $a|HS\rangle + e^{i\theta}b|LS\rangle$



Amplitude (Higgs) mode

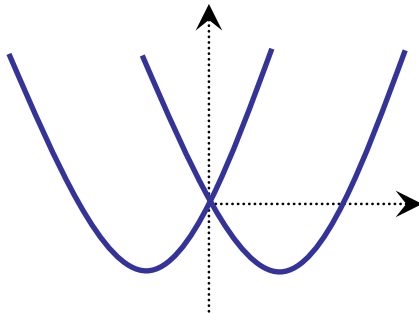
Phase mode : Goldstone mode

(similar to SC)

□ If pair-hopping

$$\tau_{\Gamma}^x \rightarrow -\tau_{\Gamma}^x \quad \tau_{\Gamma}^y \rightarrow -\tau_{\Gamma}^y$$

$Z_2$  Relative sign  $a|HS\rangle \pm b|LS\rangle$



Amplitude (Higgs) mode

# Meaning of sign degree of freedom

From more general point of view

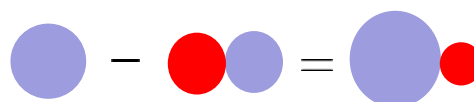
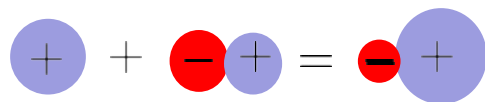
□  $\tau_{\Gamma}^x \rightarrow -\tau_{\Gamma}^x$      $\tau_{\Gamma}^y \rightarrow -\tau_{\Gamma}^y$

$Z_2$

Relative sign

$a|HS\rangle \pm b|LS\rangle$

a-orbital    b-orbital

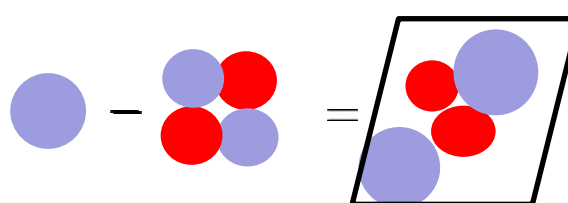
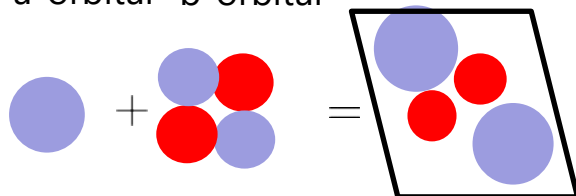


s-wave    p-wave



c.f. electronic ferroelectricity

a-orbital    b-orbital

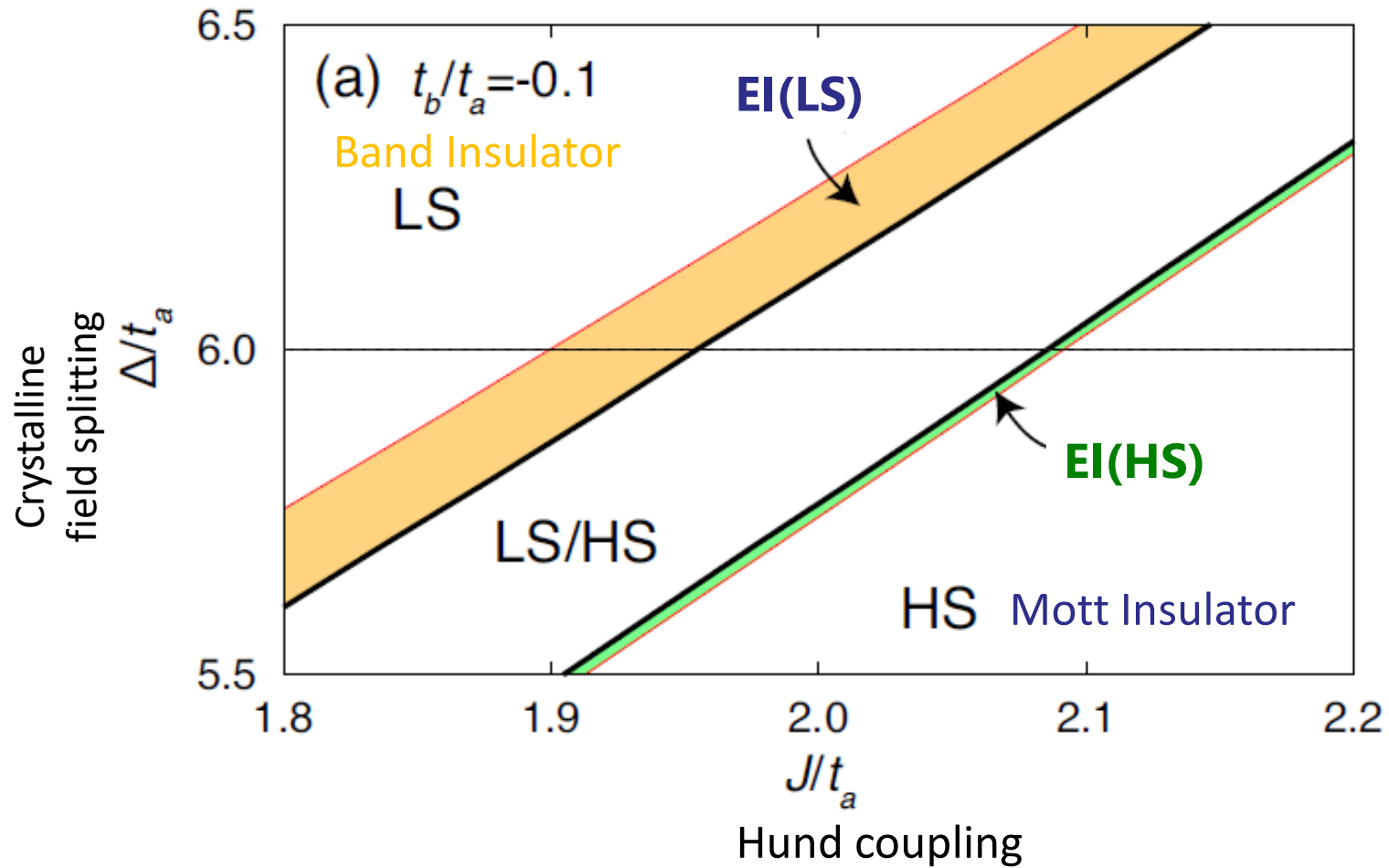


s-wave    d-wave

Ferroelastic  
Cubic-monoclinic

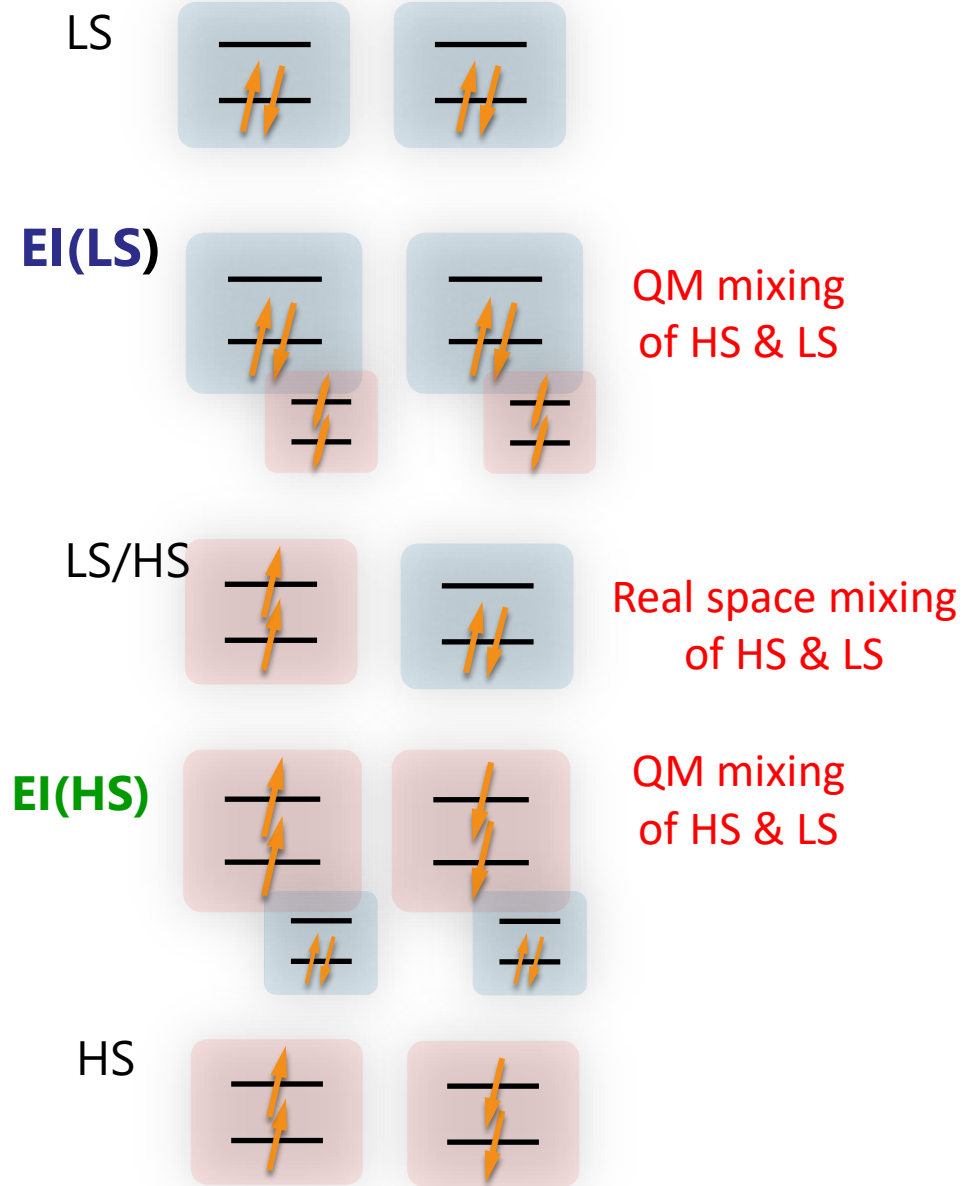
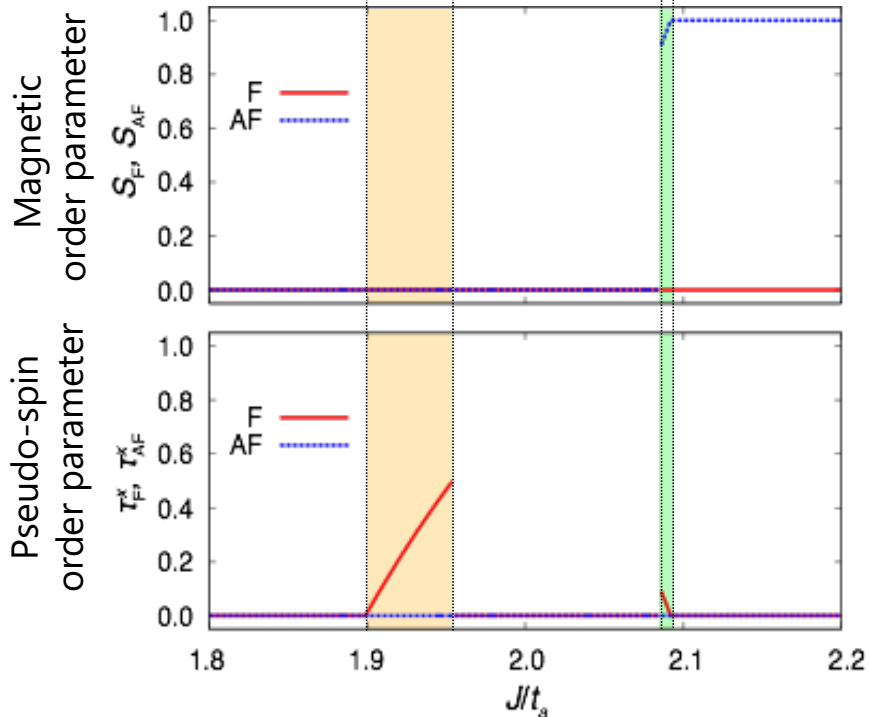
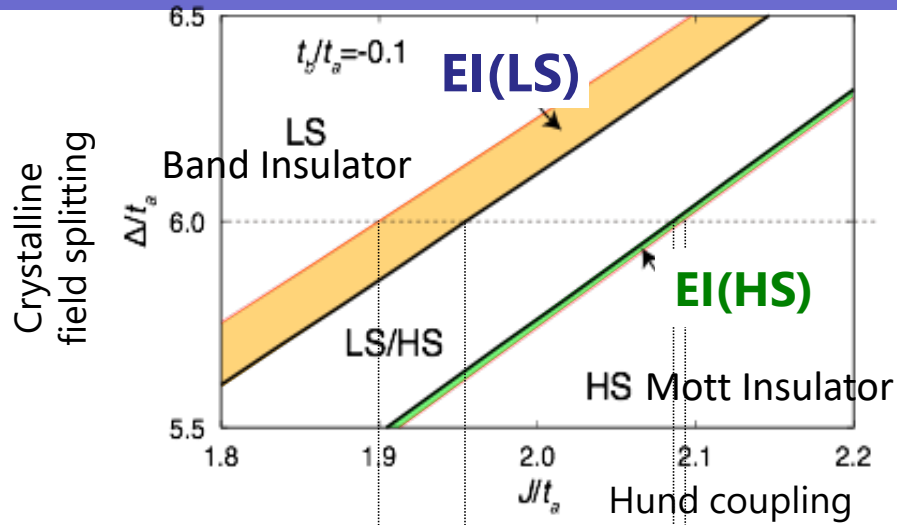
# Phase diagram at T=0

Mean field approximation  
2dim square lattice



# Phase diagram

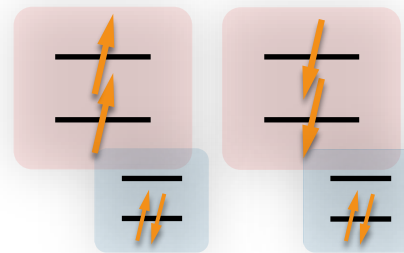
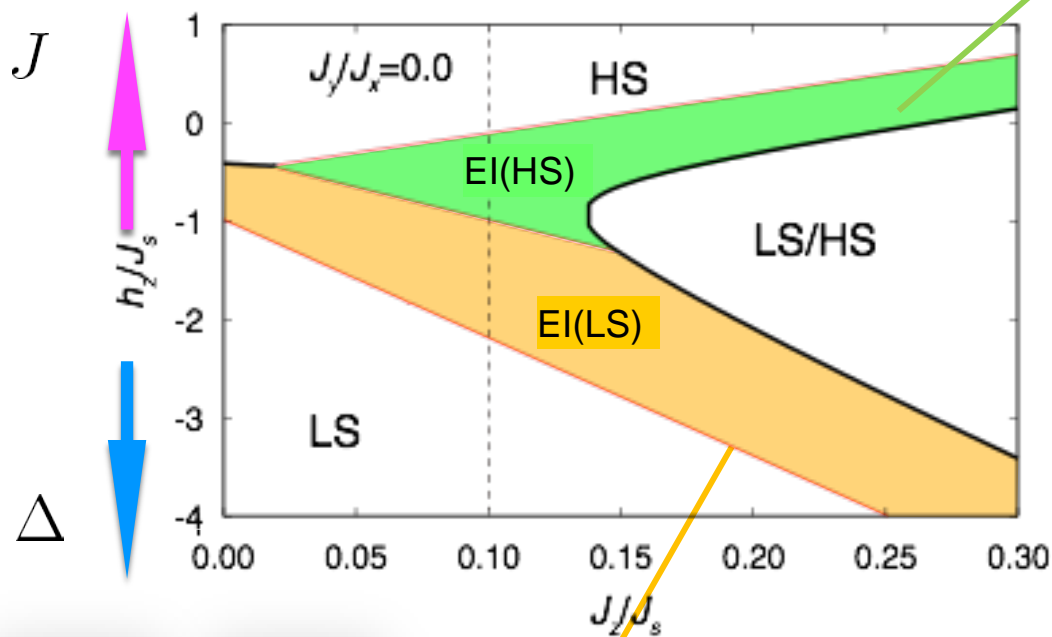
Mean field approximation  
2dim square lattice



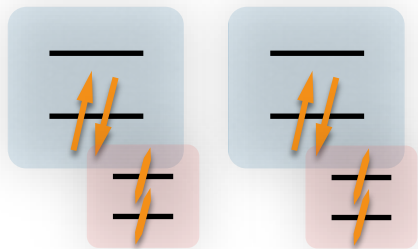
# Two EI phases

$$\mathcal{H}_{eff} = E_0 - h_z \sum_i \tau_i^z + J_s \sum_{\langle ij \rangle} \vec{S}_i \cdot \vec{S}_j + J_z \sum_{\langle ij \rangle} \tau_i^z \tau_j^z + J_x \sum_{\langle ij \rangle \Gamma} \tau_{i\Gamma}^x \tau_{j\Gamma}^x + J_y \sum_{\langle ij \rangle \Gamma} \tau_{i\Gamma}^y \tau_{j\Gamma}^y$$

