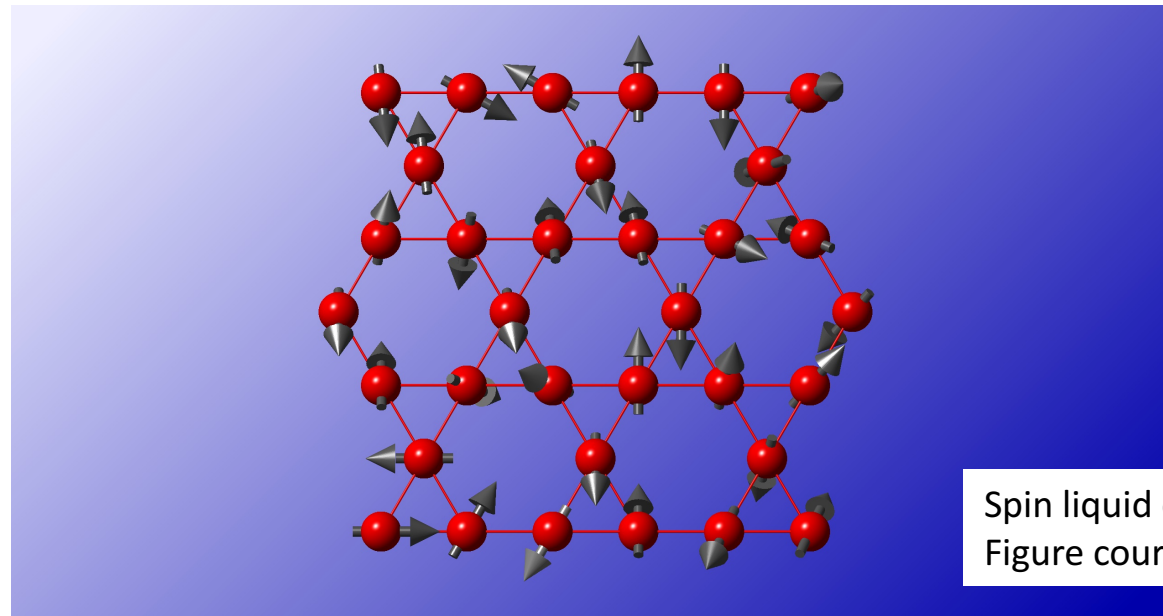


**NMR Evidence for a gapped spin-liquid ground state
in a kagome Heisenberg antiferromagnet (herbertsmithite $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$)**

Takashi Imai

McMaster University

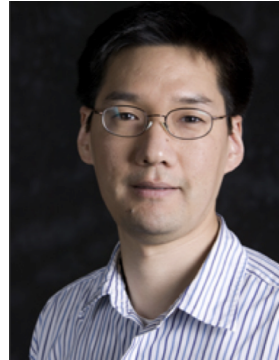
Canadian Institute for Advanced Research



A Short List of Recent Collaborators



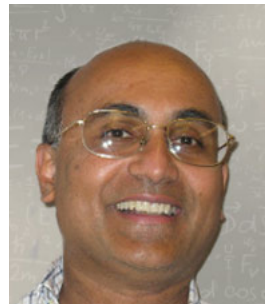
Dr. Mingxuan Fu
McMaster
→PDF at Johns Hopkins
→NSERC PDF at Univ. of Toronto



Prof. Y.S. Lee
M.I.T. → Stanford
(Neutron / X'tal growth)



Dr. T. H. Han
M.I.T. → Chicago/Argonne Nat. Lab.
(Neutron / X'tal growth)



Prof. R.R.P. Singh
U.C. Davis
(Series expansion)



N.E. Sherman
U.C. Davis
(Series expansion)

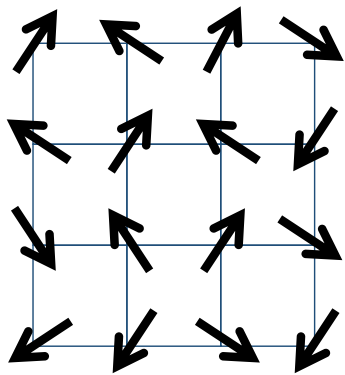
Outline

1. Introduction: kagome lattice in herbertsmithite, and why NMR is useful
T. Imai and Y.S. Lee., *Physics Today*, p-30, August (2016).
2. First generation ^{35}Cl , ^1H , and ^{63}Cu powder NMR measurements
T. Imai *et al.*, *PRL* [100](#) (2008) 077203
3. Second generation single crystal ^2D NMR measurements on $\text{ZnCu}_3(\text{OD})_6\text{Cl}_2$
T. Imai *et al.*, *PRB* [83](#)(2011) 020411 (Rapid).
4. Third generation single crystal ^{17}O NMR measurements on $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$
M. Fu, T. I. *et al.*, *Science* [350](#) (2015) 655.
N. Sherman, T.I., R.R.P. Singh, *PRB* 94 (2016) 140405. [Series expansion.]
5. Summary

Paramagnetic ground state vs. antiferromagnetic phases

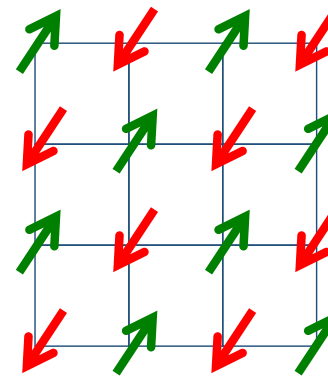
Antiferromagnetic “Heisenberg model” (model Hamiltonian)

$$\hat{H} = J \sum_{\langle i,j \rangle} \hat{S}_i \cdot \hat{S}_j \quad (J > 0)$$



Higher temperatures

Paramagnetic state with randomly oriented spins



$T \leq T_N$
(Neel temperature)

Neel state : usually, spins are antiferromagnetically ordered with a regular pattern ($T_N=0$ for square-lattice)

In analogy with.....



Liquid water

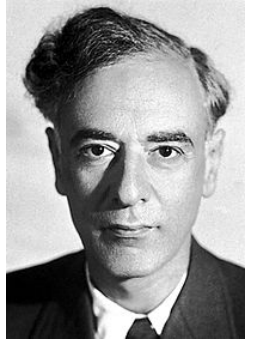


Solid ice
 $T < 273 \text{ K}$

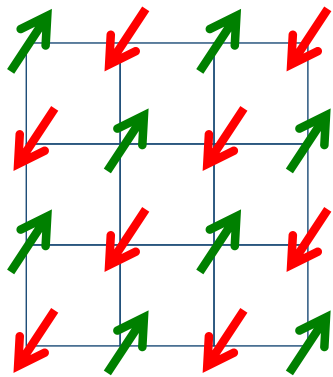
Old controversy: Antiferromagnetically ordered state vs. Landau's superposed singlets

Antiferromagnetic "Heisenberg model"
(model Hamiltonian)

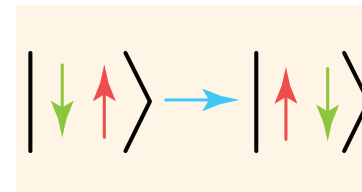
$$\hat{H} = J \sum_{\langle i,j \rangle} \hat{S}_i \cdot \hat{S}_j \quad (J > 0)$$



"Neel state" is not an eigenstate of the Hamiltonian.

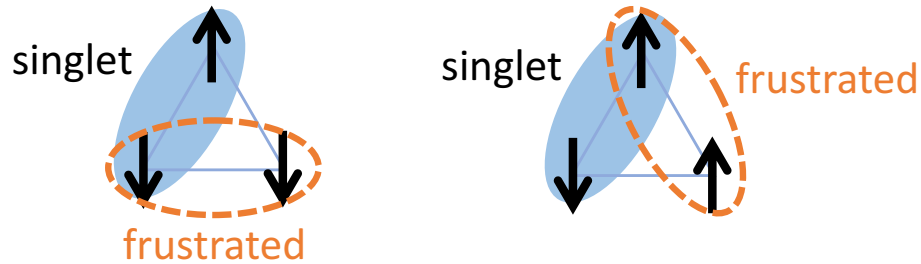


Landau (1962 Nobel Physics) thought *there is no such a thing as antiferromagnetically ordered state*; Instead, *superposed singlet states must be realized*.



Mostly forgotten idea for decades, because antiferromagnets do exist after all.

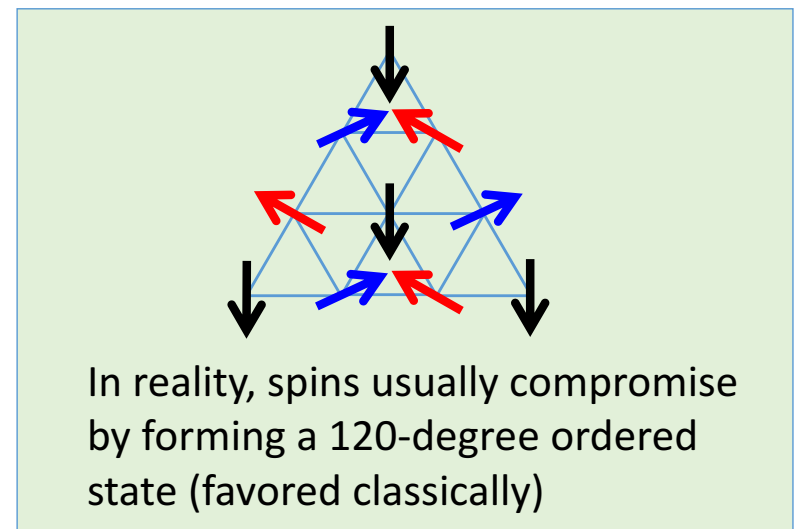
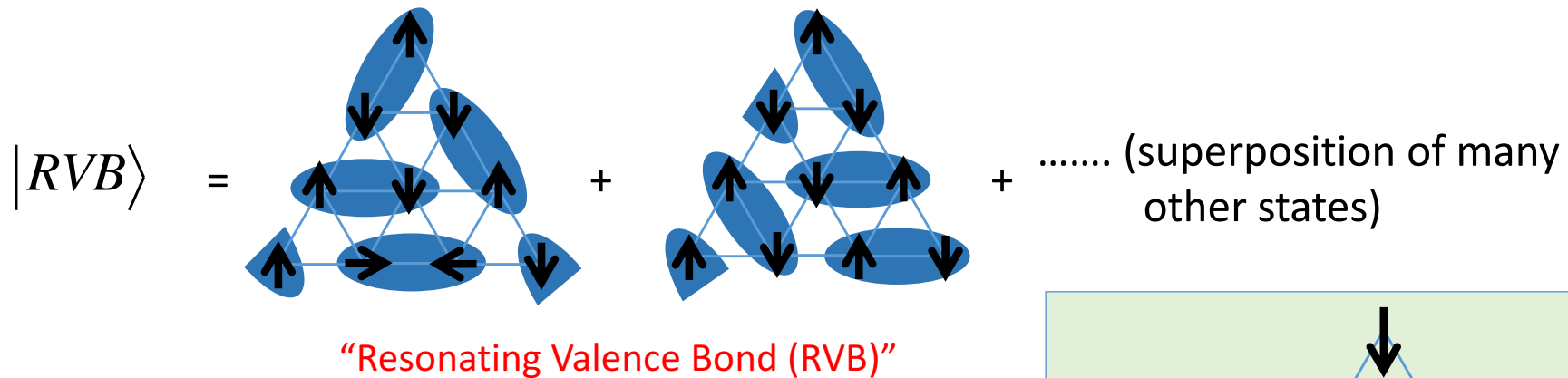
Geometrical frustration effects of spins on the triangular-lattice Heisenberg model and the **RVB** “spin liquid” (P.W. Anderson 1973)



P.W. Anderson (Nobel physics 1977)



Frustration effects arise from love-and-hate relationship between $S=1/2$ spins on a triangle