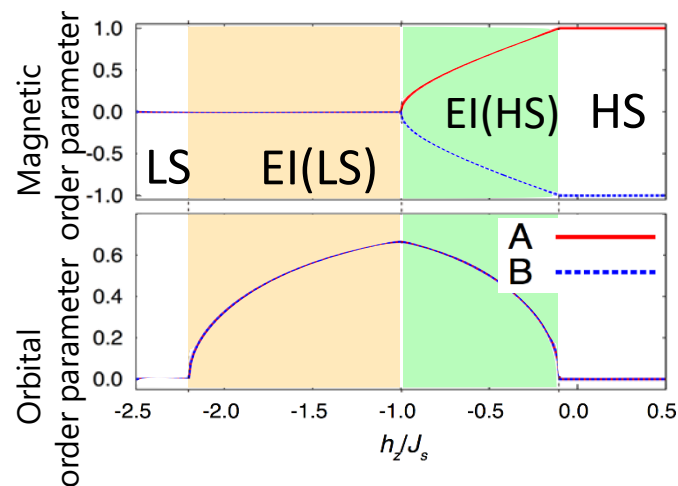
$$|J_x|/J_s = 0.5 \quad J_x < 0, J_y < 0$$



$\langle \tau^x \rangle \neq 0$  Pseudo spin: F  
 $\langle S^z \rangle \neq 0$  Spin: AF



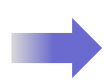
$\langle \tau^x \rangle \neq 0$   $\langle S^z \rangle = 0$   
 $\langle Q^{x^2-y^2} \rangle = \langle (S^x)^2 - (S^y)^2 \rangle \neq 0$   
 Pseudo spin: F  
 Spin: quadrupole (nematic)



# Spin nematic order

$$\langle S^\gamma \rangle = 0$$

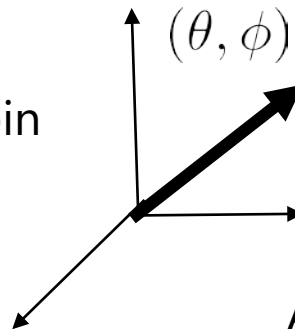
$$\langle S^\alpha S^\beta \rangle \neq 0$$



$$S = 1 \quad |\Psi\rangle = a|1\rangle + b|0\rangle + c|-1\rangle$$

6-2=4 degrees of freedom

Classical vector for spin



2 degrees of freedom

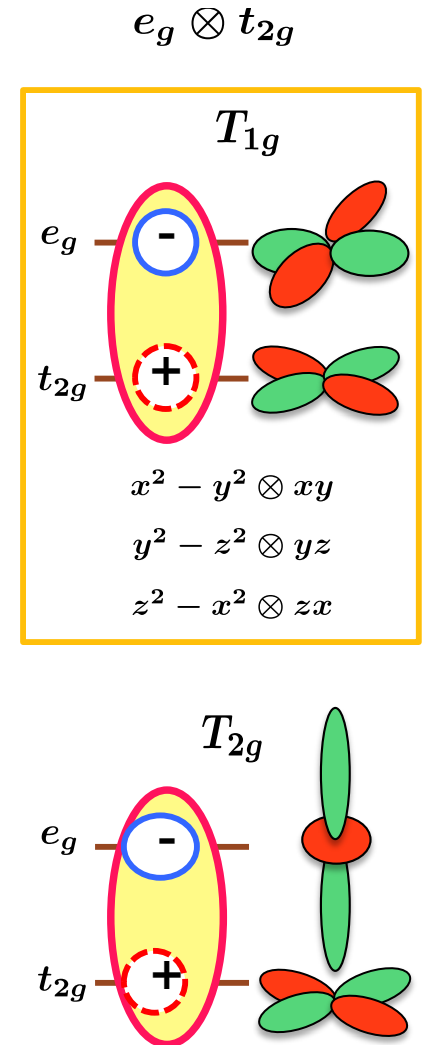
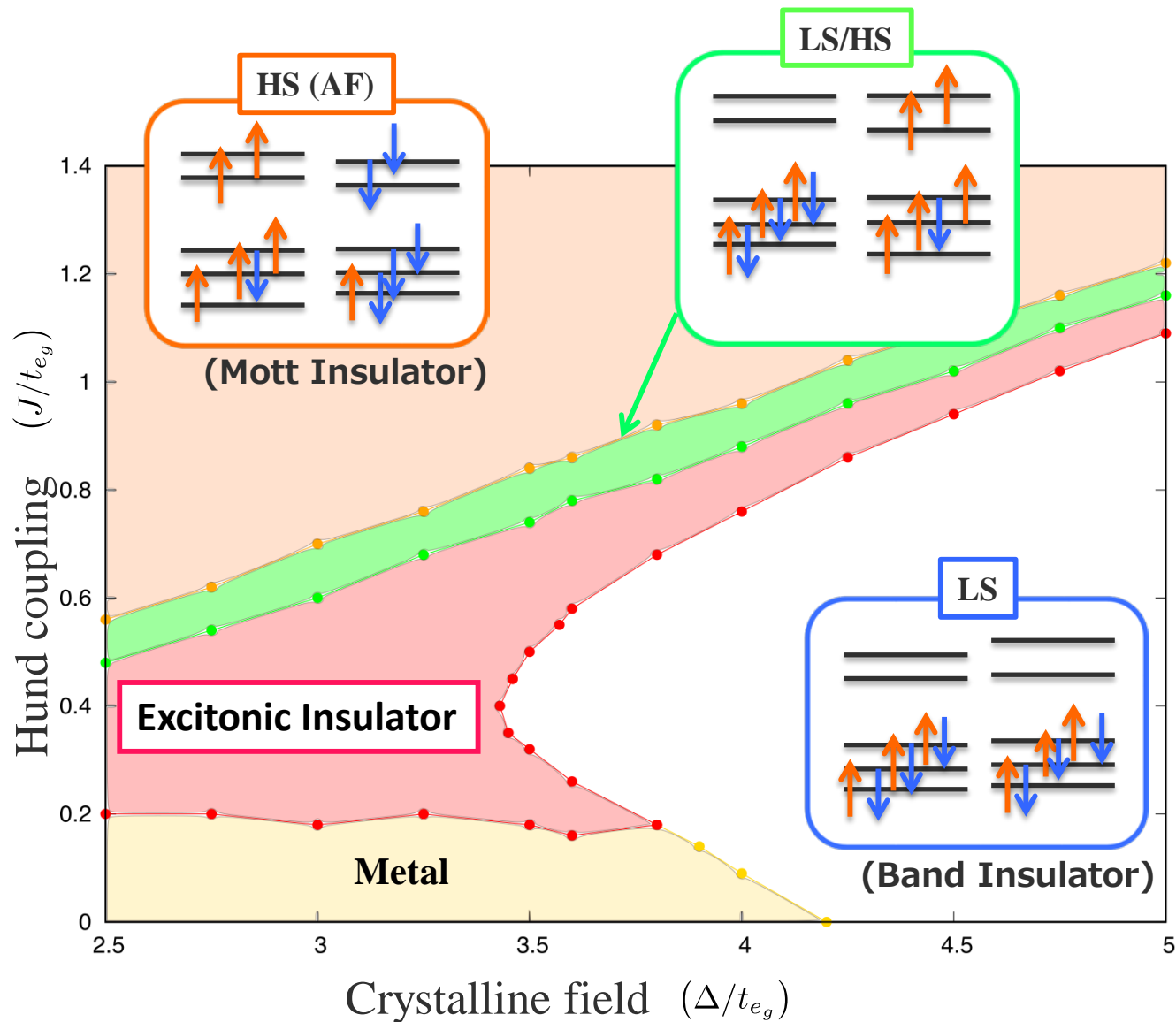
Additional 2 degrees of freedom exist

NiGa<sub>2</sub>S<sub>4</sub>

A. Läuchli, F. Mila, and K. Penc, PRL 97, 087205 (2006).  
 H. Tsunetsugu and M. Arikawa, JPSJ 75, 083701 (2006).

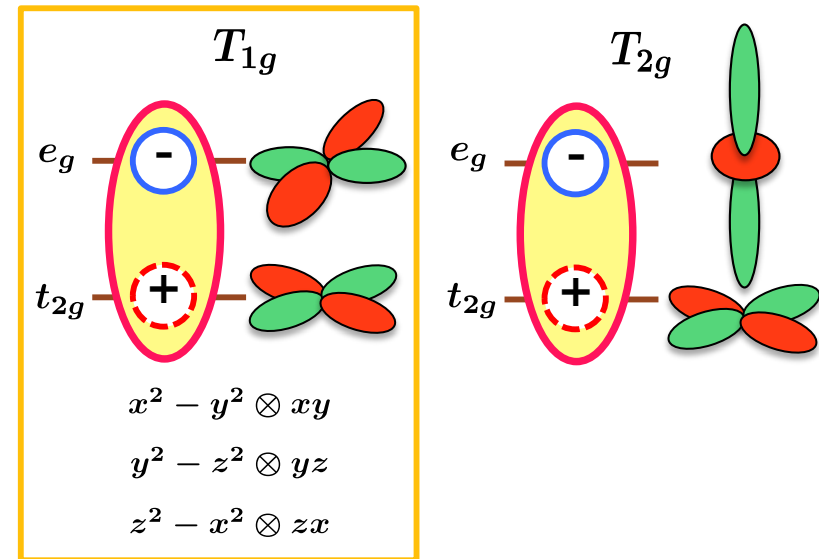
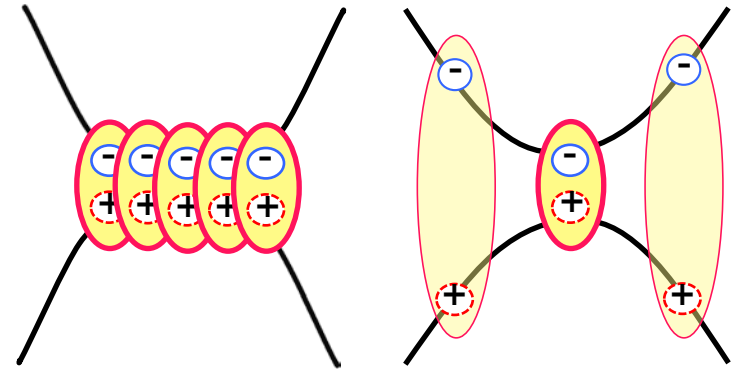
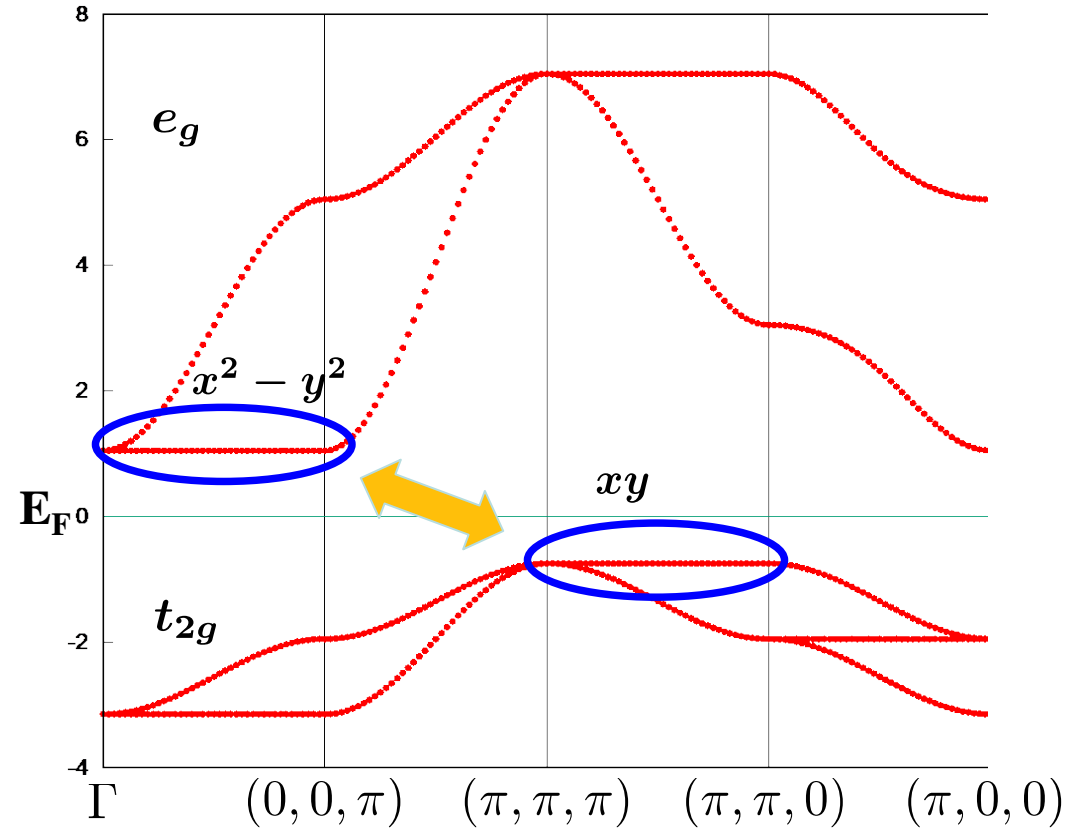


# 5 orbital model

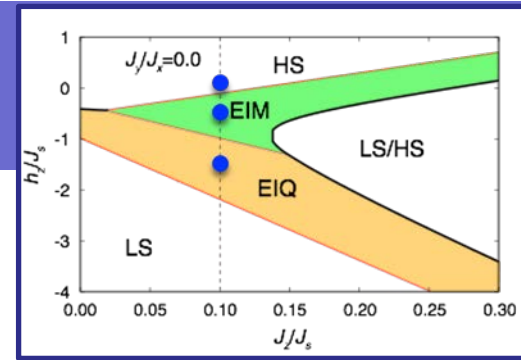


# 5 orbital model

Non-interacting  
electron band



# Magnetic Excitation



2 orbital model

Phys. Rev. B **93**, 205136 (2016)

Dynamical spin correlation function

$$S^{ll}(\mathbf{q}, \omega) = \frac{1}{N} \sum_{ij} \int_{-\infty}^{\infty} dt \langle S_i^l(t) S_j^l \rangle e^{i\omega t - i\mathbf{q} \cdot (\mathbf{r}_i - \mathbf{r}_j)}$$

$$S^{xx}(\mathbf{q}, \omega) = S^{yy}(\mathbf{q}, \omega)$$

AFM Spin wave in  $S_{xx}$  (Transverse)