Resurrection of the old RVB idea in the context of undoped square-lattice Heisenberg antiferromagnet La_2CuO_4 (Parent phase of Copper-oxide high T_c superconductors)

P.W. Anderson, Science 235 (1987) 1196

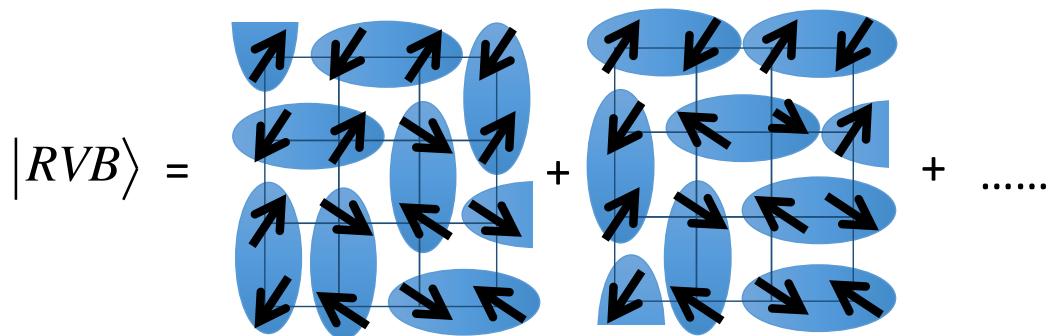
The Resonating Valence Bond State in La_2CuO_4 and Superconductivity

P. W. ANDERSON

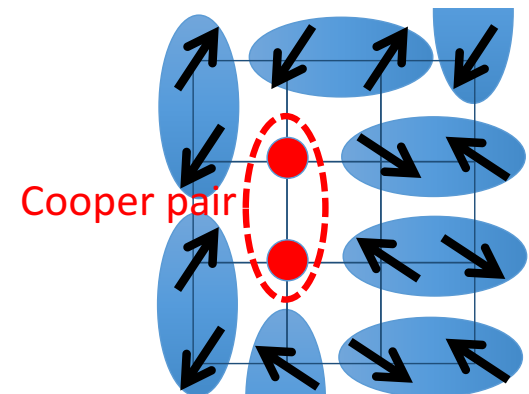
The oxide superconductors, particularly those recently discovered that are based on La_2CuO_4 , have a set of peculiarities that suggest a common, unique mechanism: they tend in every case to occur near a metal-insulator transition into an odd-electron insulator with peculiar magnetic properties. This insulating phase is proposed to be the long-sought “resonating-valence-bond” state or “quantum spin liquid” hypothesized in 1973. This insulating magnetic phase is favored by low spin, low dimensionality, and magnetic frustration. The preexisting magnetic singlet pairs of the insulating state become charged superconducting pairs when the insulator is doped sufficiently strongly. The mechanism for superconductivity is hence predominantly electronic and magnetic, although weak phonon interactions may favor the state. Many unusual properties are predicted, especially of the insulating state.



Cu^{2+} ion ($S=1/2$) at each corner

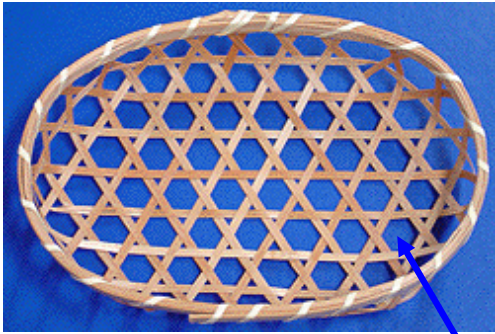


Anderson's proposition:
High temperature superconductivity emerges when we remove $\sim 15\%$ of spins



Where should we look for a quantum spin liquid?

“Kagome” 籠目 : “Basket pattern” composed of **corner-sharing triangles**

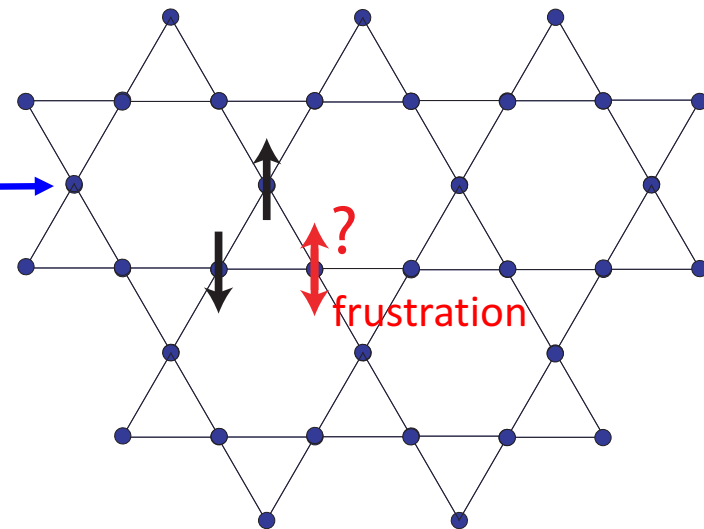


“Basket pattern”
(kago) (me)
籠 目



Japanese “Kagome Tomato Ketchup”

Corner-sharing triangles

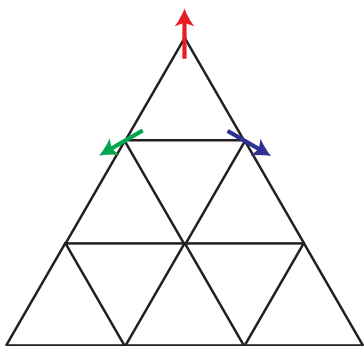


Advantage of the kagome Heisenberg antiferromagnet = (strong degeneracy).

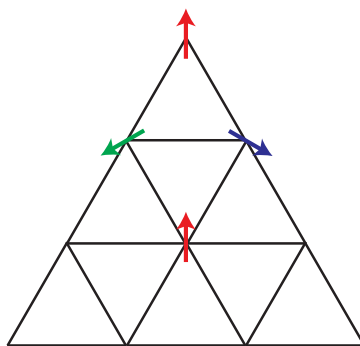
Favors a quantum spin liquid ground state

Edge-sharing triangular lattice

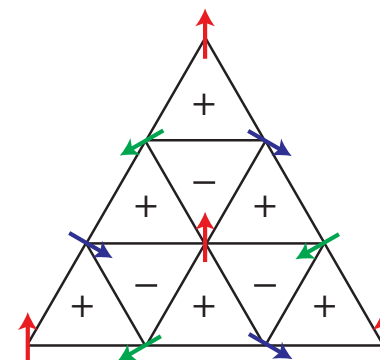
120 degree arrangement on a triangle
minimizes the energy (classically)



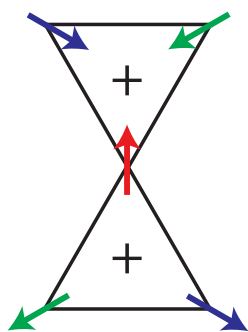
... and constrains
another spin



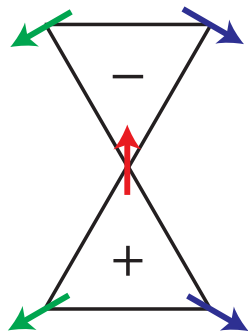
... and all spins



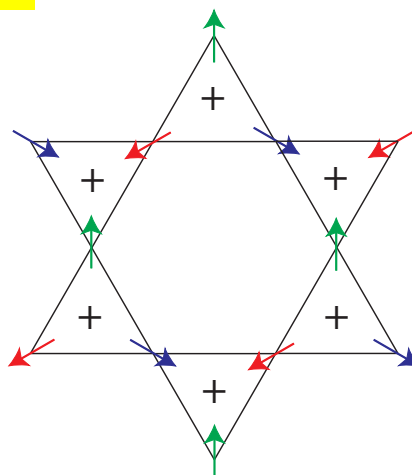
Corner-sharing triangular lattice (kagome)



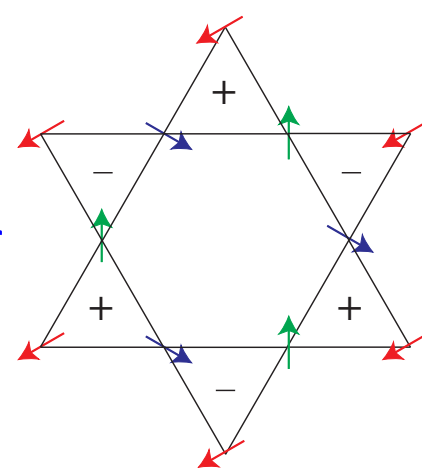
or



One triangle does not constrain the
arrangement of the adjacent triangle



or



Spins have a hard time to choose ordering pattern!

“The ground state of the kagome Heisenberg antiferromagnet is a gapped Z_2 spin liquid”

Spin-Liquid Ground State of the $S = 1/2$ Kagome Heisenberg Antiferromagnet

Simeng Yan,¹ David A. Huse,^{2,3} Steven R. White^{1*}

We use the density matrix renormalization group to perform accurate calculations of the ground state of the nearest-neighbor quantum spin $S = 1/2$ Heisenberg antiferromagnet on the kagome lattice. We study this model on numerous long cylinders with circumferences up to 12 lattice spacings. Through a combination of very-low-energy and small finite-size effects, our results provide strong evidence that, for the infinite two-dimensional system, the ground state of this model is a fully gapped spin liquid.

We consider the quantum spin $S = 1/2$ kagome Heisenberg antiferromagnet (KHA) with only nearest-neighbor isotropic exchange interactions (Hamiltonian $H = \sum \vec{S}_i \cdot \vec{S}_j$, where \vec{S}_i and \vec{S}_j are the spin operators for sites i and j , respectively) on a kagome

lattice (Fig. 1A). This frustrated spin system has long been thought to be an ideal candidate for a simple, physically realistic model that shows a spin-liquid ground state ($I-3$). A spin liquid is a magnetic system that has “melted” in its ground state because of quantum fluctuations, so it has

no spontaneously broken symmetries (4). A key problem in searching for spin liquids in two-dimensional (2D) models is that there are no exact or nearly exact analytical or computational methods to solve infinite 2D quantum lattice systems. For 1D systems, the density matrix renormalization group (DMRG) (5, 6), the method we use here, serves in this capacity. In addition to its interest as an important topic in quantum magnetism, the search for spin liquids thus serves as a test-bed for the development of accurate and widely applicable computational methods for 2D many-body quantum systems.

¹Department of Physics and Astronomy, University of California, Irvine, CA 92617, USA. ²Department of Physics, Princeton University, Princeton, NJ 08544, USA. ³Institute for Advanced Study, Princeton, NJ 08540, USA.

*To whom correspondence should be addressed. E-mail: srwhite@uci.edu

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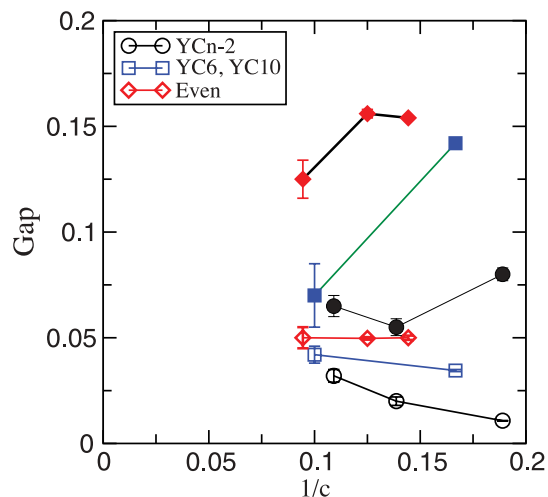


Fig. 4. Spin triplet (solid symbols) and singlet (hollow symbols) gaps for various cylinders with circumferences c . The type of cylinder (15) is indicated in the key (inset).

Large scale DMRG (Density Matrix Renormalization Group) calculations

Yan, Huse, and White, *Science* **332** (2011) 1173.