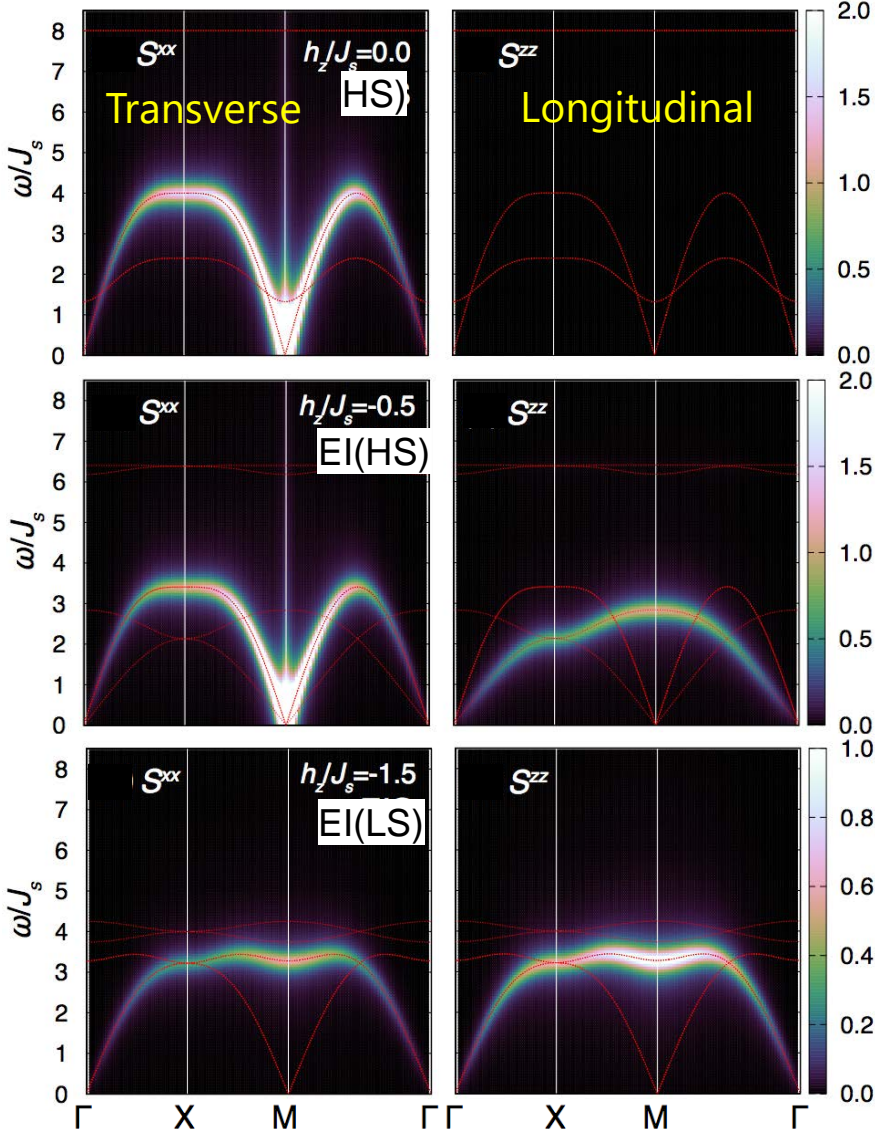
AFM Spin wave

$S^{xx}$ (Transverse) and

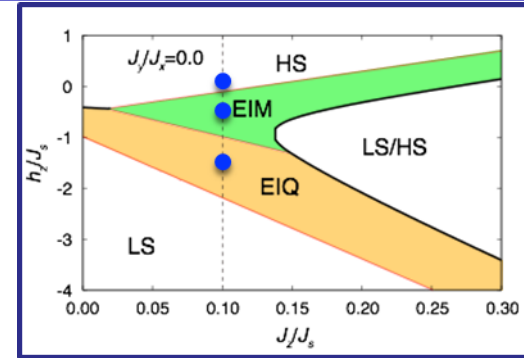
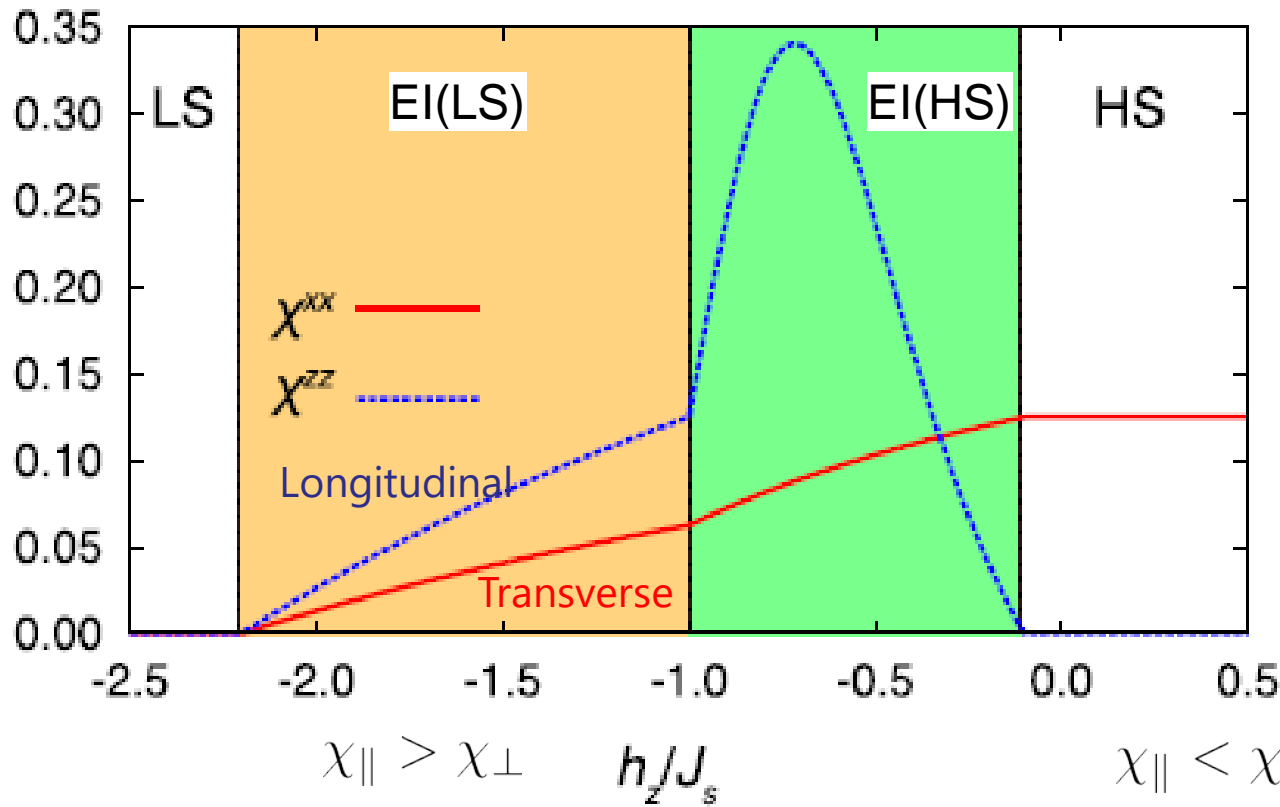
$S^{zz}$ (Longitudinal) (due to LS-HS mixing)

$$a|HS\rangle + b|LS\rangle$$

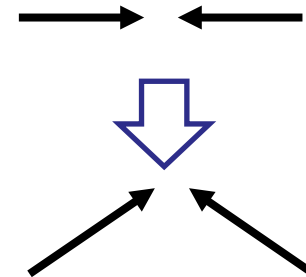
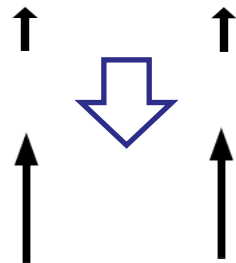
Spin wave in spin nematic order



# Magnetic susceptibility (T=0)

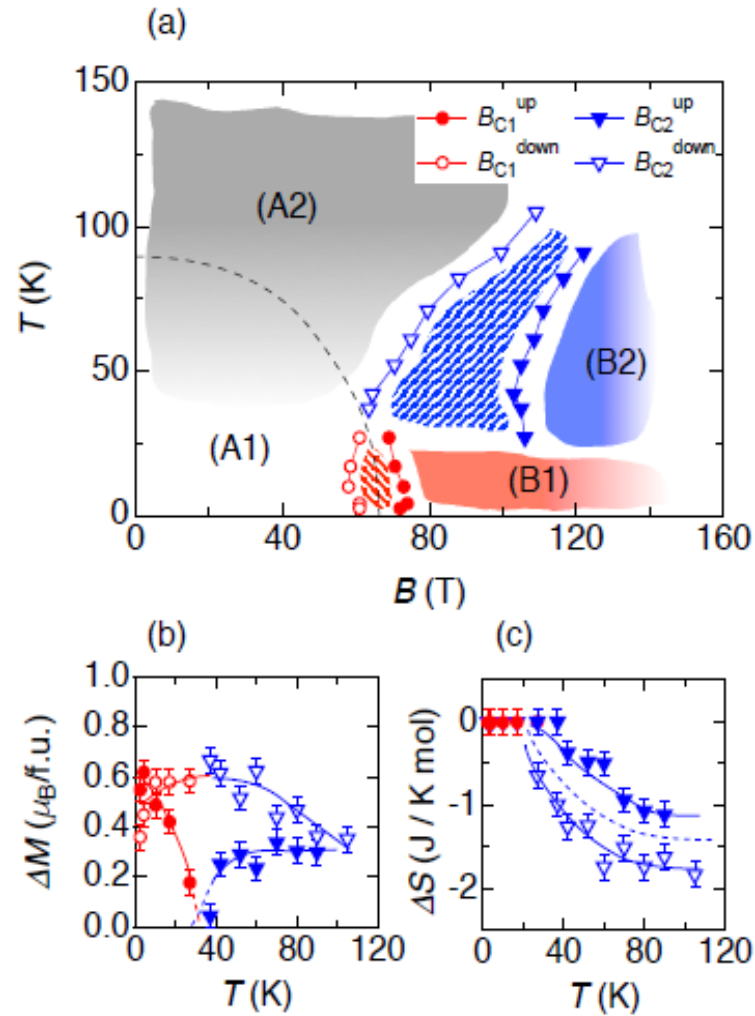
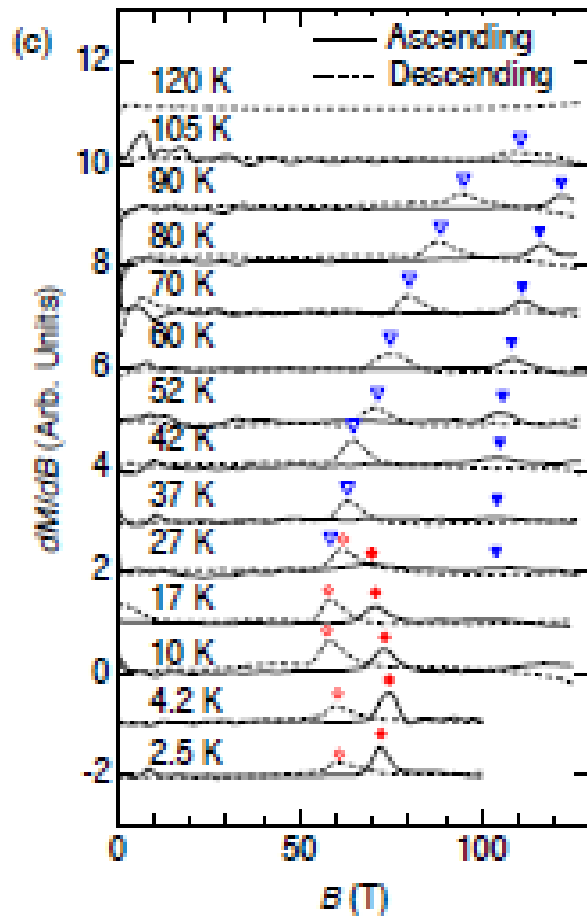


$$a|HS\rangle + b|LS\rangle$$



# Magnetic field effect

LaCoO<sub>3</sub>



See also

J. Kuneš et al. (Sci. Rep. 2016)

Phys. Rev. B 93, 220401 (2016)

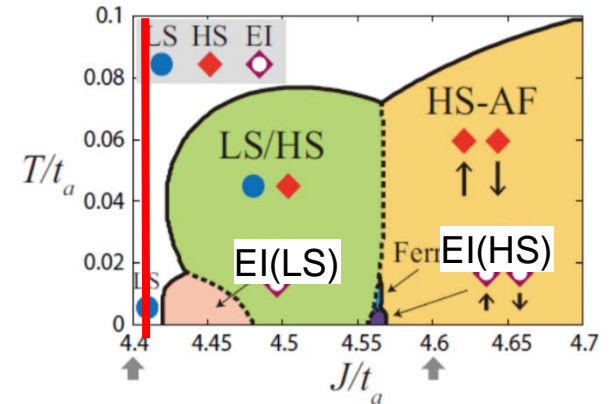
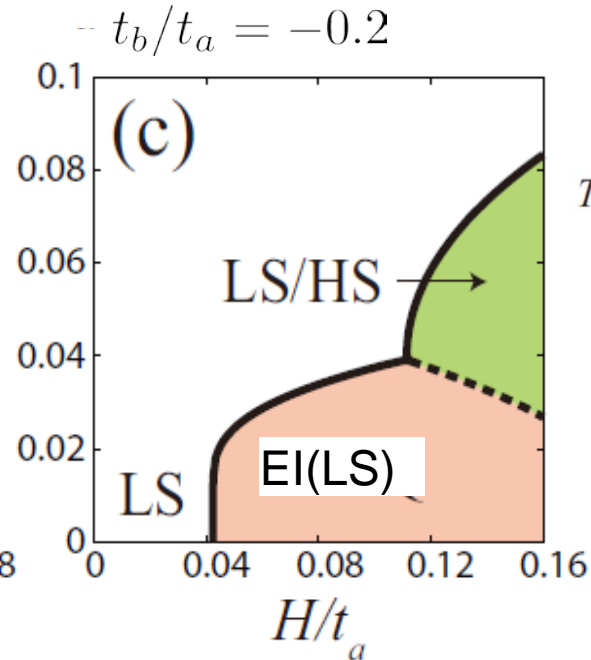
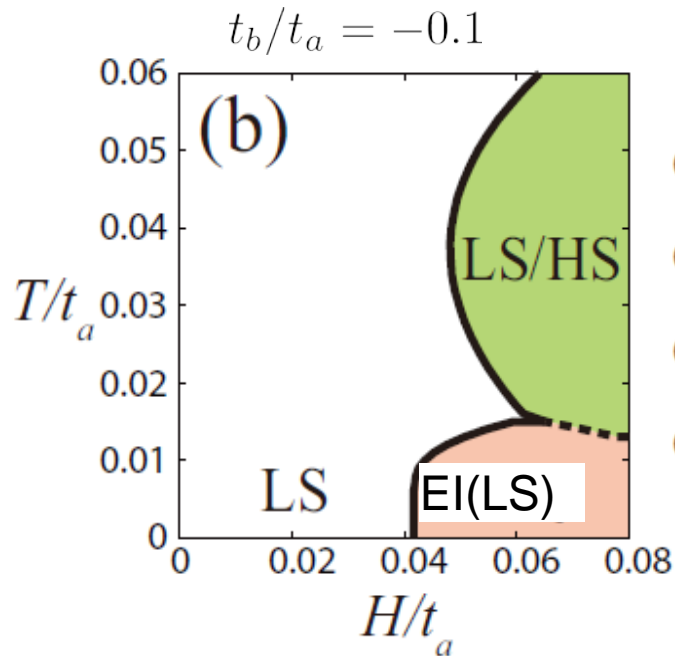
A Ikeda, T Nomura, Y. H. Matsuda, A. Matsuo, K. Kindo, and K. Sato

# Magnetic field induced EI

T. Tatsuno, E. Mizoguchi, J. Nasu, M. Naka, and SI,

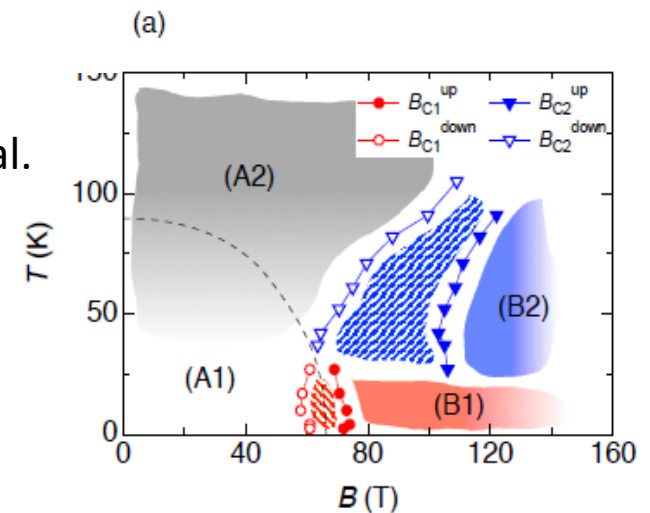
J. Phys. Soc. Jpn. 85, 083706 (2016)

LS GS



Magnetic field induced  
EI & LS/HS

Exp. Ikeda et al.



See also J. Kuneš et al. (Sci. Rep. 2016)

# Summary

Mott Insulator vs. **Band Insulator**: **EI** is a possible candidate

## ■ Ground state

- Two EI phases
- Breaking Z2 symmetry in EI phase  
(In no-pair hopping, U(1))
- Nematic spin order in EI(LS)

## ■ Collective excitations

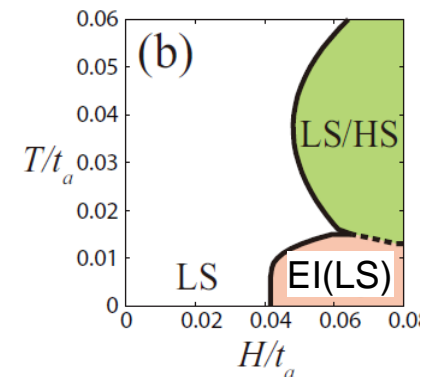
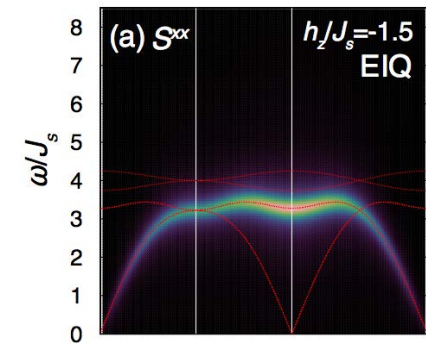
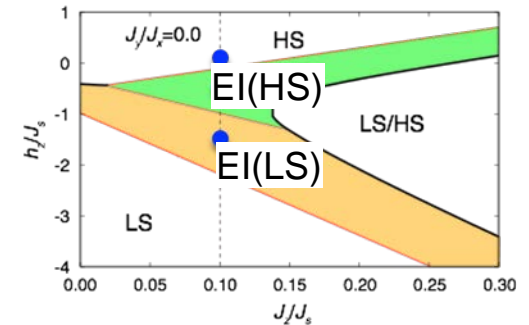
- Magnons : Longitudinal excitation
- Excitonic mode (Higgs mode)

Good targets for  
X-ray / Neutron  
spectroscopies

## ■ Magnetic field effect

- Transverse v.s longitudinal susceptibilities
- H induced EI

Phys. Rev. B **93**, 205136 (2016)  
J. Phys. Soc. Jpn. **85**, 083706 (2016)



# Outline

## [1] Excitonic insulating state in a correlated material

J. Nasu (Tokyo Tech.), M. Naka (Waseda Univ.)

T. Tatsuno (Tohoku Univ.), T. Watanabe (Chiba Tech.)

J. Nasu, T.Watanabe, M.Naka, and SI, Phys. Rev. B **93**, 205136 (2016)

T. Tatsuno, E. Mizoguchi, J. Nasu, M. Naka, and SI,

J. Phys. Soc. Jpn. 85, 083706 (2016)

## [2] Double exchange interaction in non-equilibrium state

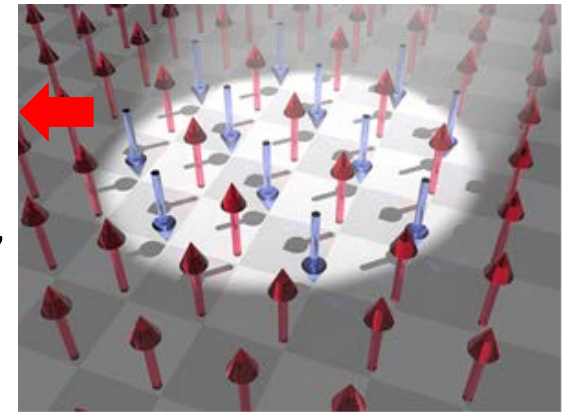
A. Ono (Tohoku Univ.) J. Ohara (Hokkaido Univ.),

Y Kanamori (Tohoku Univ.)

A. Ono and SI, Phys. Rev. Lett. 119, 207202 (2017)

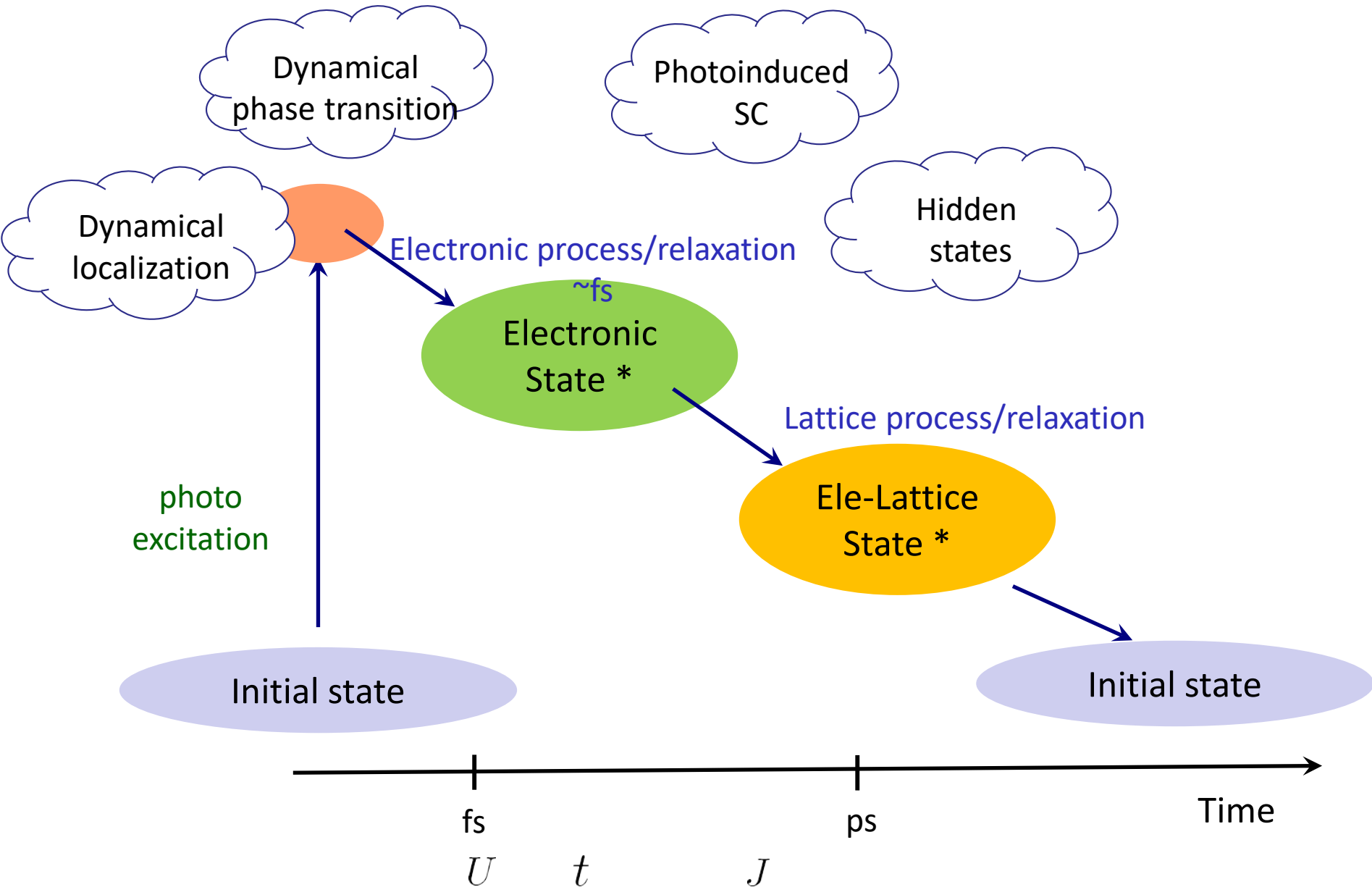
(Editors' suggestion)

J. Ohara, Y. Kanamori and SI, Phys. Rev. B 88, 085107 (2013)





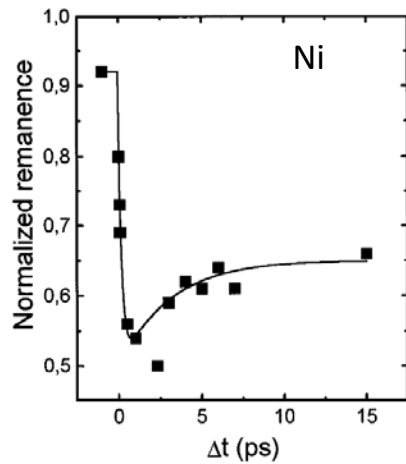
# Non-eq. dynamics in correlated materials



# Optical manipulation of magnetism

## Ultrafast demagnetization

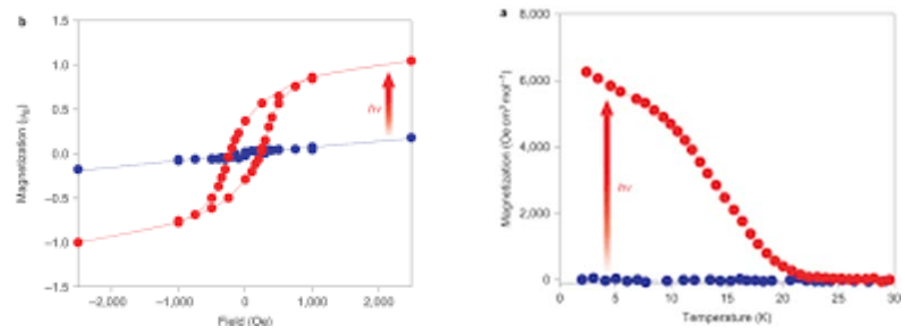
E. Beaurepaire, J. Merle, et al. PRL (1996)



## Light induced spin crossover

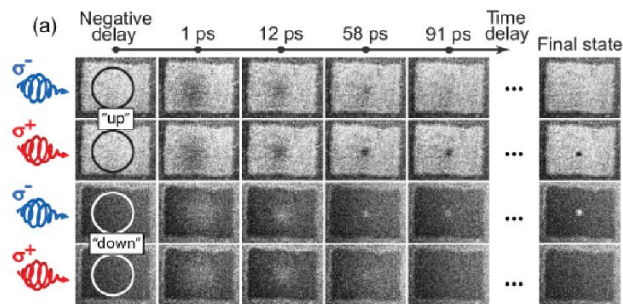
S. Ohkoshi, et al. Nat. Chem. (2010)

$\text{Fe}_2[\text{Nb}(\text{CN})_8] \cdot (4\text{-pyridinealdoxime})_8 \cdot 2\text{H}_2\text{O}$



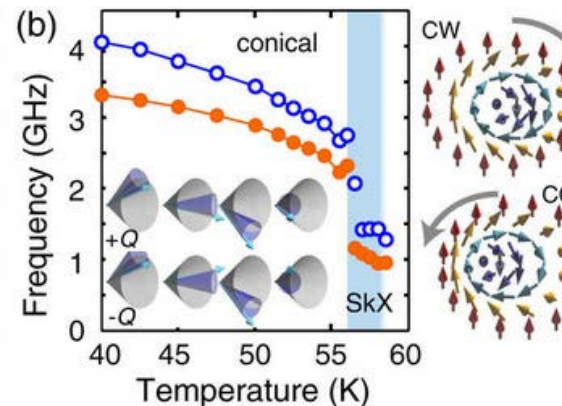
## Ultrafast magnetization reverse

K. Vahaplar, et al. PRL (2009)  $\text{Gd}_{22}\text{Fe}_{68.3}\text{Co}_{9.8}$



## Optical excitation of skyrmion

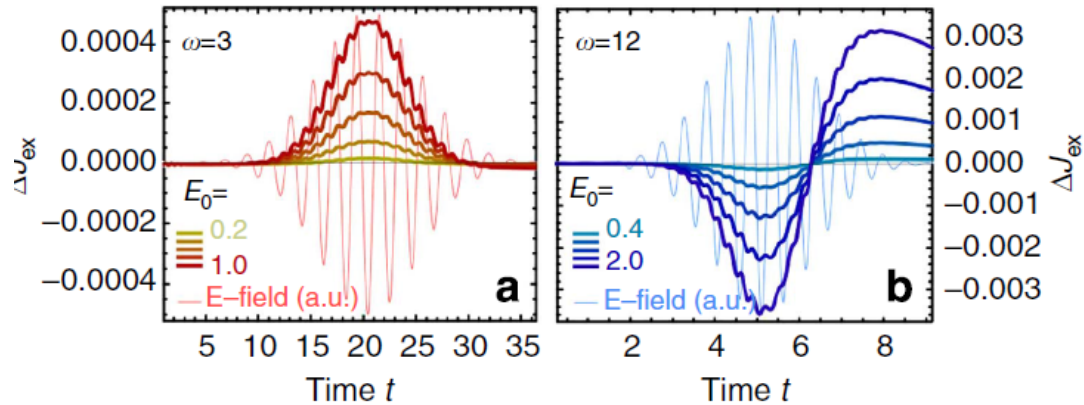
N. Ogawa, et al. Sci. Rep. (2015)  $\text{Cu}_2\text{OSeO}_3$



# Manipulation of exchange interaction

## Superexchange interaction in Mott insulator

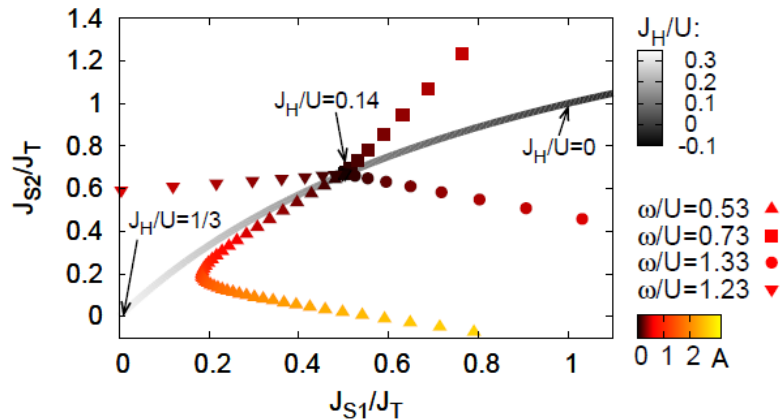
J. H. Mentink, K. Balzer, and M. Eckstein, Nat. Commun. (2015).



$$J S_i S_j$$

## Spin-orbital exchange interaction in orbital degenerate Mott insulator

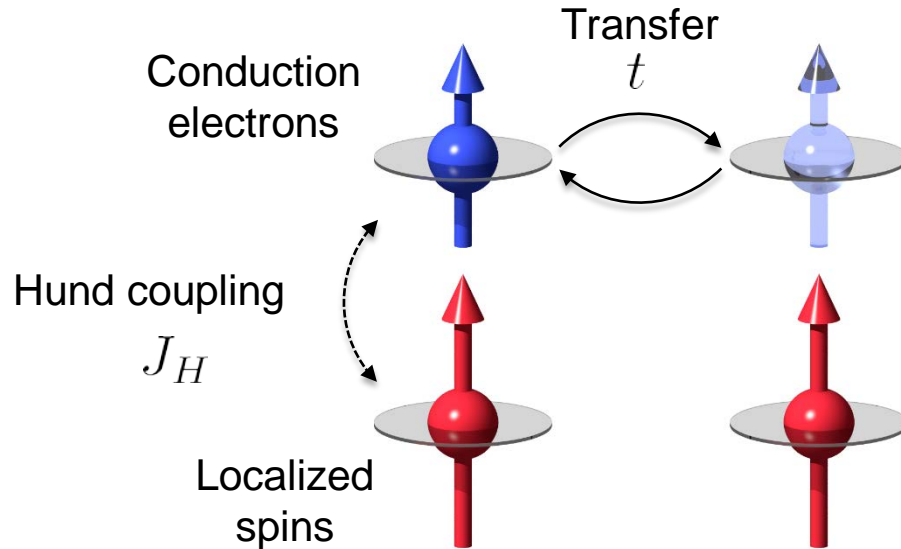
M. Eckstein, J. H. Mentink, and P. Werner, arXiv:1703.03269v1



$$J(T_i T_j)(S_i S_j)$$

# Double exchange interaction

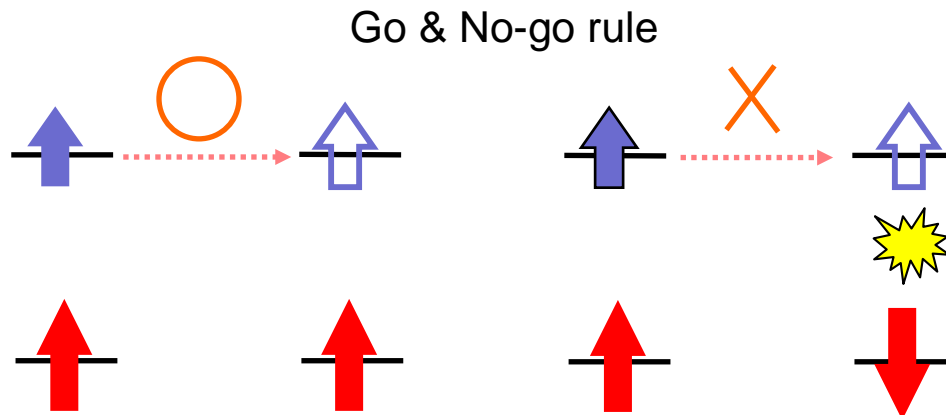
Zener ('51), Anderson-Hasegawa ('55), de Gennes ('59)  
Metallic magnet



$$J_H \gg t$$

$$t_{eff} = t \cos \frac{\theta}{2}$$

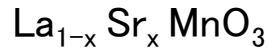
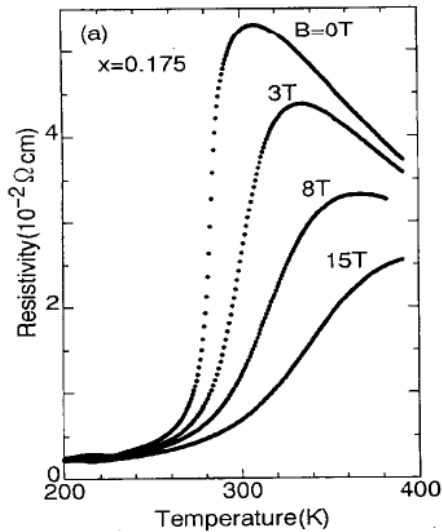
$$JS_i S_j \propto \cos \theta$$



Magnetism (Spin)  
 $\updownarrow$   
 Conduction (Electron)

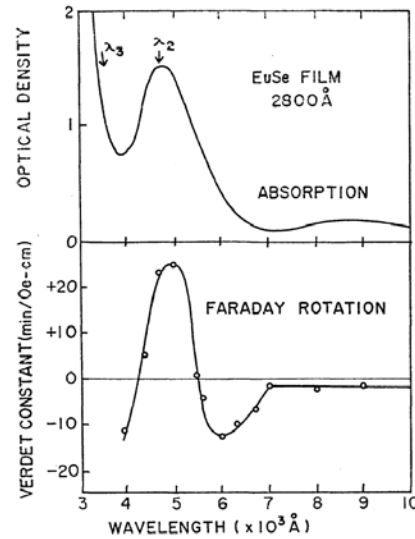
# DEX interaction in solids

## Colossal Magneto Resistance



Urushibara et al. JPSJ

## Magnetic semiconductor



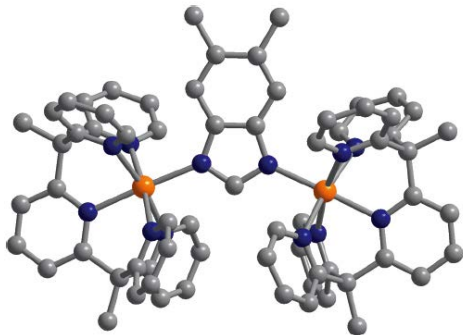
EuSe

From  
 A. Yanase, and T. Kasuya,  
 J. Phys. Soc. Jpn. 25,(1968).