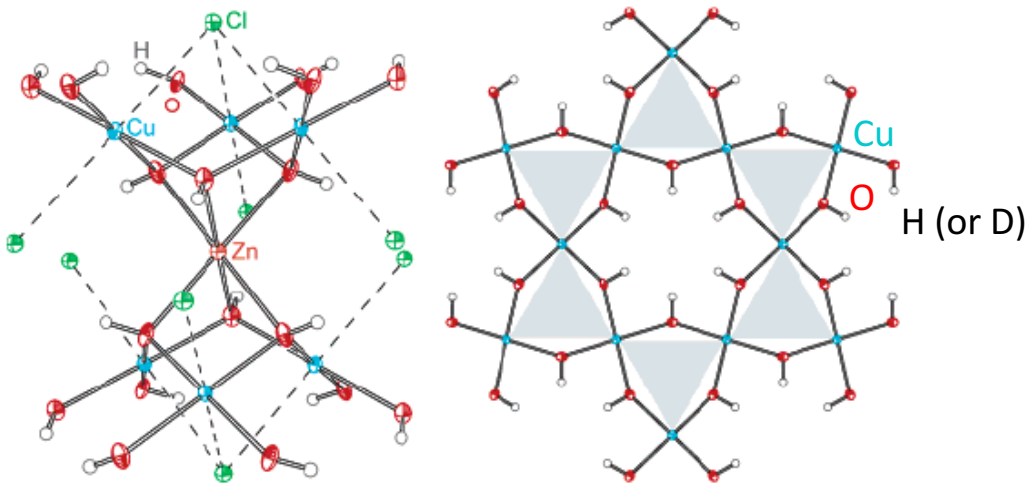
Also see Jiang *et al.*, *PRL* **101** (2008) 117203;

Deepenblock *et al.*, *PRL* **109** (2011) 067201;

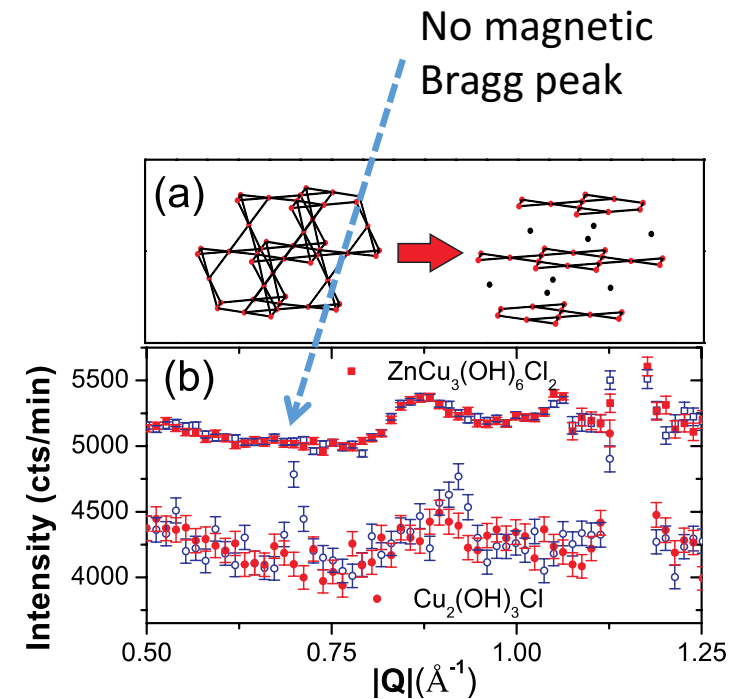
Liao *et al.*, *PRL* **118** (2017) 137202.

Successful laboratory-synthesis of the structurally ideal kagome lattice Herbertsmithite $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$

M.P. Shores, D. Nocera *et al.* (M.I.T. Chemistry)
J. Amer. Chem. Soc. **127**, (2005) 13462



- Cu^{2+} ions ($S = \frac{1}{2}$) form a perfect kagome lattice
- Cu-Cu super-exchange interaction $J \sim 200$ K



Paramagnetic down to ~ 50 mK

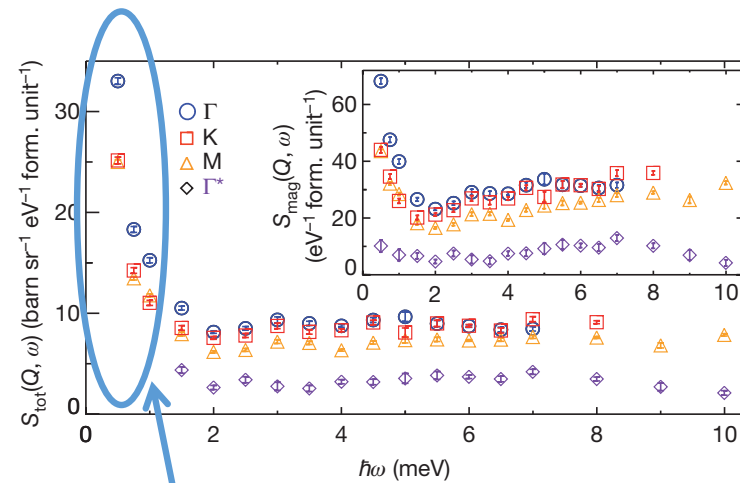
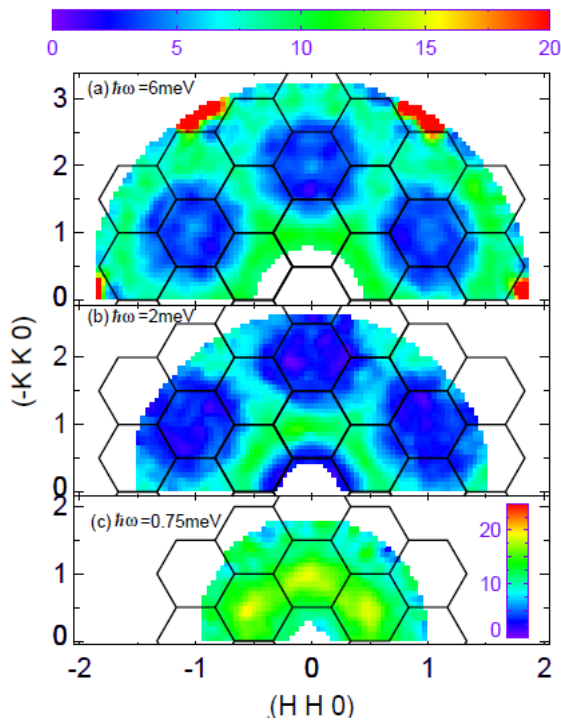
Helton *et al.* PRL 98 (2007) 107204.

Also by μSR , see Mendels *et al.*,
PRL 98 (2007) 077204.

Absence of conventional magnon excitations in $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$ in inelastic neutron scattering

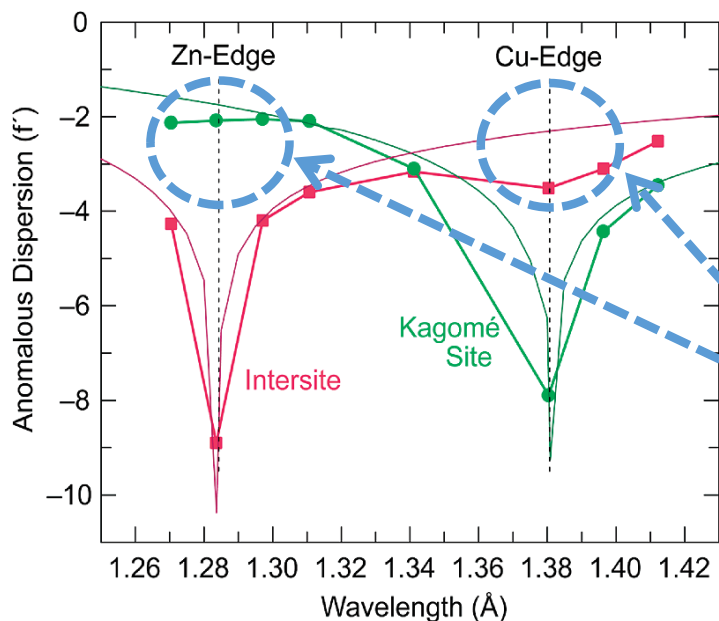
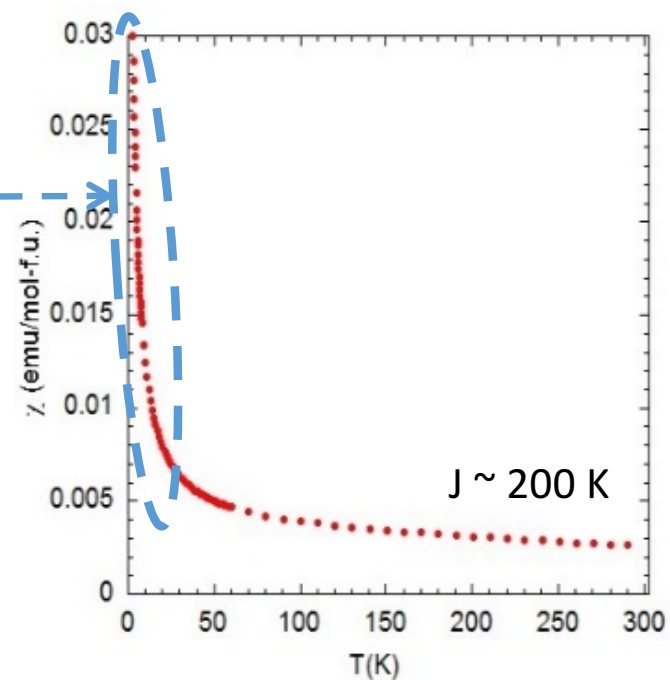
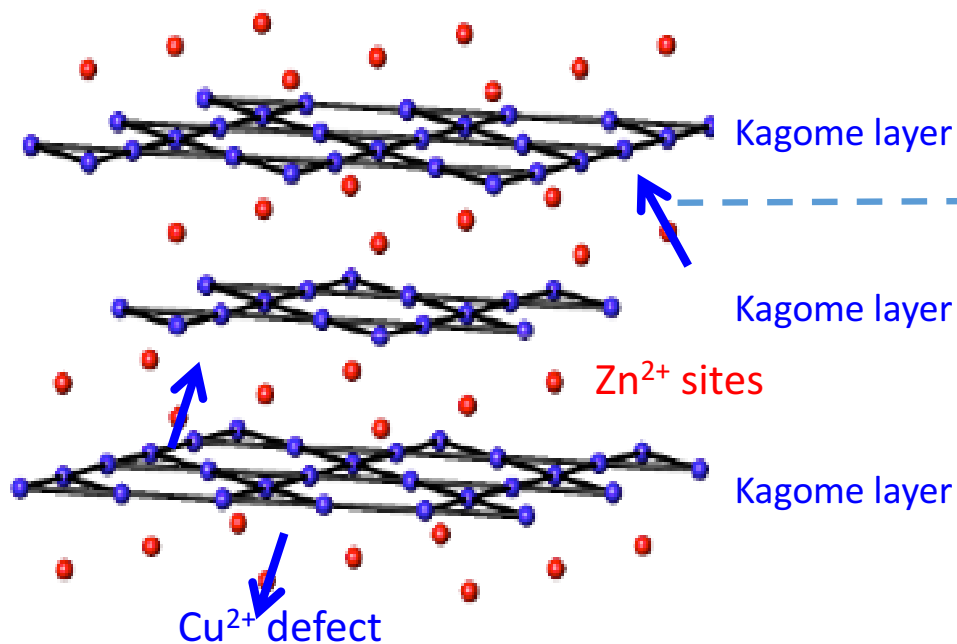
T.-H. Han, *et al.* Nature (2012)

Good news: Spinon Continuum (rather than conventional magnon dispersion);
Consistent with continuous $S=1/2$ spin excitations from a spin-liquid ground state



Bad news: Defect spins dominate the low energy part of spin excitations;
unable to study the ground state, including the possibility of a small gap