And more

## Molecular magnet

$[(\text{PY5Me}_2)\text{2V}_2(\text{m-5,6-dmbzim})]_{31}$  in  $14.3.5\text{MeCN.Et}_2\text{O}$

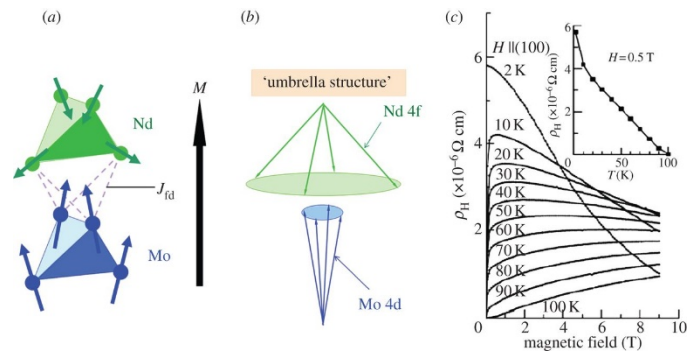


B. Bechlars, et al. Nat. Chem. 2, 362 (2010).

## Anomalous Hall effect

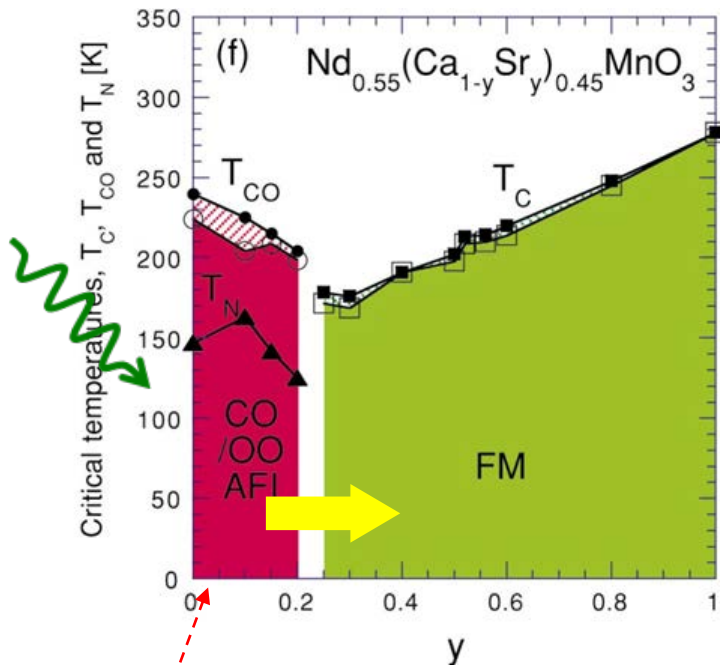
Y. Taguchi, et al. 2001 Science 291

$\text{Nd}_2\text{Mo}_2\text{O}_7$



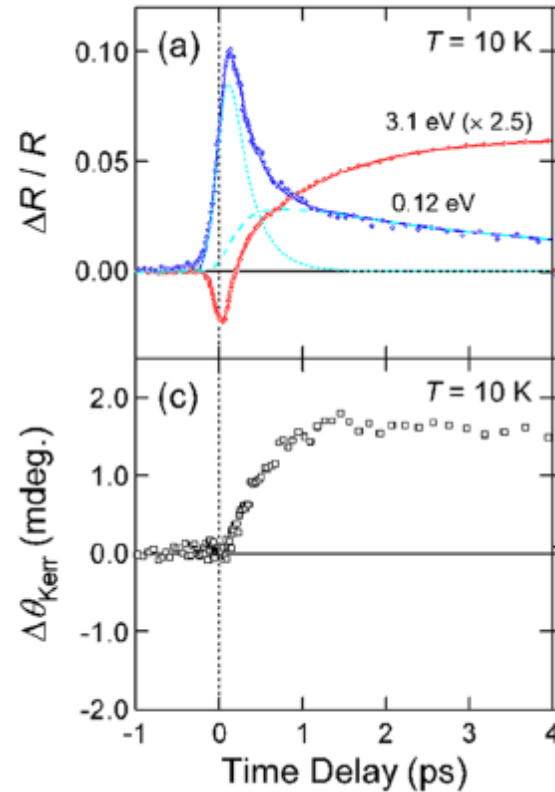
# Photo irradiation in DEx system

Tomioka-Tokura et al. PRB ('04)



AFM exchange interaction  
Coulomb interaction  
in addition to original DEx interaction

## Optical pump-probe



Fiebig, Miyano,  
Tokura, Okamoto,  
Koshihara  
and many

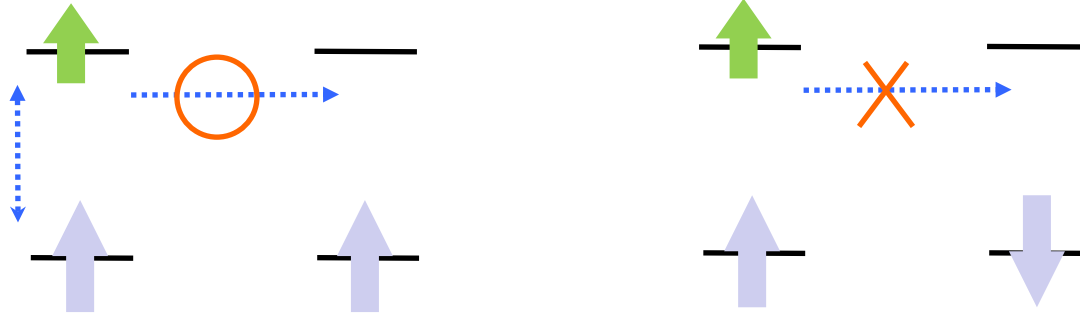
$\text{Gd}_{0.55}\text{Sr}_{0.45}\text{MnO}_3$ , Matsubara et al.

also  $\text{Nd}_{0.5}\text{Sr}_{0.5}\text{MnO}_3$ , Miyasaka et al  
Ogasawara et al. ('05)

Photo-induced  
AFM/CO to metallic FM

# Photo irradiation as a carrier doping

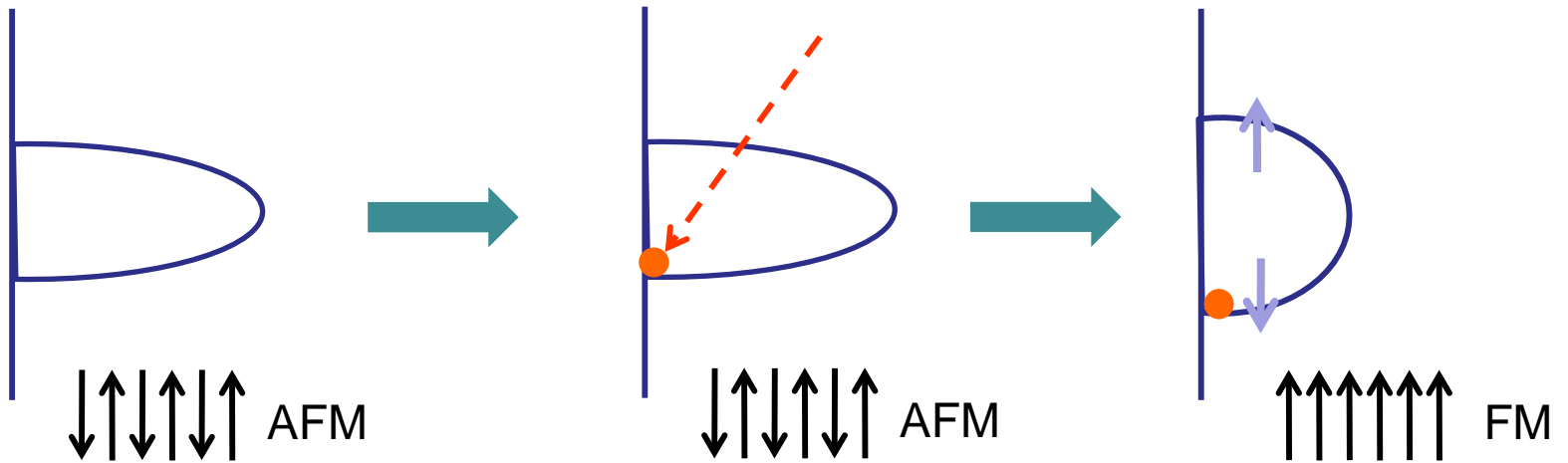
Conduction electron



Hund coupling

Local spin

Carrier doping

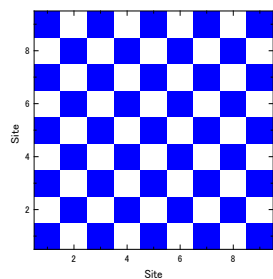
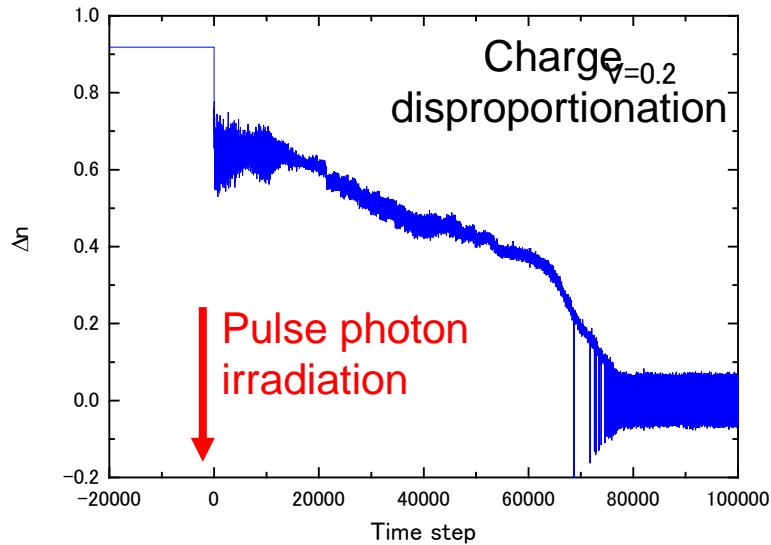


# Theoretical demonstration

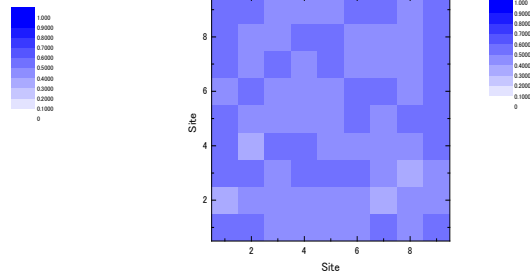
K. Satoh and SI  
JMMM 130, 798-800 (2007)

H. Matsueda & SI, JPSJ76, 083703, ('07)  
Y. Kanamori, H. Matsueda and SI PRL 103, 26740 ('09)  
Y. Kanamori, H. Matsueda and SI, PRB 82, 115101 ('10)

## Real time simulation



AFM-CO insulator



FM metal

## Pump-probe spectra

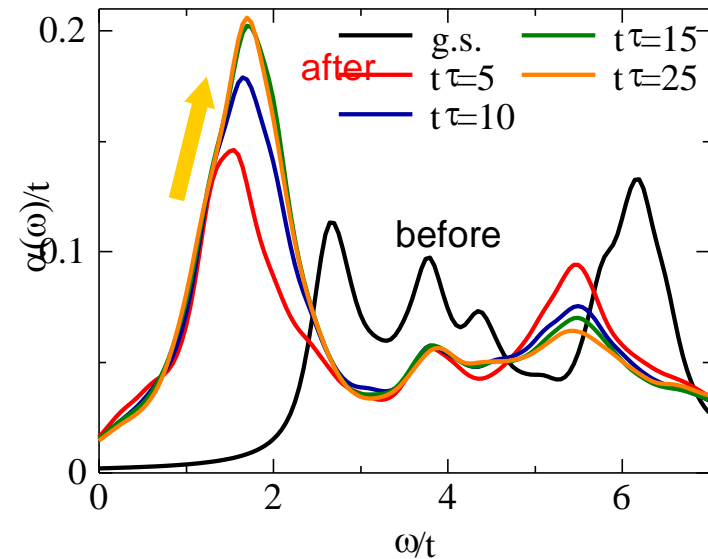
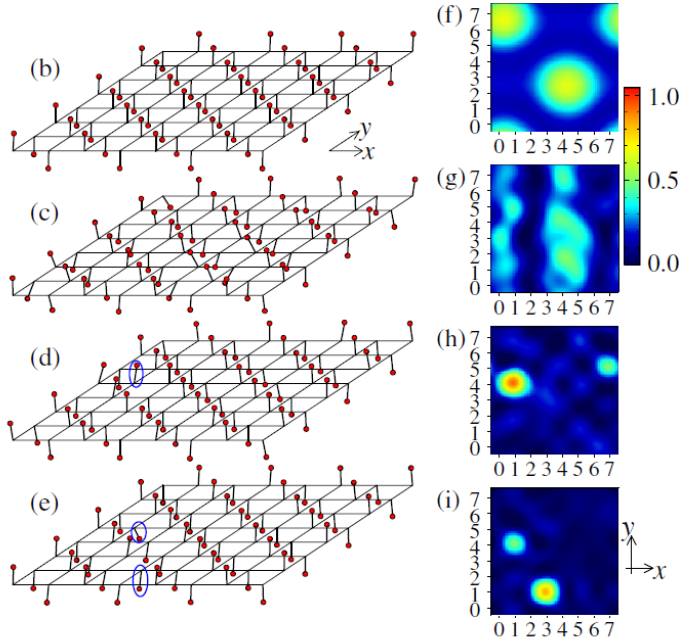
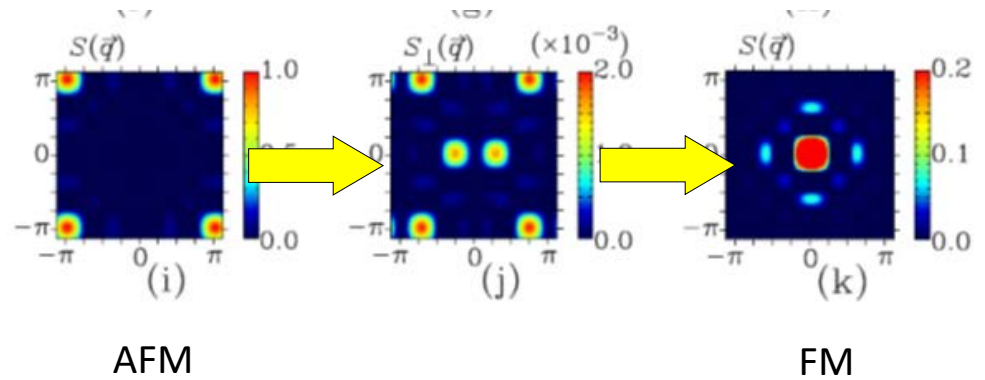
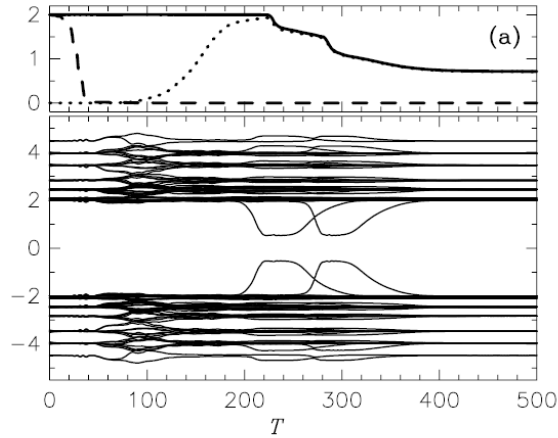


Photo-induced  
AFM/CO to metallic FM



# Theoretical demonstration

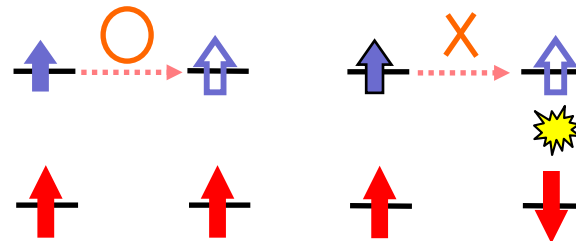
Koshibae-Furukawa-Nagaosa PRL 03, 266402 (2009)  
EPL 94, 27003 (2011)



Weak excitation ( $\sim 1$  photon/100sites)