Complications : Defect Cu^{2+} spins occupy the non-magnetic Zn^{2+} sites with 15% probability
 \rightarrow actual composition is $(\text{Zn}_{0.85}\text{Cu}_{0.15})\text{Cu}_3(\text{OH})_6\text{Cl}_2$



Cu^{2+} defect spins dominate χ (and all *bulk-averaged* thermodynamic data) at low temperatures

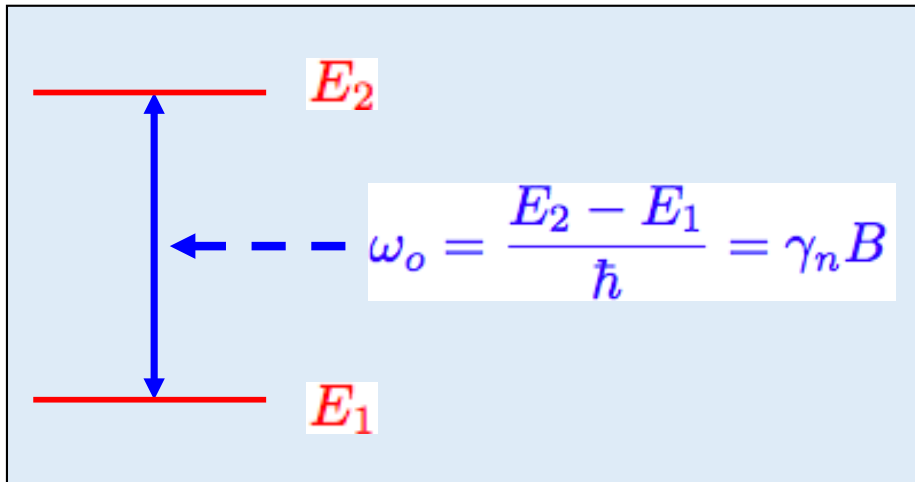
Anomalous X-ray diffraction experiments on single crystal:

- 15% of Zn^{2+} sites are occupied by Cu^{2+} defect spins
- No Zn^{2+} occupy Cu^{2+} kagome sites (*i.e.* no anti-site defects)

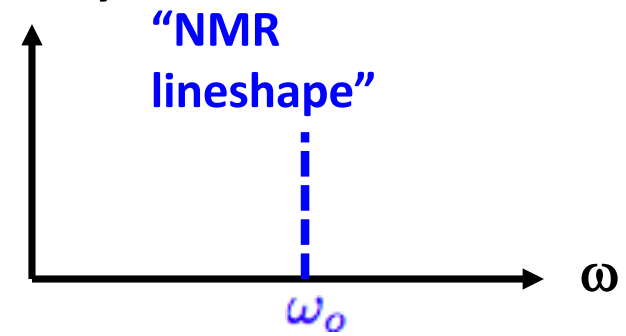
Freedman *et al*, JACS 132 (2010) 16185.

How shall we probe the properties of the kagome layers separately from the defects?

Answer: NMR

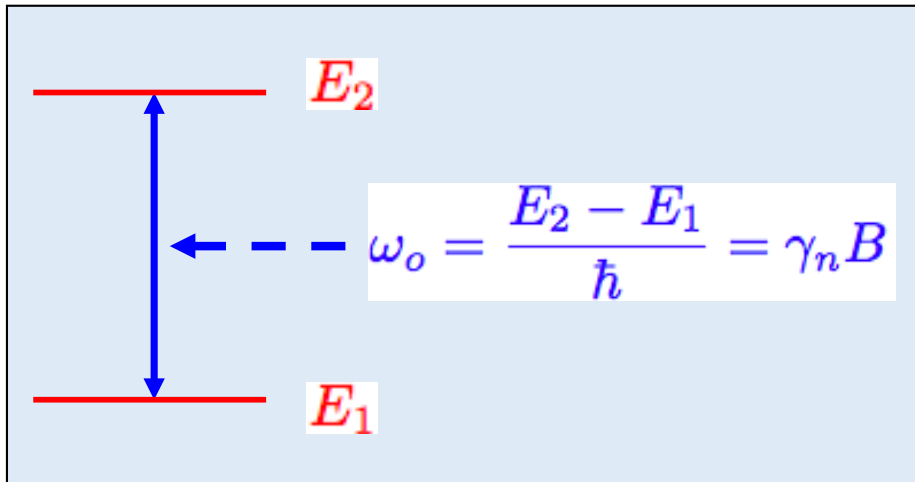


Absorption
intensity

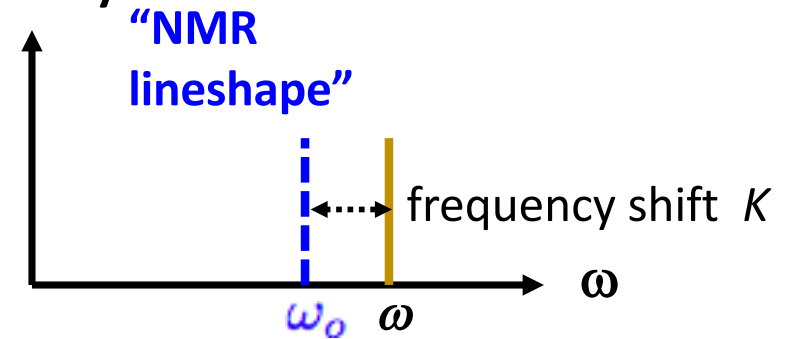


How shall we probe the properties of the kagome layers separately from the defects?

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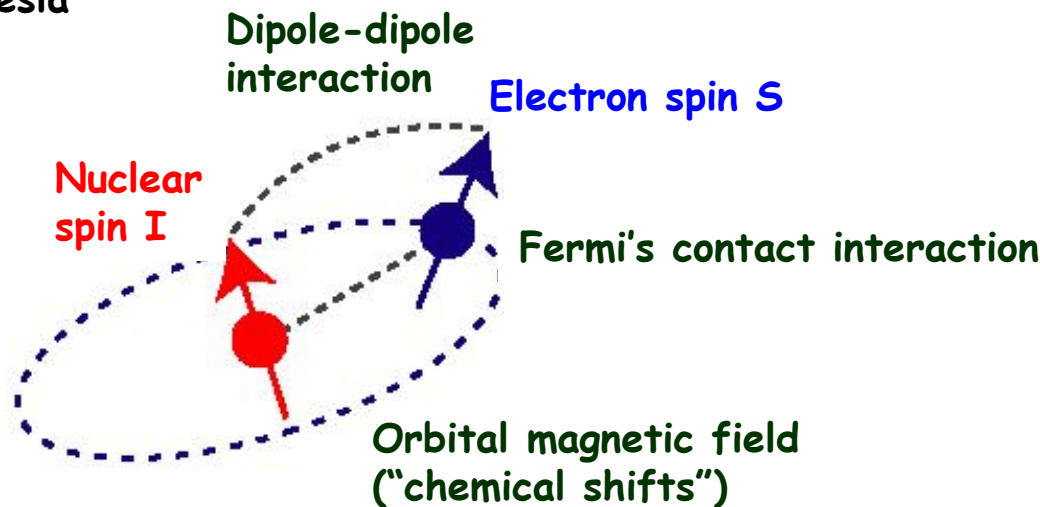


Absorption intensity



Influence of electron spins via hyperfine interactions

$B_{\text{ext}} \sim 8$ Tesla
(Zeeman)



NMR frequency shifts to

$$\omega = \gamma_n (B_{\text{ext}} + B_{\text{hf}})$$

$$= \omega_0 (1 + K)$$

$$K = \frac{A_{\text{hf}}}{N_A \mu_B} \chi_{\text{spin}} + K_{\text{chem}}$$

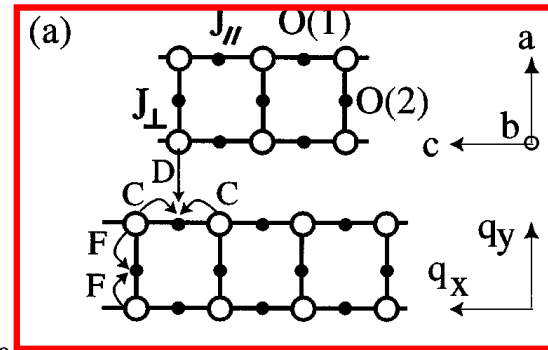
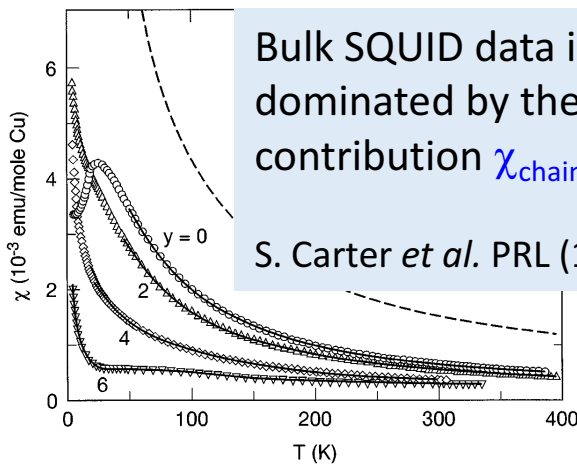
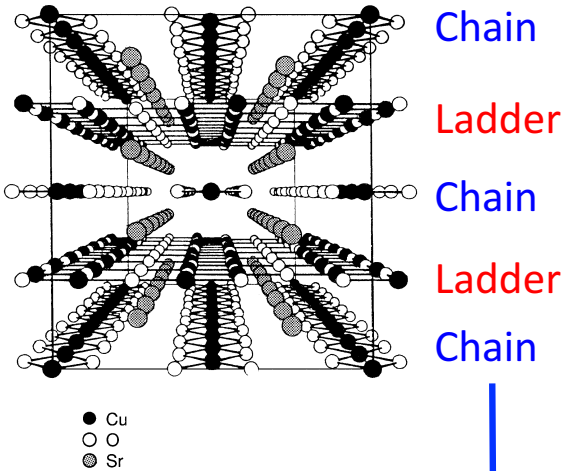
where

A_{hf} : "Hyperfine coupling"

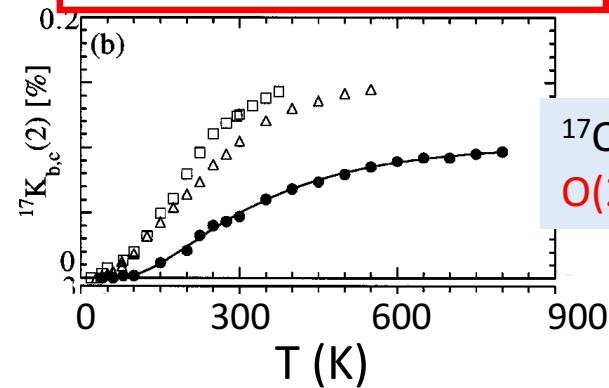
$$|K_{\text{chem}}| \sim 0.02(\%) \ll K_{\text{spin}}$$

^{17}O NMR successfully probed a spin liquid state in the two-leg ladder layers of $\text{A}_{14}\text{Cu}_{24}\text{O}_{41}$
 although the bulk spin susceptibility is dominated by chain layers !