AFM to FM

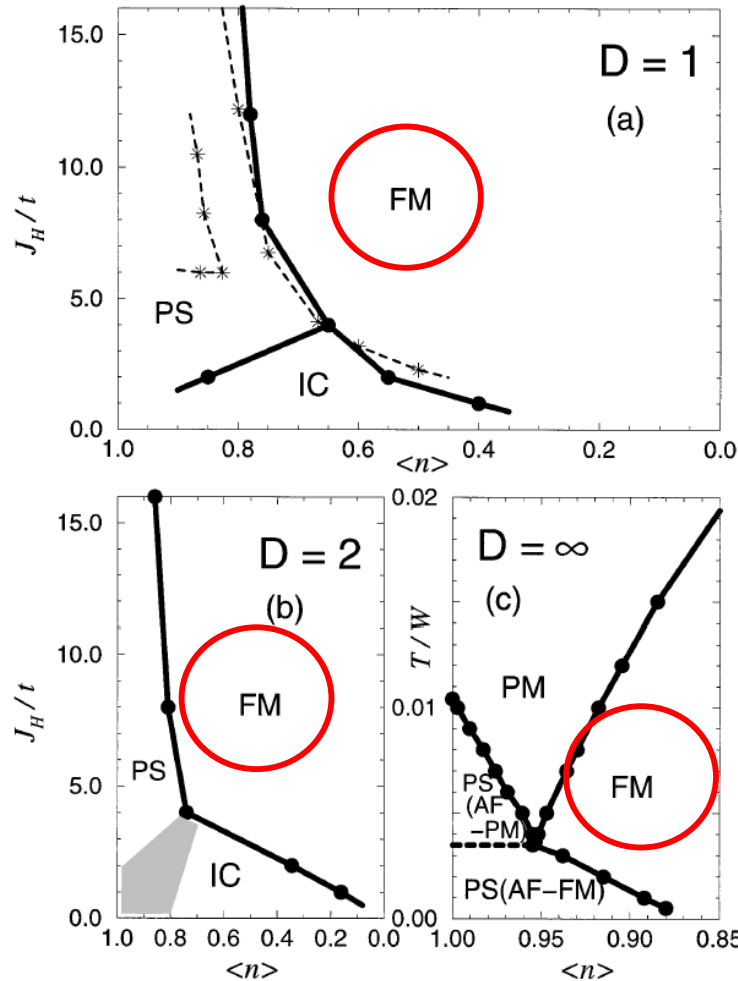
Photodoped carrier motion  $\rightarrow$  FM



# Ground state in DEx model

Yunoki et al. PRL (1998)

DEx model



$$H = -t \sum_{\langle i,j \rangle \sigma} c_{i\sigma}^\dagger c_{j\sigma} - 2J_H \sum_i \mathbf{S}_i \cdot \mathbf{s}_i$$

What is happen by  
strong excitation in FM phase

?

$$n = 1 - x$$

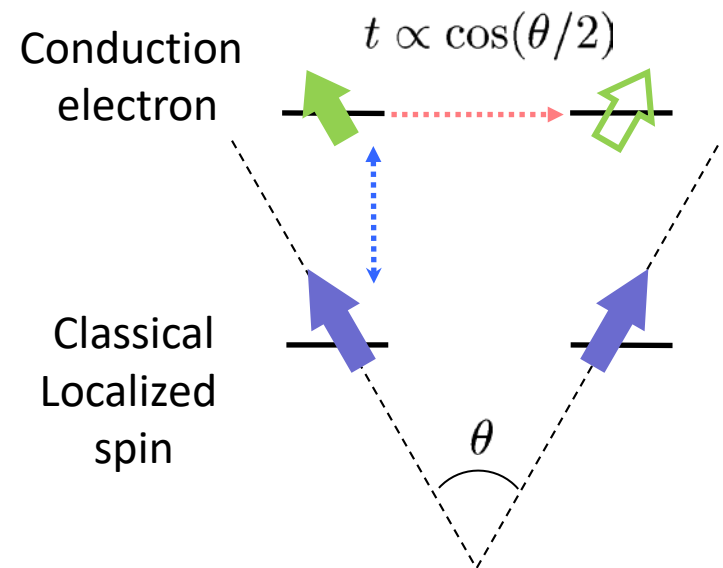
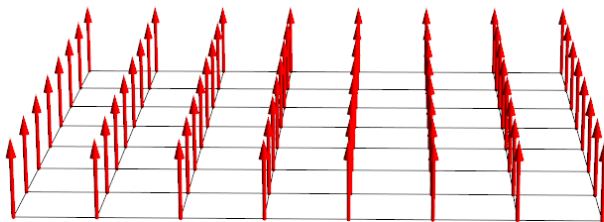
Electron # / site

# DEX interaction revisit

## (pure) Double Exchange Model

$$H = -t \sum_{\langle i,j \rangle \sigma} c_{i\sigma}^\dagger c_{j\sigma} - 2J_H \sum_i \mathbf{S}_i \cdot \mathbf{s}_i$$

- No AF interaction
- Classical localized spin
- FM metallic GS (mainly 1/4 filling)



# Model & Method

## Conduction electrons

2-dimensional square

$N = 8 \times 8 - 12 \times 12$  sites (PBC/APBC)

Wave function

$$|\Psi(\tau)\rangle = \prod_{\nu=1}^{N_e} \psi_{\nu}^{\dagger}(\tau)|0\rangle$$

$$H(\tau) = \sum_{\nu} \varepsilon_{\nu}(\tau) \tilde{c}_{\nu}^{\dagger}(\tau) \tilde{c}_{\nu}(\tau)$$

Time evolution

$$\psi_{\nu}^{\dagger}(\tau + \delta\tau) = e^{iH(\delta\tau)\delta\tau} \psi_{\nu}^{\dagger}(\tau) e^{-iH(\delta\tau)\delta\tau}$$

Vector potential

$$t \rightarrow te^{iA(\tau)}$$

## Localized classical spins

Linearly polarized CW / Pulse field

Landau–Lifshitz–Gilbert (LLG) equation

$$\frac{d\mathbf{S}_i}{d\tau} = \mathbf{h}_i^{\text{eff}} \times \mathbf{S}_i + \alpha \mathbf{S}_i \times \frac{d\mathbf{S}_i}{d\tau}$$

$\alpha$  : Gilbert damping factor

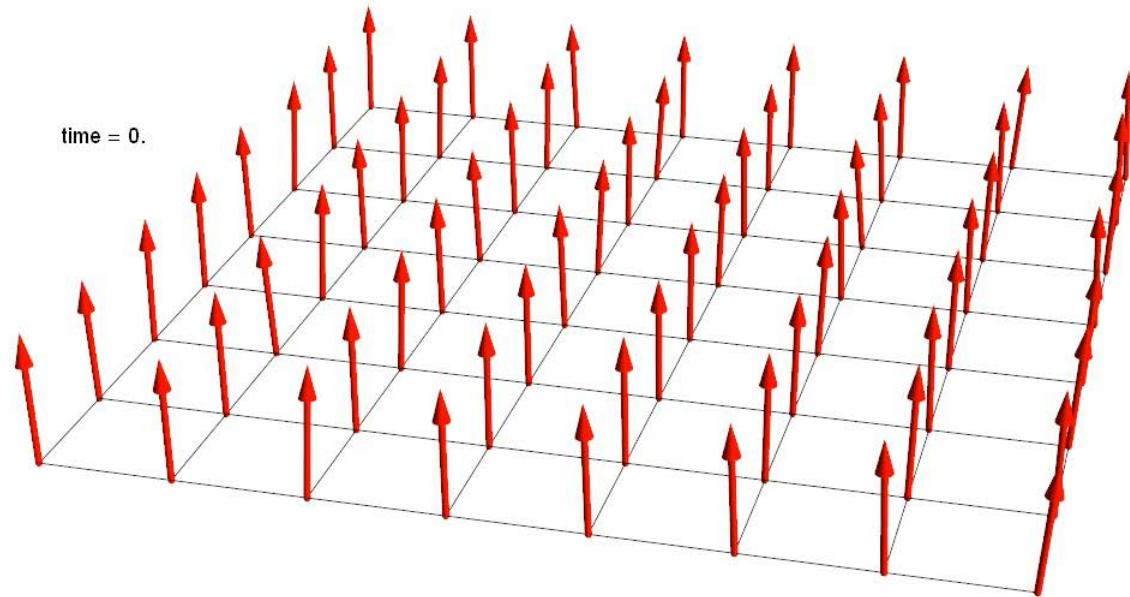
$$A \sim \text{MV/cm}$$

$$\omega \sim t$$

Randomness in initial spins

# Animation

CW field:  $A_0/t = 2.0$ ,  $\omega/t = 1.0$

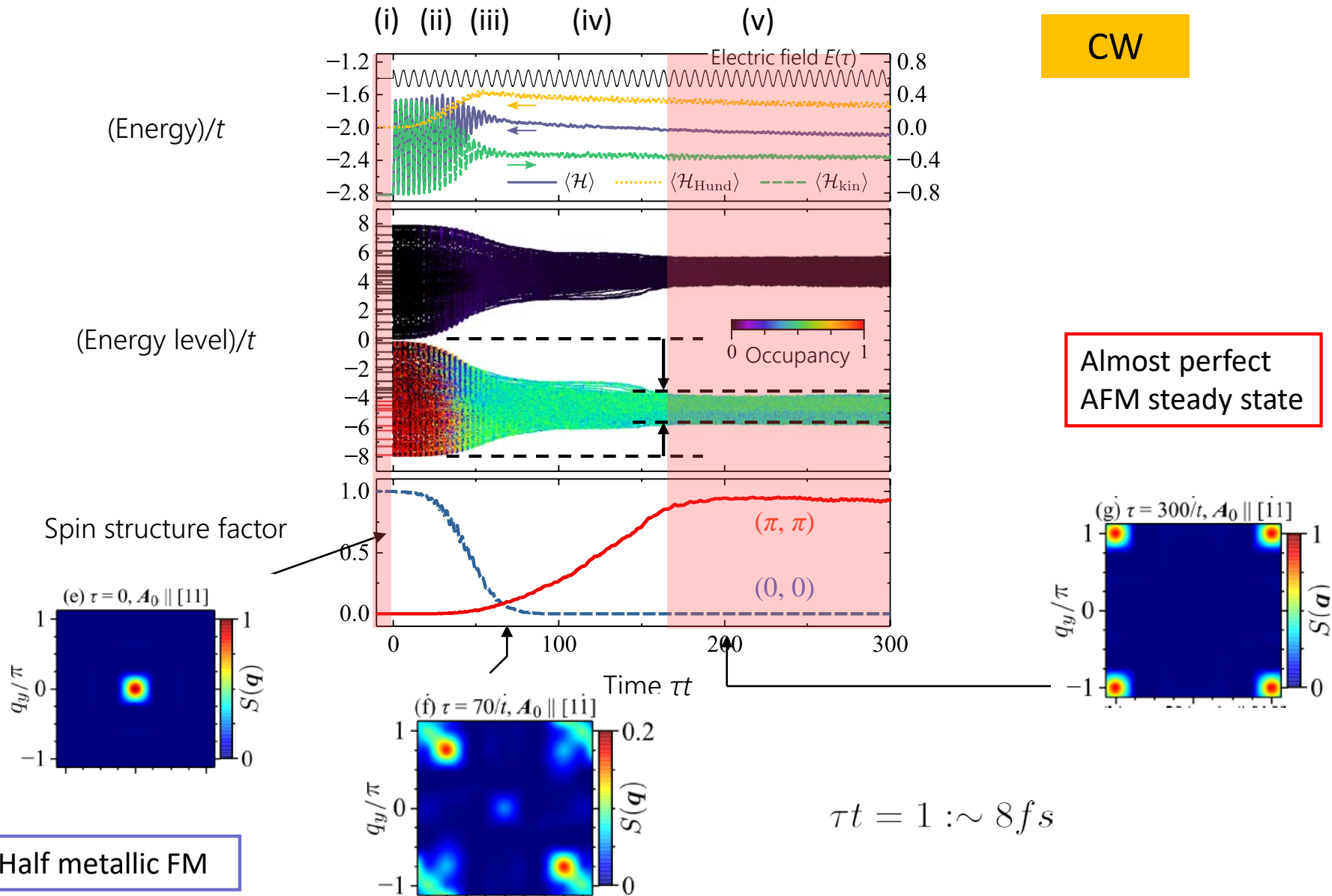


Ferromagnetic metal



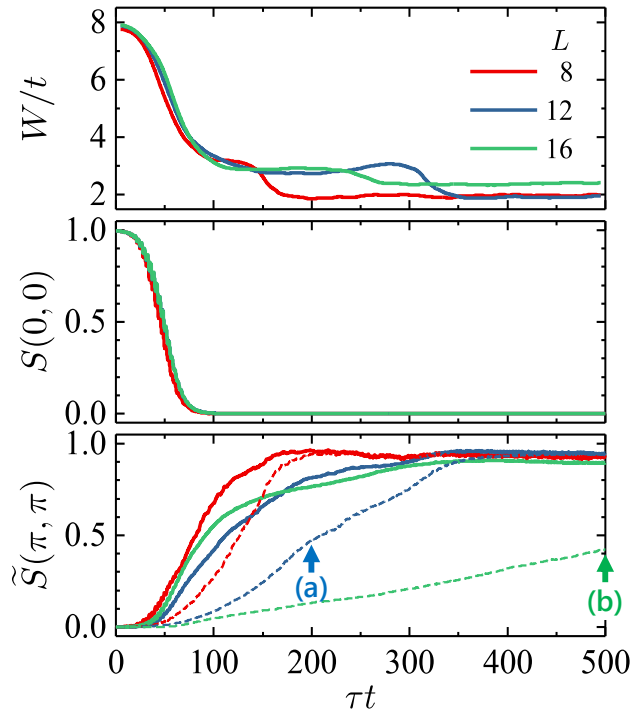
Antiferromagnet

# Time profiles



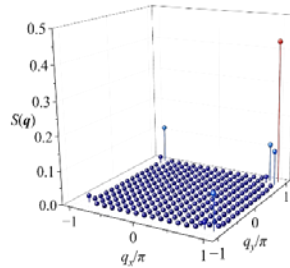
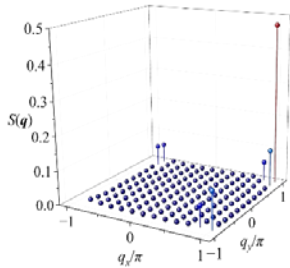
# Cluster Size & Light Polarization dependences

## Cluster size

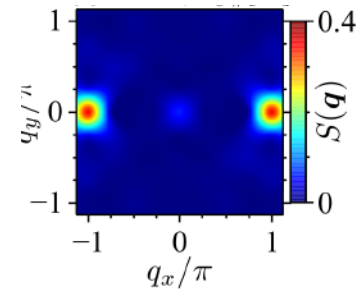
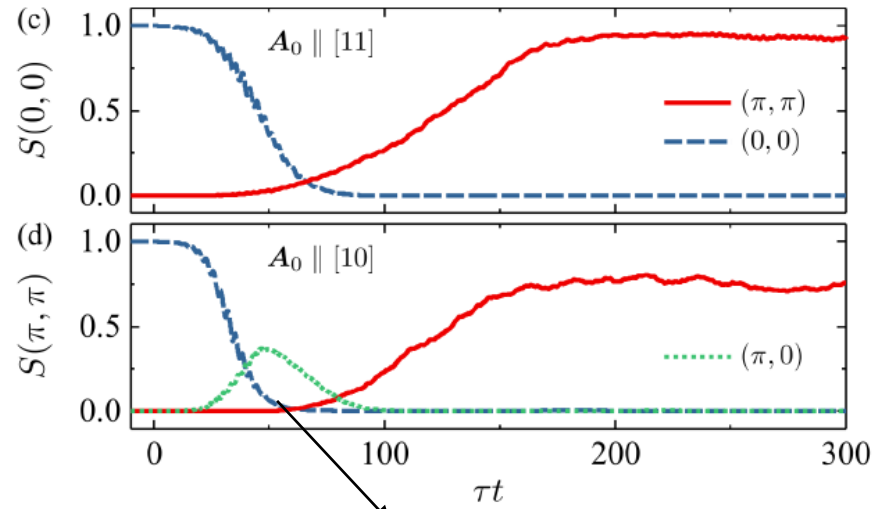