T. Imai et al., PRL 81 (1998) 220.



Spin liquid on two-leg ladder layer



^{17}O NMR Knight shift at O(2) sites reflects χ_{Ladder}

^{17}O nuclear spins at O(1) and O(2) sites couple mostly with Cu electron spins in the ladder layers

First generation ^{63}Cu , ^1H and ^{35}Cl , NMR in partially aligned powder sample of $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$

T. I. *et al.*, PRL 100 (2008) 077203

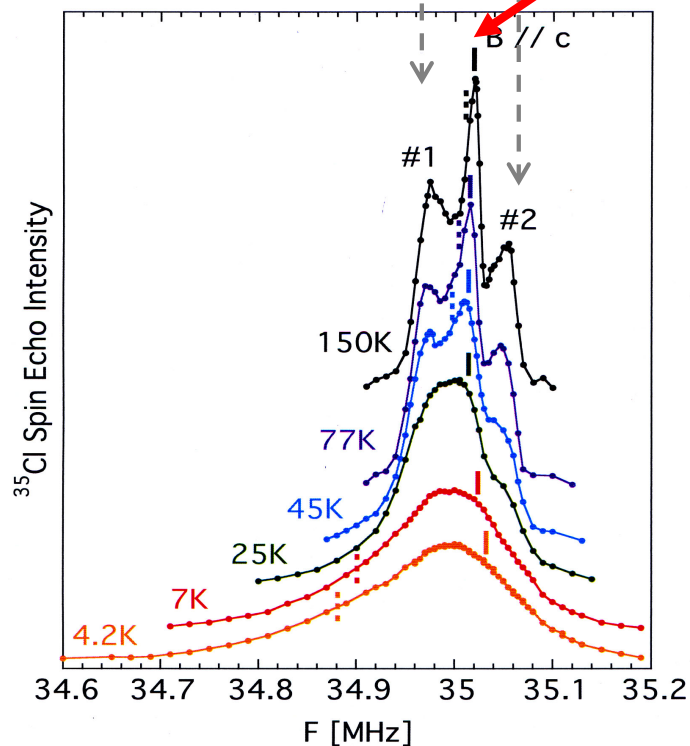
$^{63,65}\text{Cu}$ NMR : Direct but inconvenient probe (nuclear quadrupole interaction too large).

^1H NMR : hyperfine coupling is too small, compared with line broadening induced by defect spins

^{35}Cl nuclear spin has decent strength of *negative* hyperfine coupling with Cu electron spins.

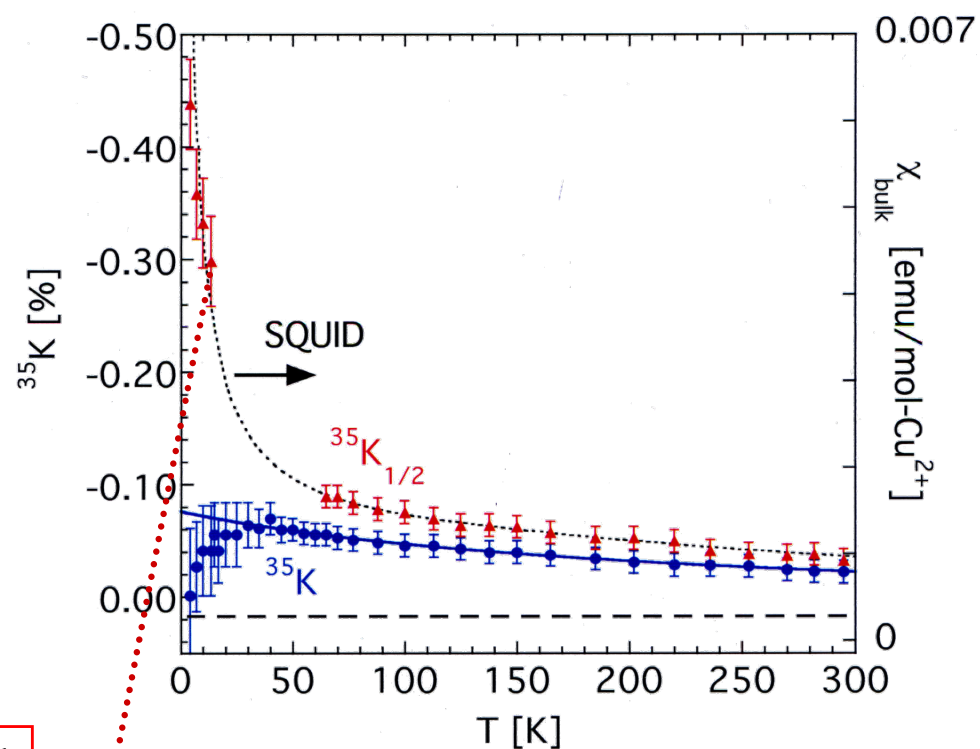
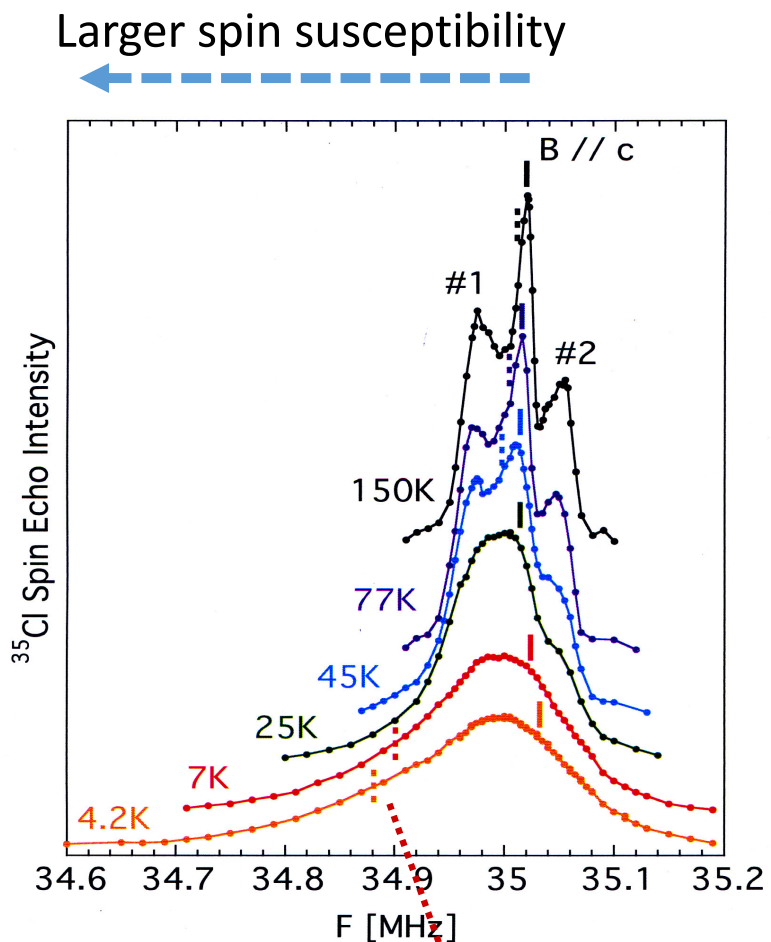
Undesirable shoulders #1 & #2 from other grains split by second order nuclear quadrupole interaction (to be ignored)

Main ^{35}Cl NMR peak from grains aligned along the c-axis



^{35}Cl NMR in partially aligned powder sample of $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$

T. I. et al., PRL 100 (2008) 077203

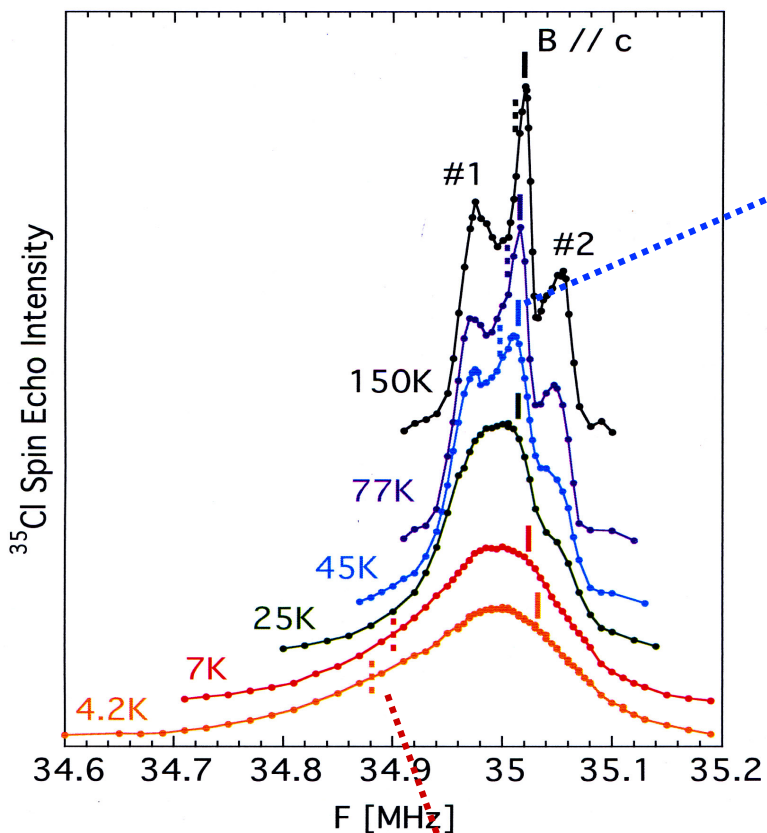


Asymmetrically broadened. Low frequency tail reflects large Curie-Weiss defect susceptibility.

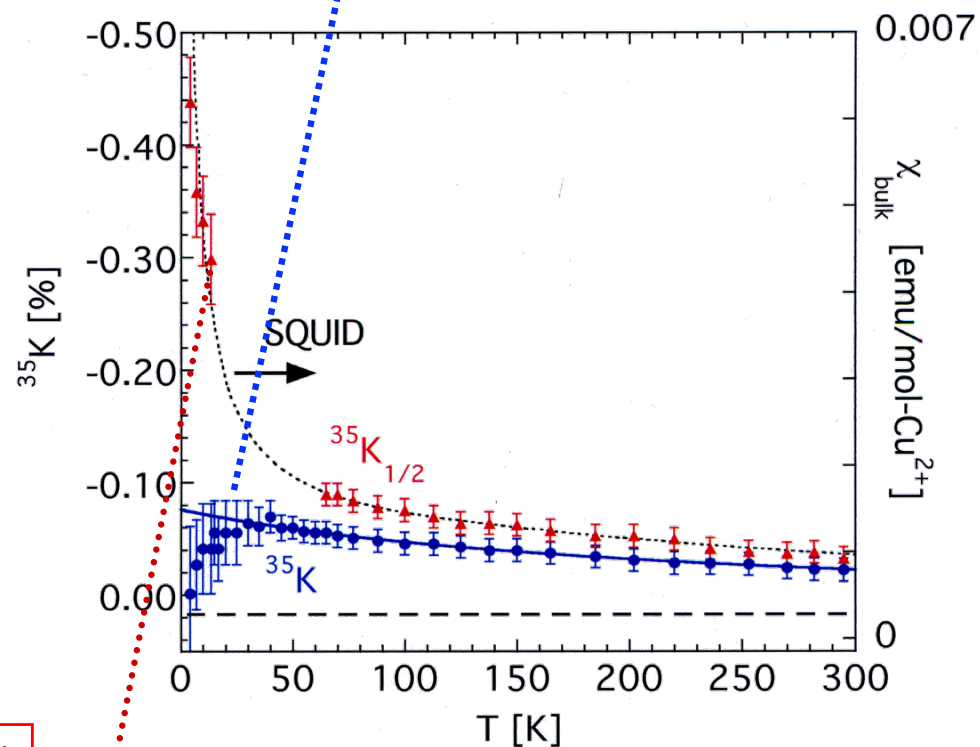
^{35}Cl NMR in partially aligned powder sample of $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$