(a)  $L = 12$

(b)  $L = 16$



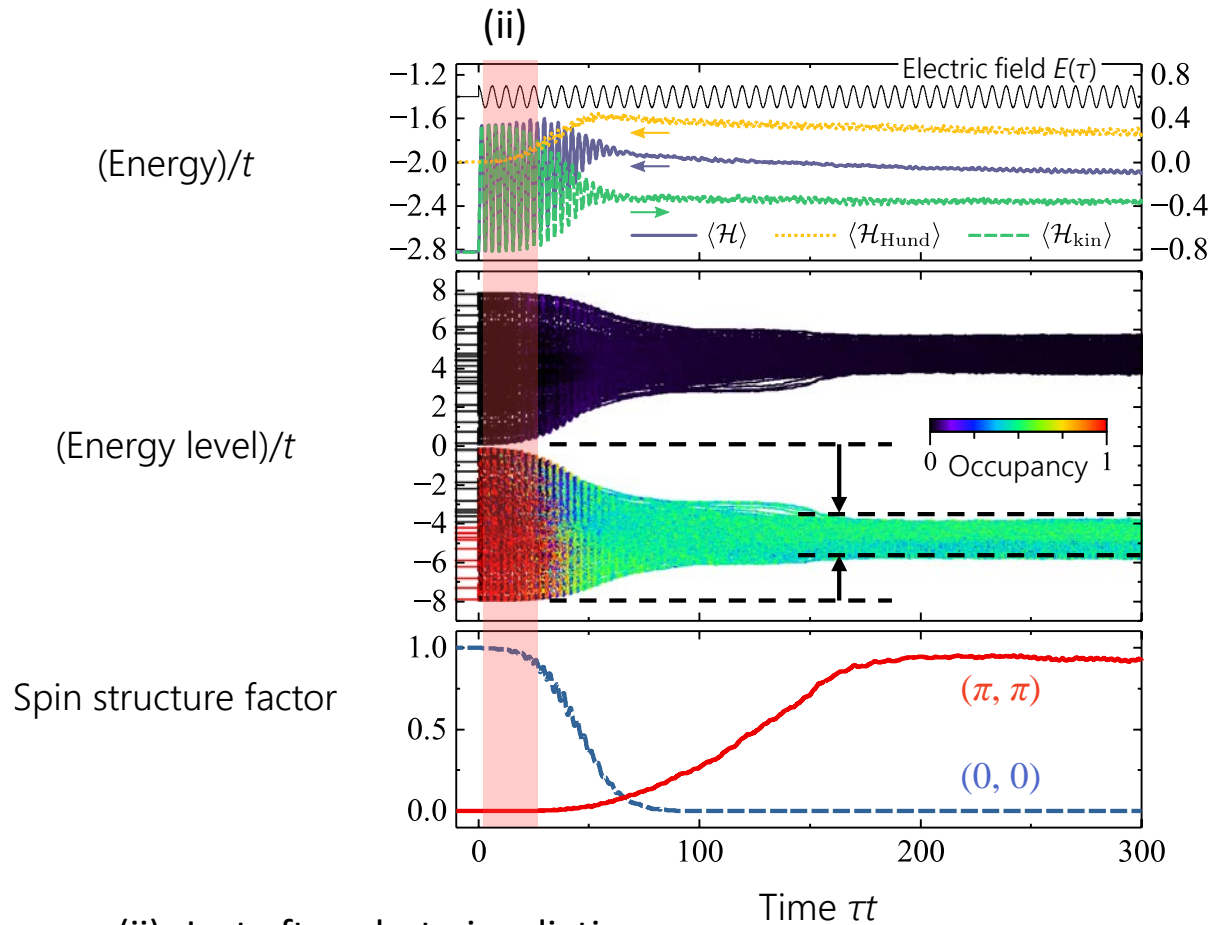
## Light polarization



$$\begin{aligned} \tilde{S}(\pi, \pi) &= S(\pi, \pi) \\ &+ 2S(\pi - \Delta q, \pi) + 2S(\pi, \pi - \Delta q) \\ &+ 2S(\pi - \Delta q, \pi - \Delta q), \\ (\delta q &= 2\pi/L) \end{aligned}$$

# At early time domain

CW



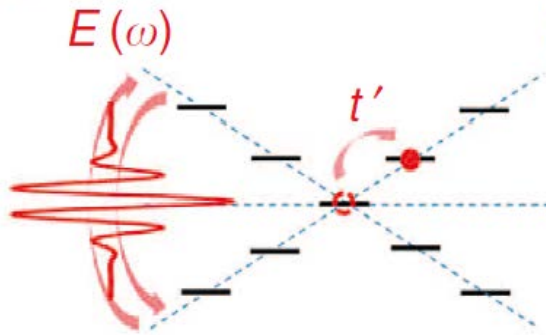
(ii): Just after photo irradiation

Excitation inside of the lower band :  $\langle n \rangle = 1$  and 0 are intermingled.

Band width reduction : **Dynamical localization**



# Dynamical localization at early time domain

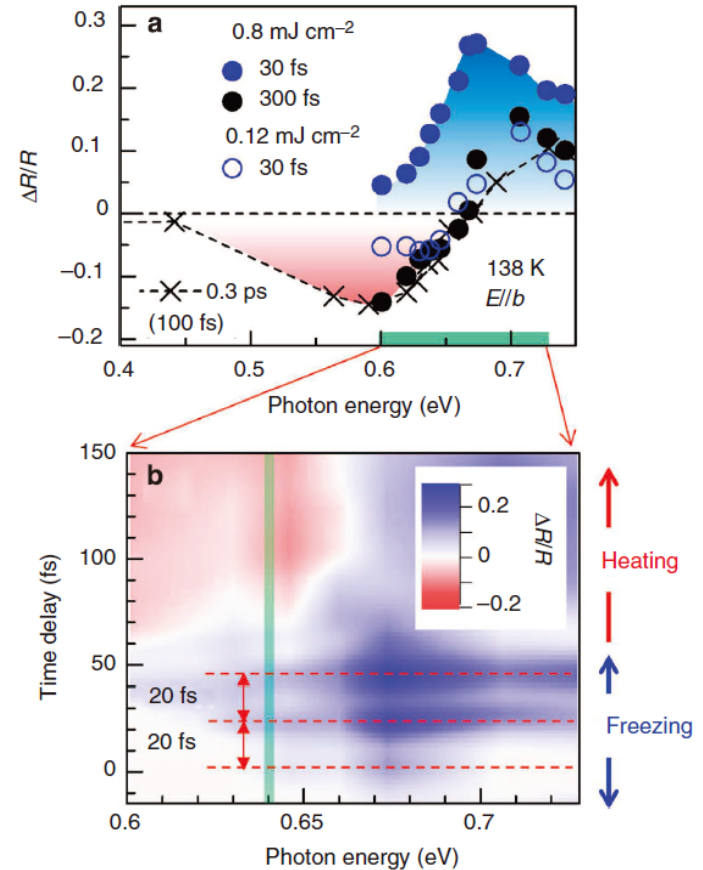
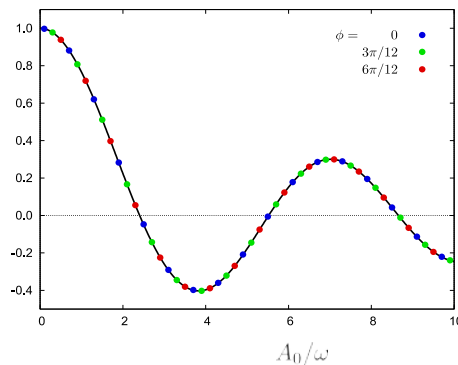


- D. H. Dunlap and V. M. Kenkre, PRB **34**, 3625 (1986)  
 Y. Kayanuma, Phys. Rev. A **50**, 843 (1994).  
 N. Tsuji, T. Oka, H. Aoki, and P. Werner, PRB **85**, 155124 (2012).  
 K. Yonemitsu and K. Nishioka, JPSJ **84**, 054702 (2015).  
 Ishikawa, S. Iwai et al. Nature commun. **5**, 5528(2014)  
 A. Ono and SI Phys. Rev. B **95**, 085123 (2017)  
 and more

Effective electron transfer

$$t_{\text{eff}} = t J_0(A_0/\omega)$$

0-th order Bessel function

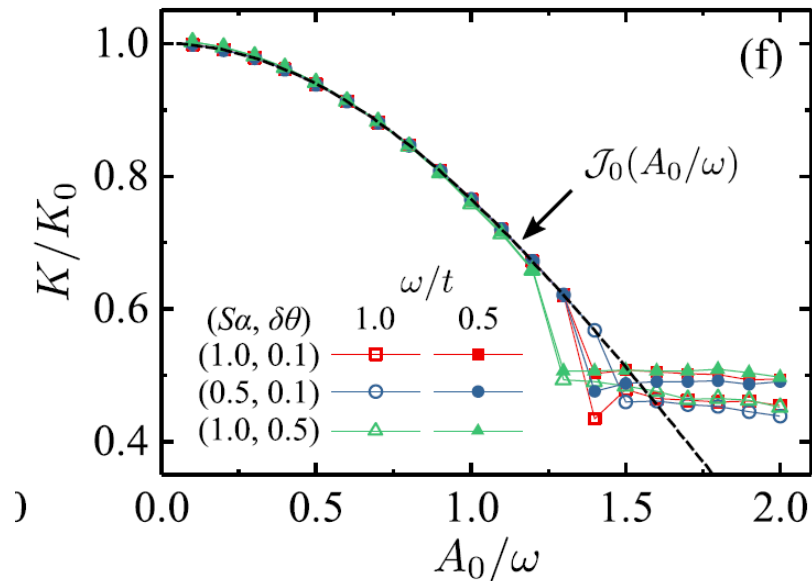


T. Ishikawa, SI, K. Yonemitsu, S. Iwai et al.  
 Nature commun. **5**, 5528(2014)

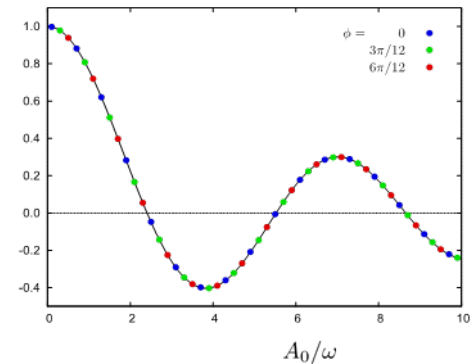
# Dynamical localization at early time domain

Time average of the kinetic energy in early time domain

$$\bar{K} \equiv (\Delta T)^{-1} \int_{\Delta T} d\tau \langle \mathcal{H}_t \rangle$$



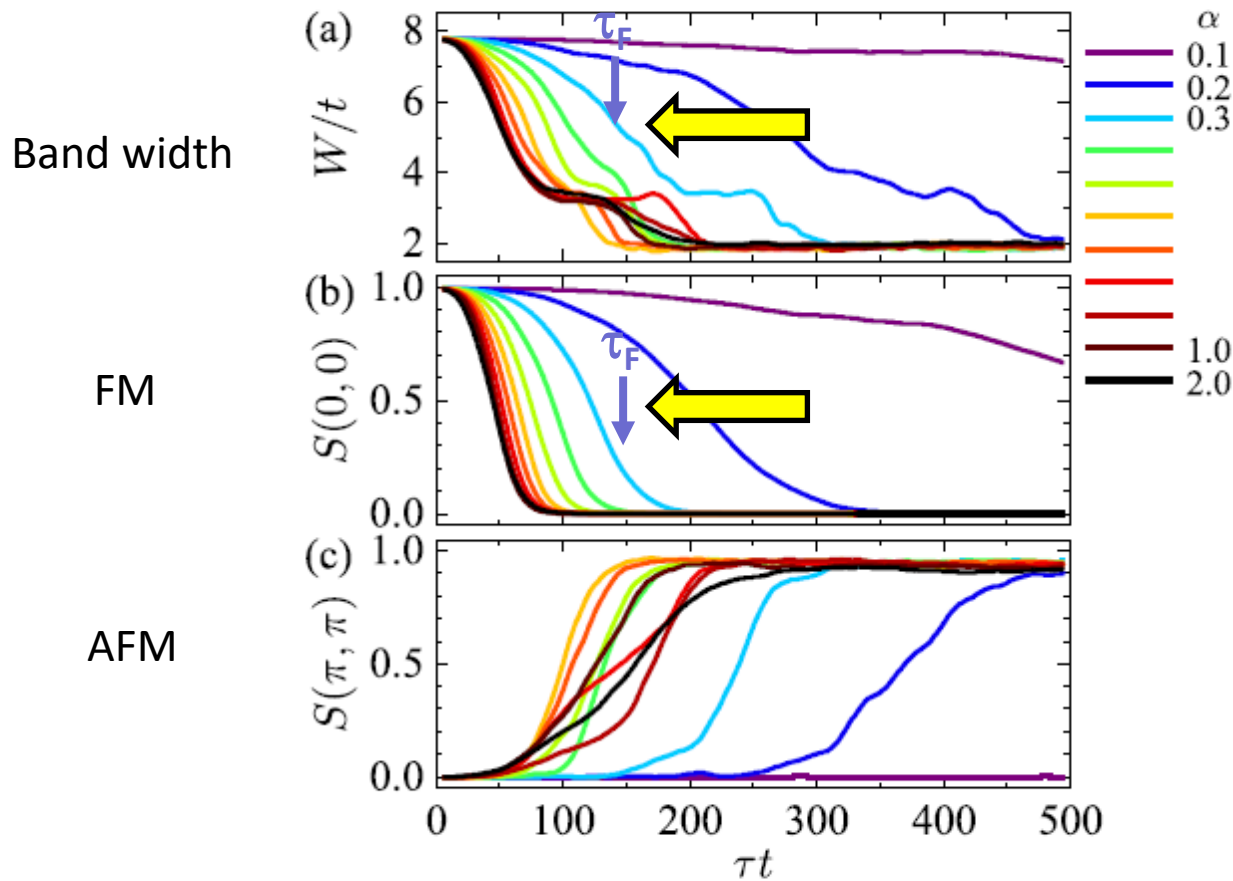
$$t_{\text{eff}} = tJ_0(A_0/\omega)$$



Dynamical localization scenario works well at early stage

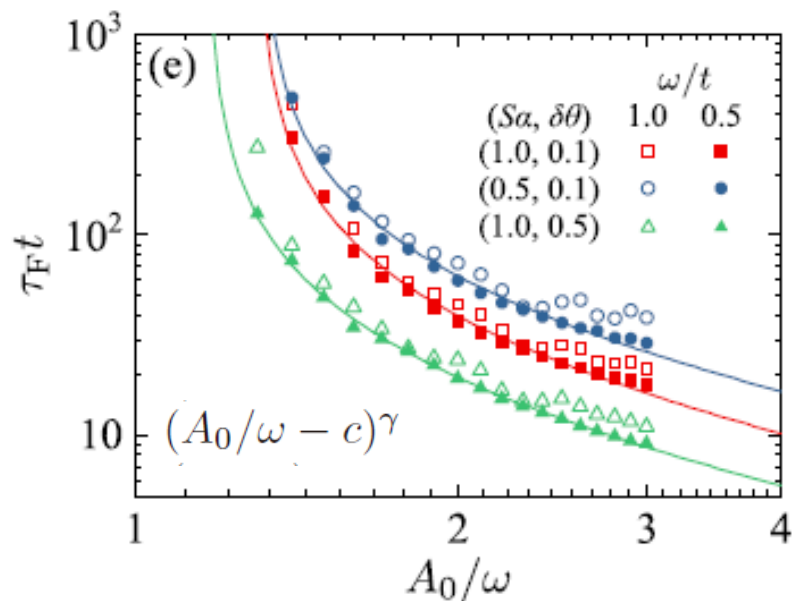
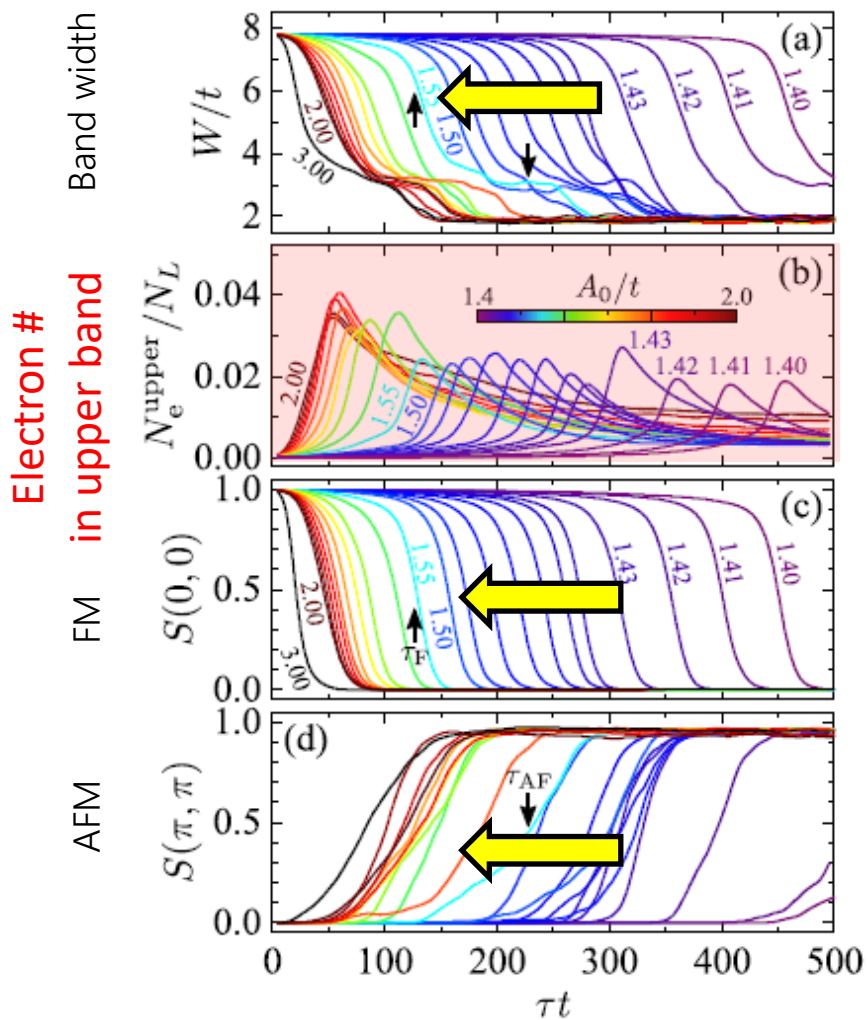
# Key parameters for the FM-to-AFM conversion

Gilbert damping  $\alpha$  dependence



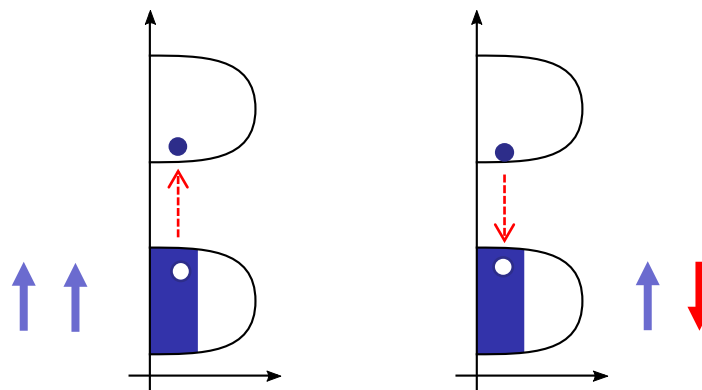
# Key parameters for the FM-to-AFM conversion

A (pump fluence) dependence



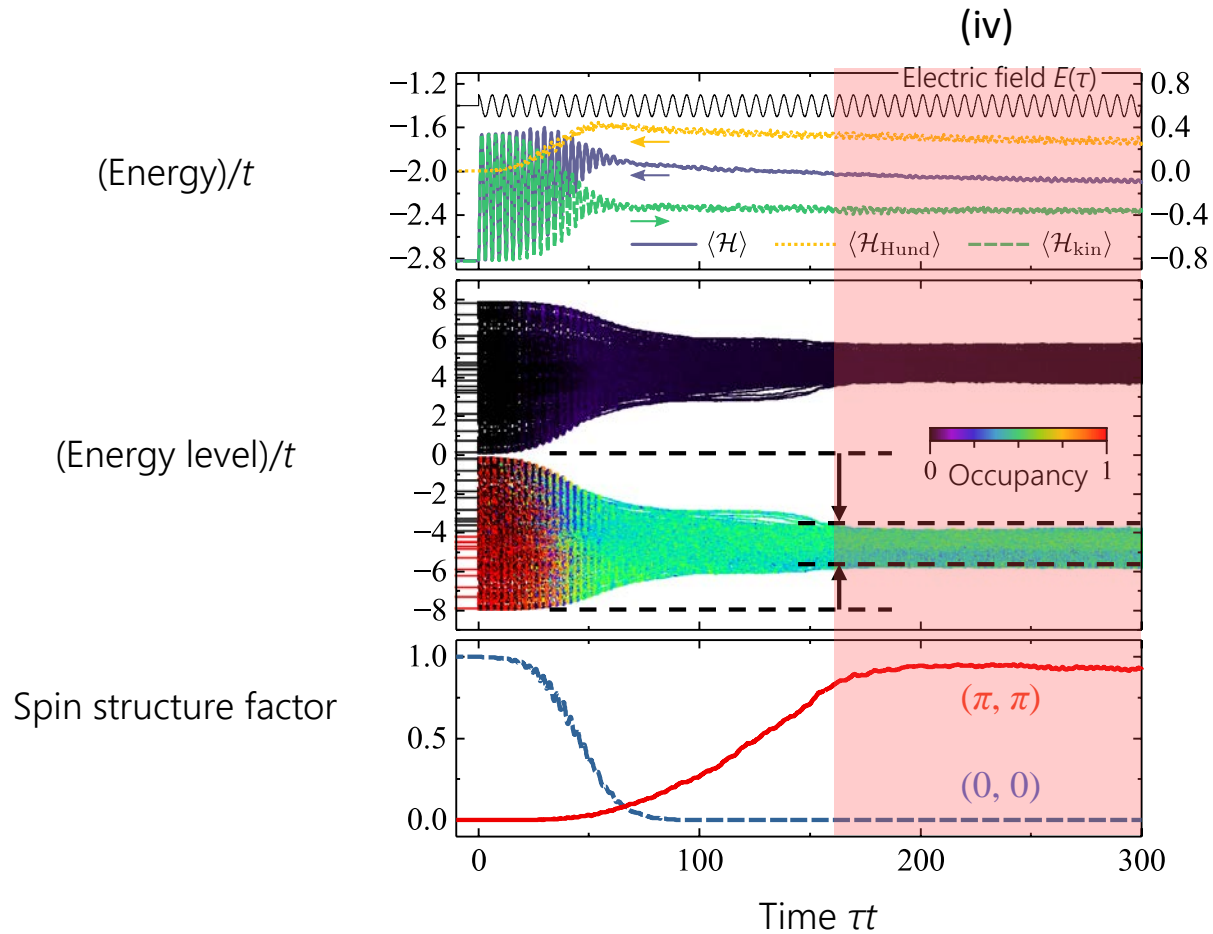
$\tau_F$  : scaled by  $A_0/\omega$

Auger-like process



# Steady NEq AFM state

CW

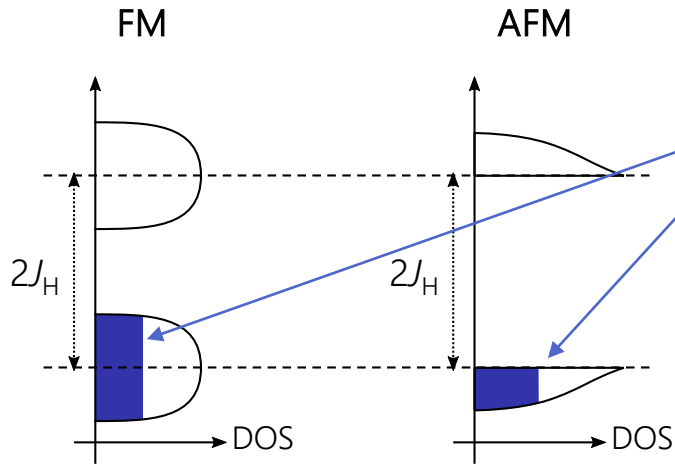


(iv): Steady AFM state

Electron distribution is almost uniform in the lower band

# Steady NEq AFM state

Equilibrium cal.



Assumption:

Uniform electron distribution ( $\neq$  Fermi-Dirac)

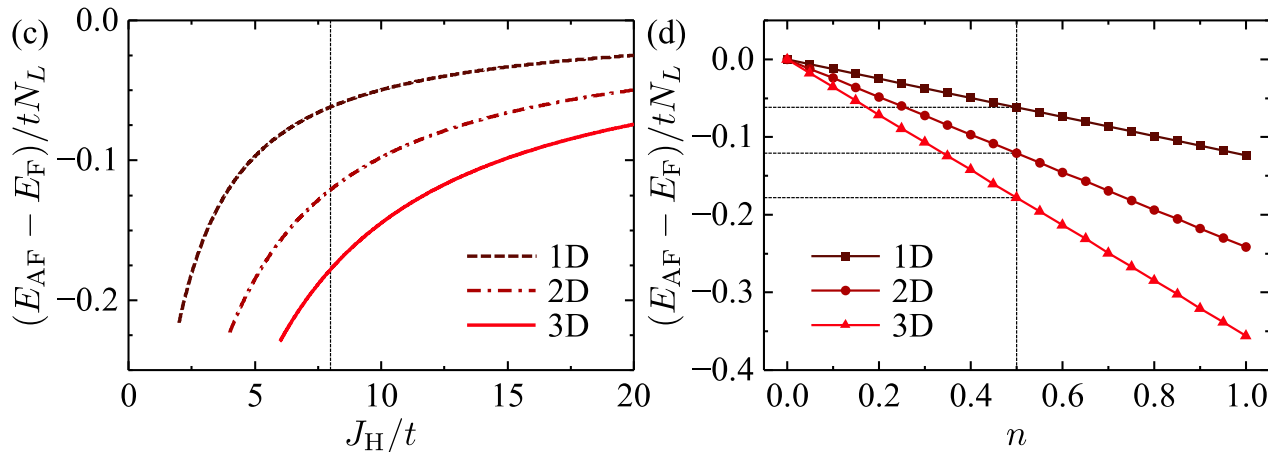
$$\langle n_\nu \rangle = \text{const.}$$



$$\text{Total energy } E_\alpha = \frac{1}{N} \int_{-\infty}^0 d\varepsilon \varepsilon D_\alpha(\varepsilon) f(\varepsilon)$$

( $\alpha = F, AF$ )

Energy difference  $E(AF) - E(F)$  with uniform electron distribution



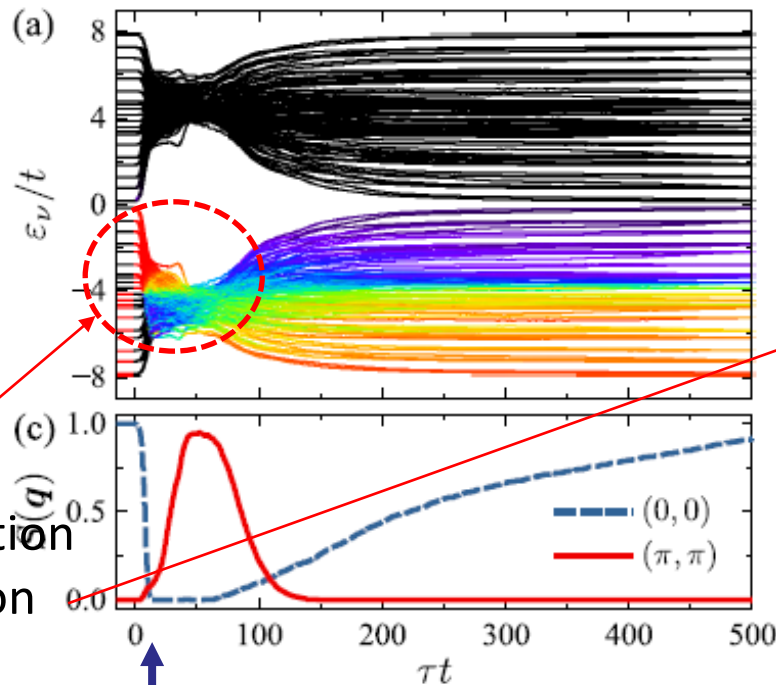
AFM steady state gives lower energy in wide range

# Beyond the CW light

## Pulse

$$A(\tau) = A_1\theta(\tau)$$

$$E(\tau) = -A_1\delta(\tau)$$

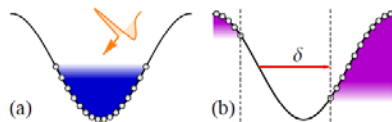


Population inversion

$\pi$ -shift

$$\delta k = (\pi, \pi)$$

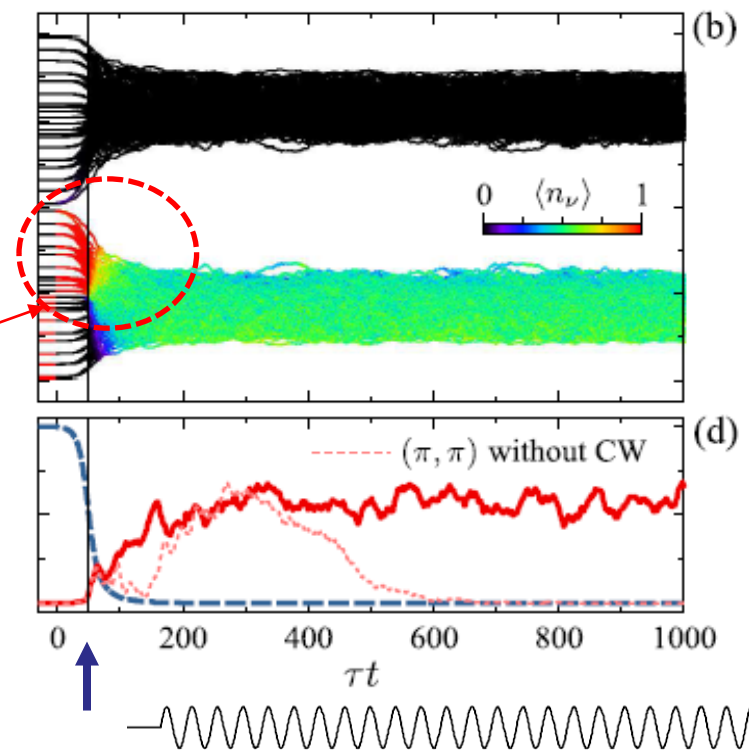
$$\delta k = \int d\tau E(\tau)$$



## Pulse + CW

$$A(\tau) = \dot{A}_1\theta(\tau) + (A_0/\omega) \sin[\omega(\tau - \tau_0)]\theta(\tau - \tau_0)$$

$$E(\tau) = -A_1\delta(\tau) - A_0 \cos[\omega(\tau - \tau_0)]\theta(\tau - \tau_0)$$



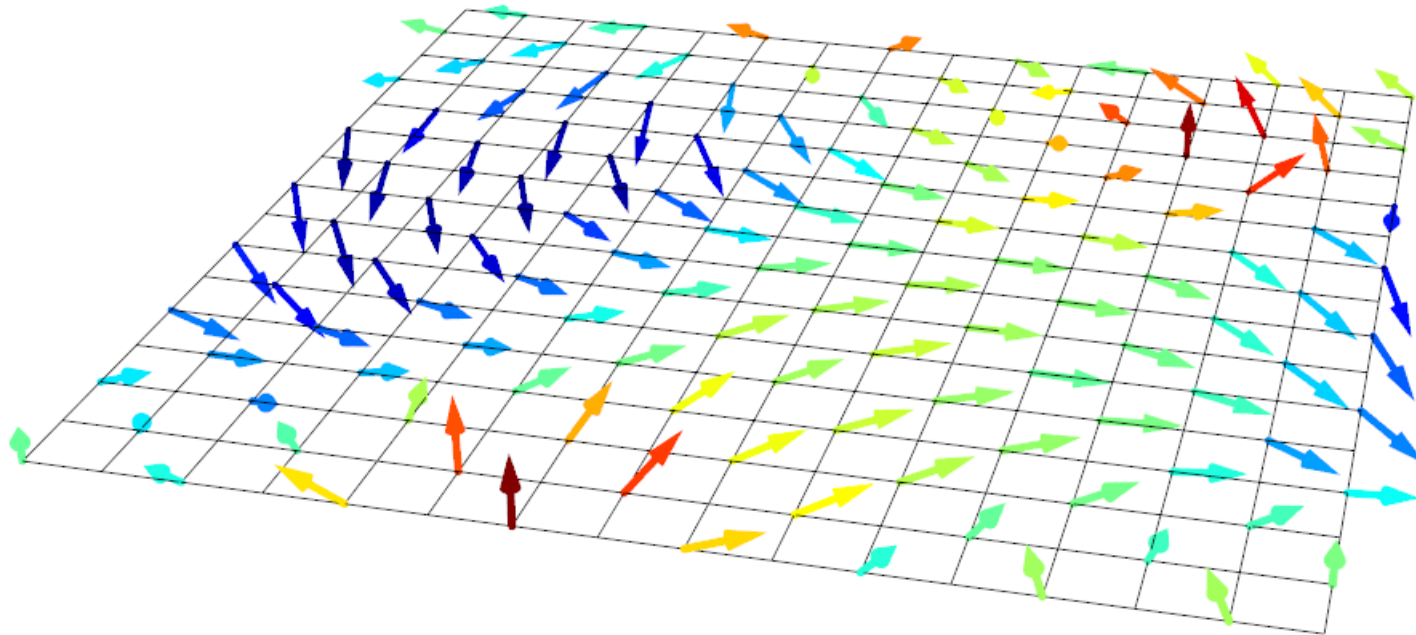
# Transient spin structure

Intermediate time domain ( $\tau = 200/t$ )  
Larger cluster ( $L = 16$ )

CW

Sublattice A

$S_i^z = -1$    $+1$



Vortex-like magnetic structure



# Summary

## Double exchange interaction in non-eq. state revisited

FM to AFM conversion by strong light field

Non-eq. electron distribution

Topological texture in transient state

### Experimental confirmation

Candidates: cubic/layered manganites

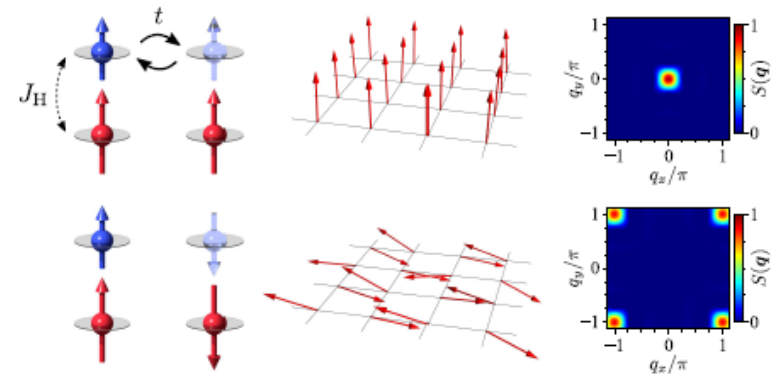
Pulse + CW method : more realistic

transient optical spectra

tr. magnetic x-ray diffraction

tr. ARPES (BZ folding)

tr. Raman (AFM magnon)



A. Ono and SI, Phys. Rev. Lett. 119, 207202 (2017) (Editor suggestion)

A. Ono and SI, Phys. Rev. B 95, 085123 (2017)