T. I. et al., PRL 100 (2008) 077203

Larger spin susceptibility

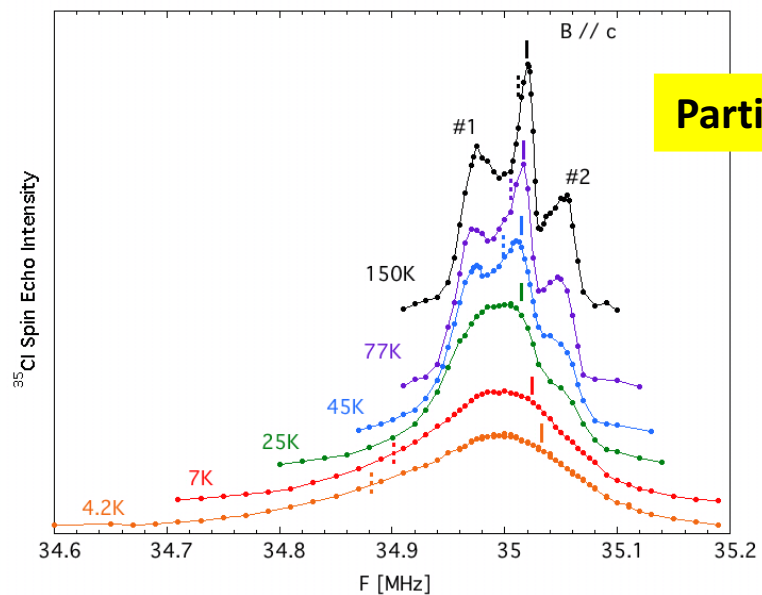


Main peak seems to suggest $\chi_{\text{kagome}} \rightarrow 0$ at $T = 0$, but inconclusive

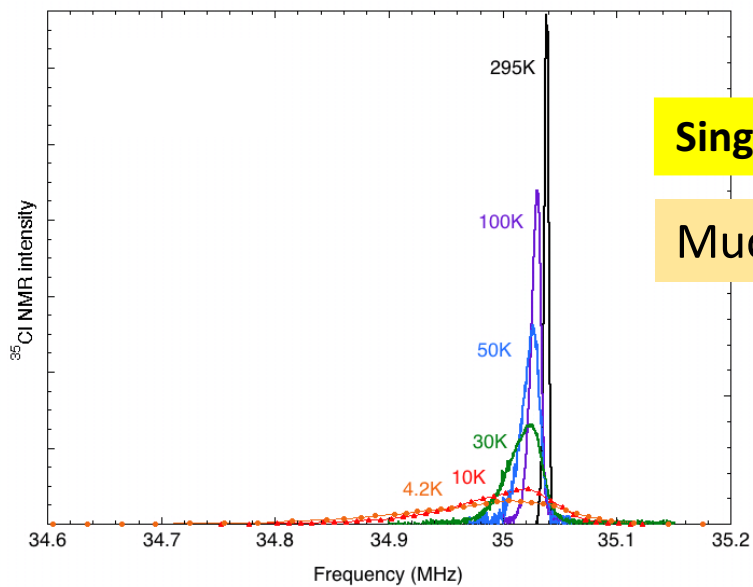


Asymmetrically broadened. Low frequency tail reflects large Curie-Weiss defect susceptibility.

Advantages of single crystal NMR of $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$



Partially aligned powder



Single crystal (B || c)

Much higher resolutions!

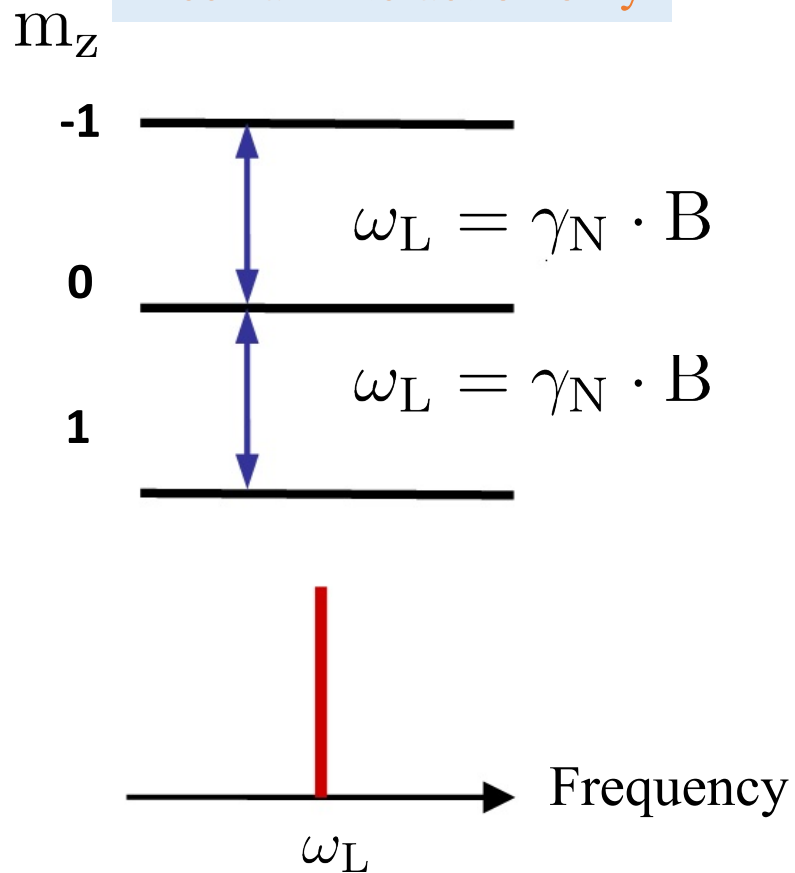
Second generation ^2D (nuclear spin $I = 1$) NMR in $\text{ZnCu}_3(\text{OD})_6\text{Cl}_2$

deuterated single crystal

T. I. *et al.*, PRB 83(2011) 020411 (Rapid).

$$H = -\gamma_n \hbar \mathbf{B} \cdot \mathbf{I}$$

Zeeman interaction only



Second generation ^2D (nuclear spin $I = 1$) NMR in $\text{ZnCu}_3(\text{OD})_6\text{Cl}_2$

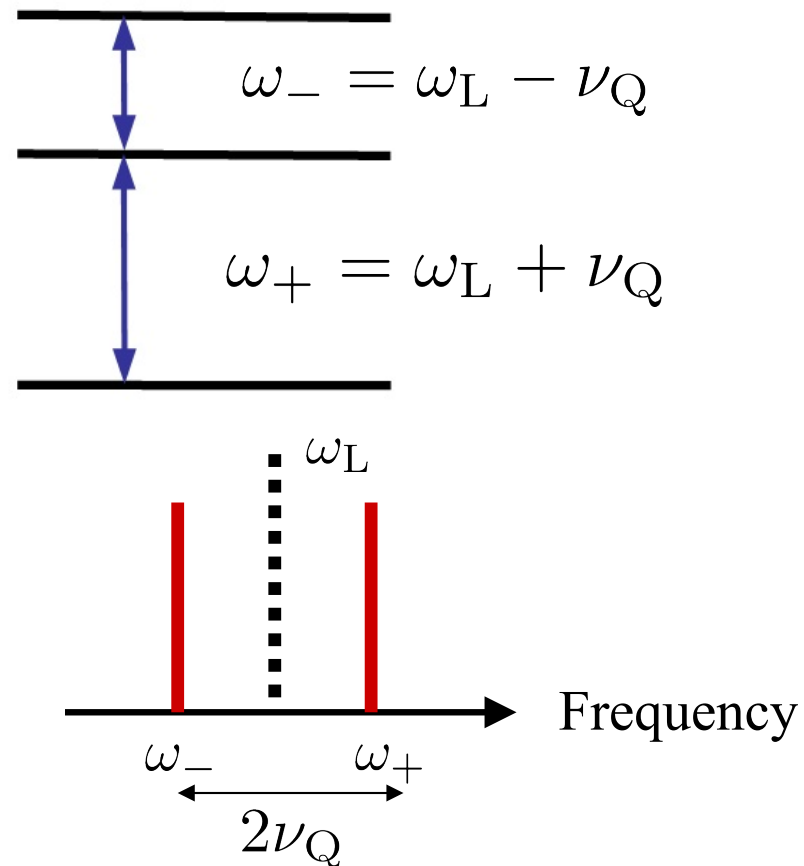
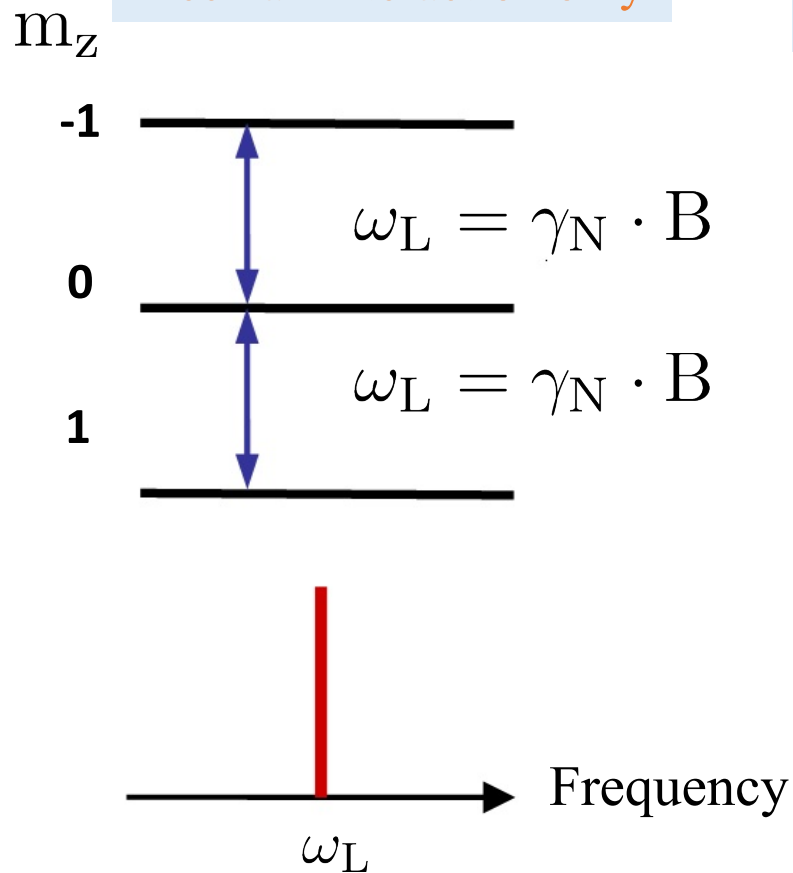
deuterated single crystal

T. I. et al., PRB 83(2011) 020411 (Rapid).

$$H = -\gamma_n \hbar \mathbf{B} \cdot \mathbf{I} + \frac{\hbar \nu_Q^Z}{6} \{3I_z^2 - I(I+1) + \eta(I_x^2 - I_y^2)\}$$

Zeeman interaction only

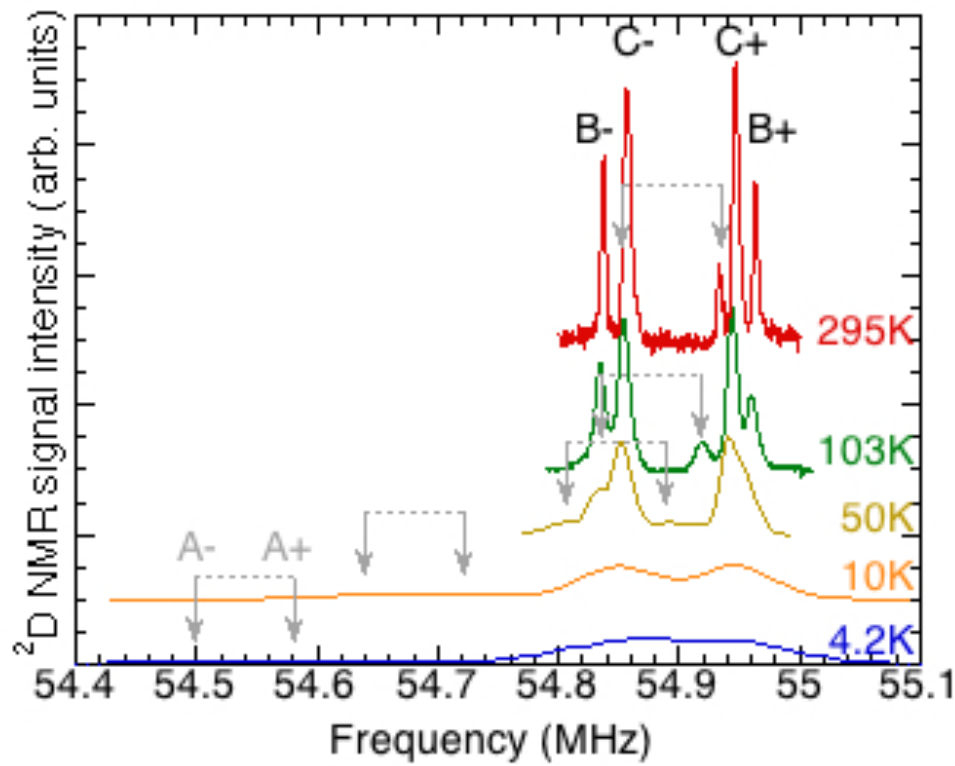
Nuclear quadrupole interaction with charge/lattice



^2D single crystal NMR revealed 14% Zn^{2+} sites are occupied by Cu^{2+} defects in $\text{ZnCu}_3(\text{OD})_6\text{Cl}_2$

3 pairs of ^2D NMR signals from 3 inequivalent ^2D sites

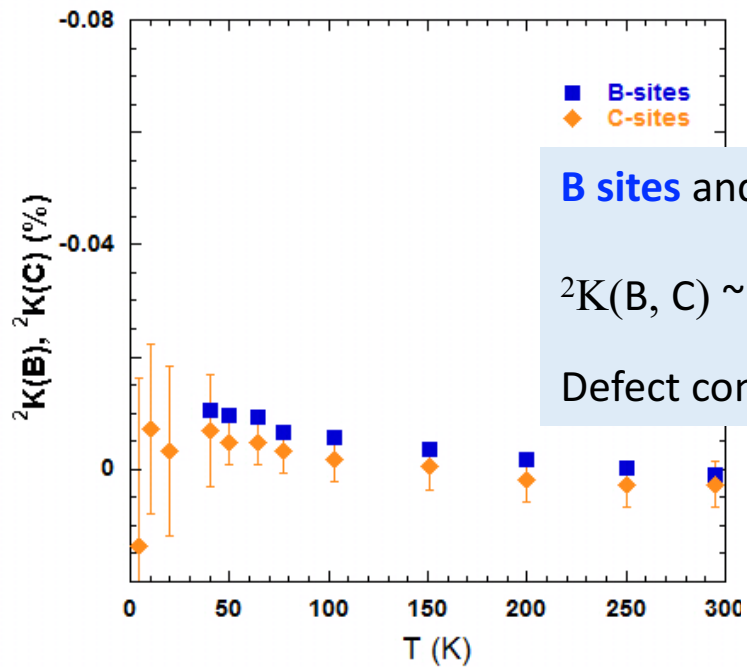
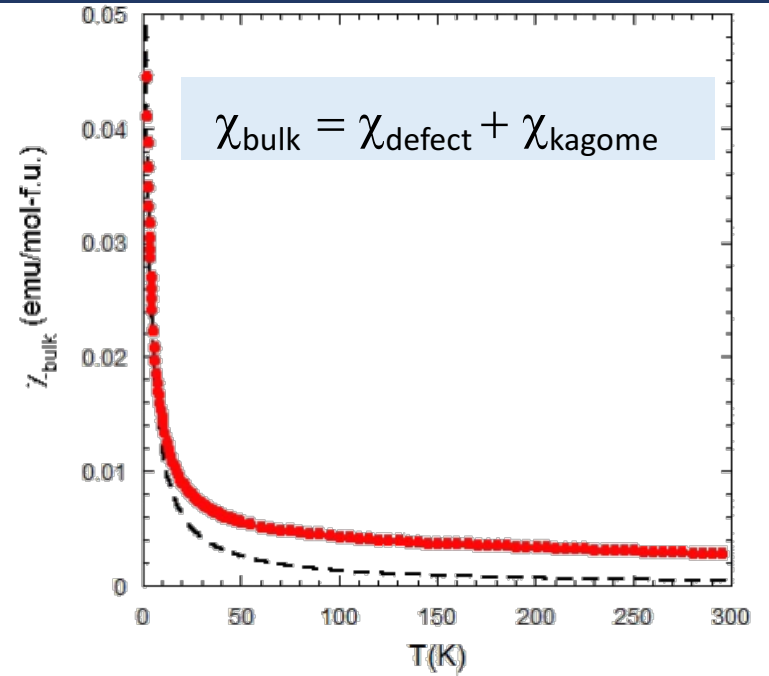
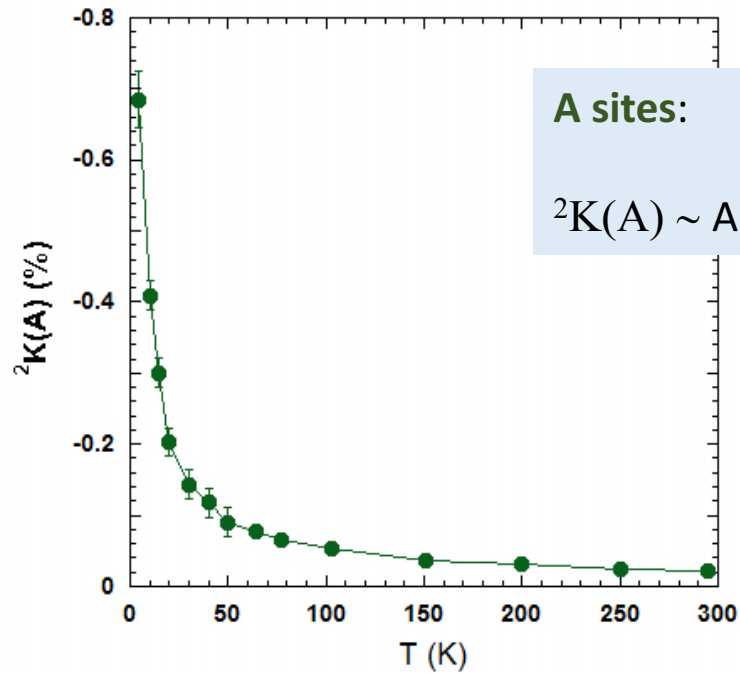
- A sites** (~14% population) : **NN of Cu^{2+} defects** occupying Zn^{2+} non-magnetic sites.
- B sites** (~28% population) : **NNN of Cu^{2+} defects** occupying Zn^{2+} non-magnetic sites
- C sites** (~58% population) : **No defects nearby**



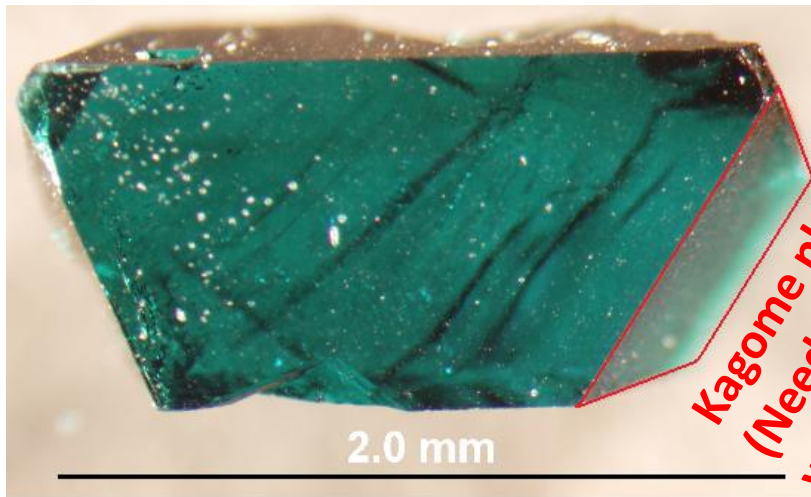
Consistent with $\text{Zn}_{0.86}\text{Cu}_{3.14}(\text{OD})_6\text{Cl}_2$;
~14% of Zn^{2+} sites are occupied by Cu^{2+}
defect spins

No evidence for anti-site Zn^{2+} defects
occupying Cu^{2+} sites

Defect spin susceptibility probed by 2D A sites in $\text{ZnCu}_3(\text{OD})_6\text{Cl}_2$



Change of strategy: angle-dependent ^{17}O (nuclear spin $I = 5/2$) NMR for isotope-enriched single crystal



*Kagome plane
(Need to be aligned
with magnetic field)*

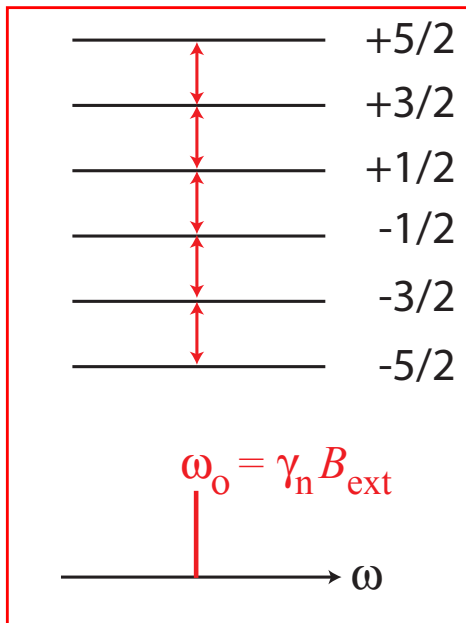


Single crystal courtesy of T.-H. Han & Y.S. Lee

Compact goniometer for NMR & X-ray designed by M. Fu

Nuclear spin Hamiltonian for ^{17}O (nuclear spin $I = 5/2$) and resonant peak(s)

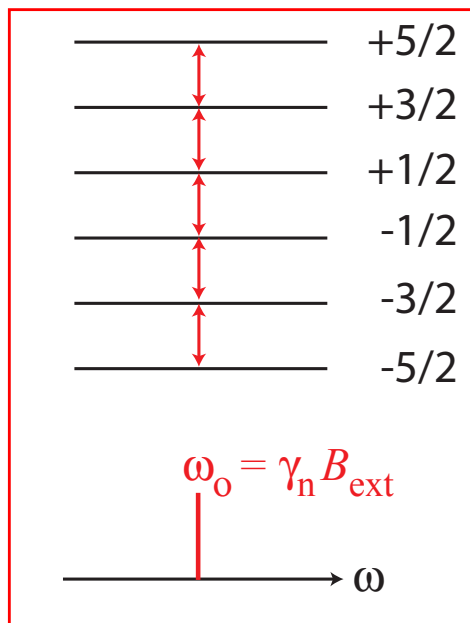
$$\hat{H} = \gamma_n \vec{B}_{ext} \cdot \vec{I}$$



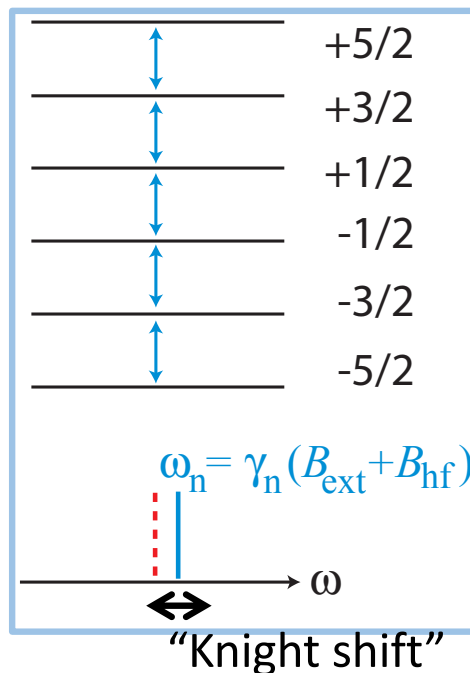
Zeeman only

Nuclear spin Hamiltonian for ^{17}O (nuclear spin $I = 5/2$) and resonant peak(s)

$$\hat{H} = \gamma_n \vec{B}_{ext} \cdot \vec{I} + \gamma_n \vec{B}_{hf} \cdot \vec{I}$$



Zeeman only



Zeeman + hyperfine

NMR frequency shifts to

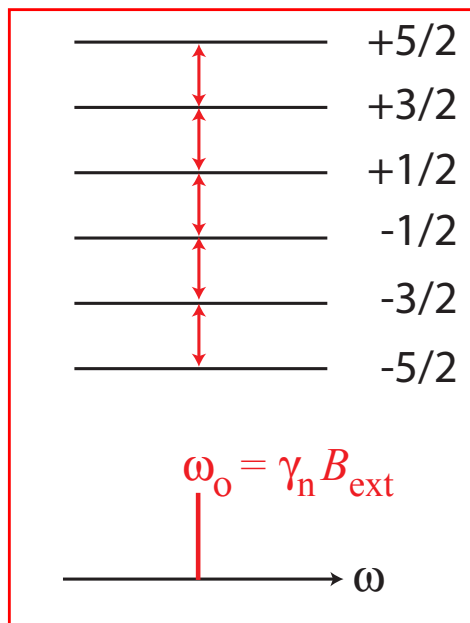
$$\omega_n = \omega_0(1 + K)$$

where
$$K = \frac{A_{hf}}{N_A \mu_B} \chi_{spin} + K_{chem}$$

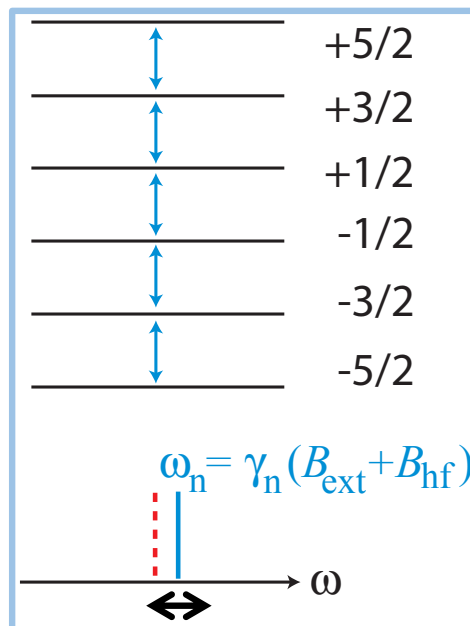
and $|K_{chem}| \sim 0.02(\%) \ll K_{spin}$

Nuclear spin Hamiltonian for ^{17}O (nuclear spin $I = 5/2$) and resonant peak(s)

$$\hat{H} = \gamma_n \vec{B}_{ext} \cdot \vec{I} + \gamma_n \vec{B}_{hf} \cdot \vec{I} + \frac{\nu_Q}{2} \hat{I}_z^2 + \dots$$

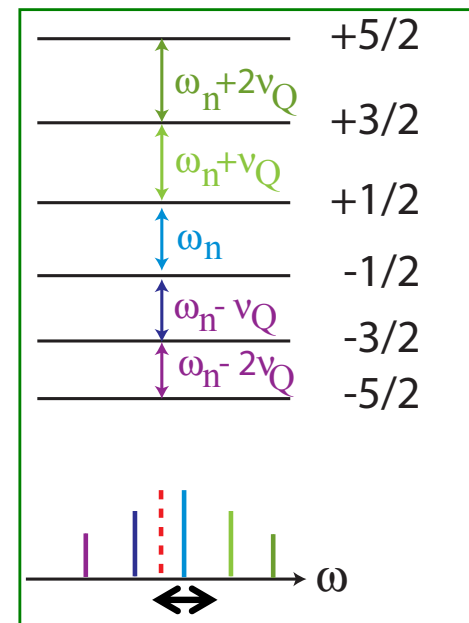


Zeeman only



"Knight shift"

Zeeman + hyperfine



"Knight shift"

Zeeman + hyperfine + quadrupole interaction

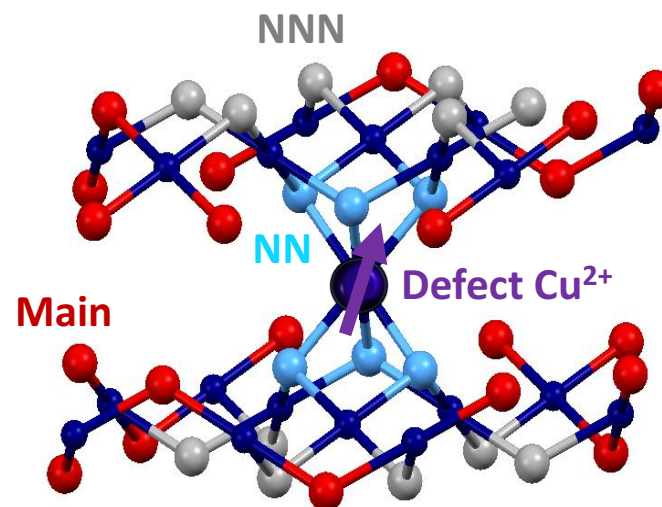
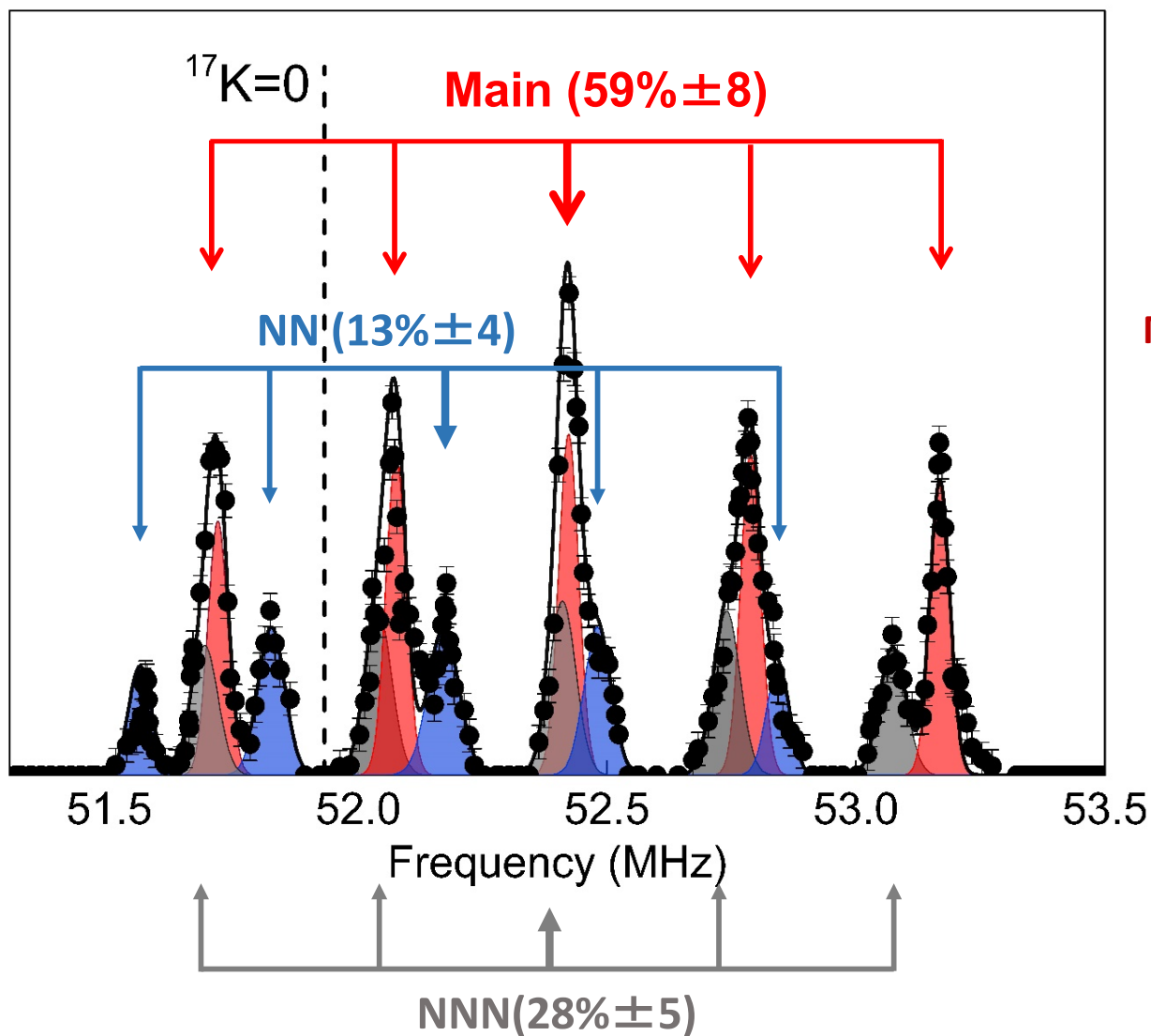
NMR frequency shifts to

$$\omega_n = \omega_0(1 + K)$$

where
$$K = \frac{A_{hf}}{N_A \mu_B} \chi_{spin} + K_{chem}$$

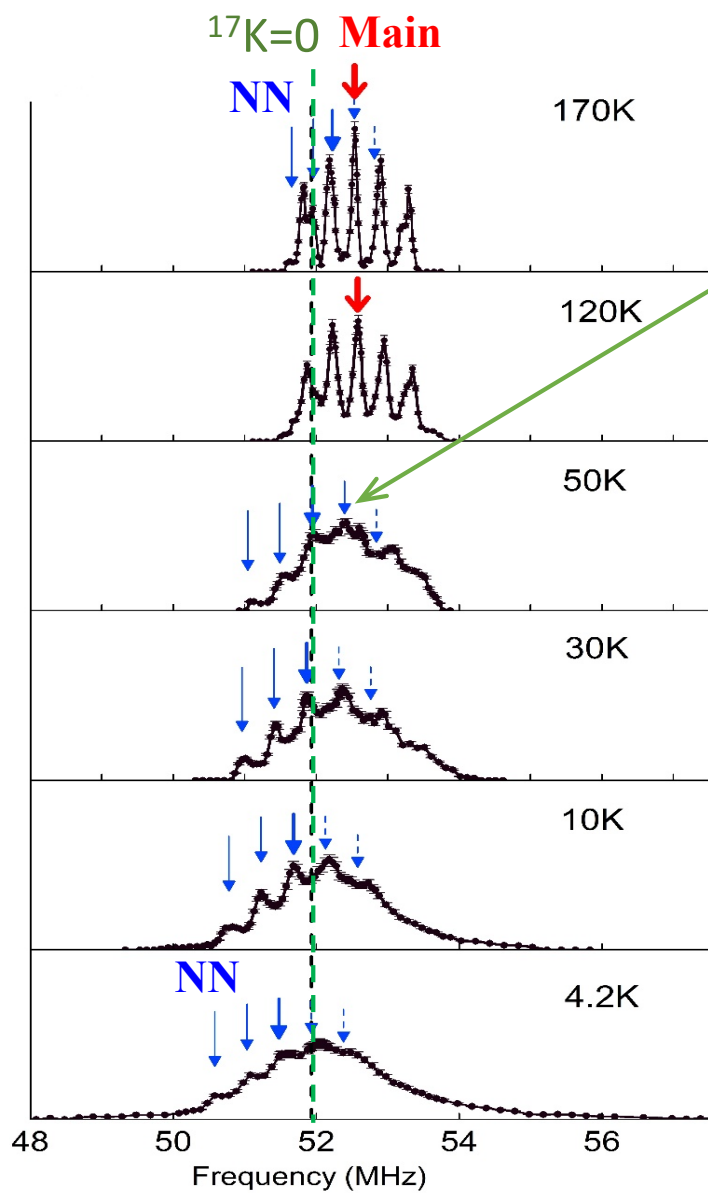
and $|K_{chem}| \sim 0.02(\%) \ll K_{spin}$

^{17}O NMR lineshape of $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$ single crystal in $B_{\text{ext}} \parallel c$



Temperature dependence of ^{17}O NMR lineshapes in $B_{\text{ext}} \parallel c$

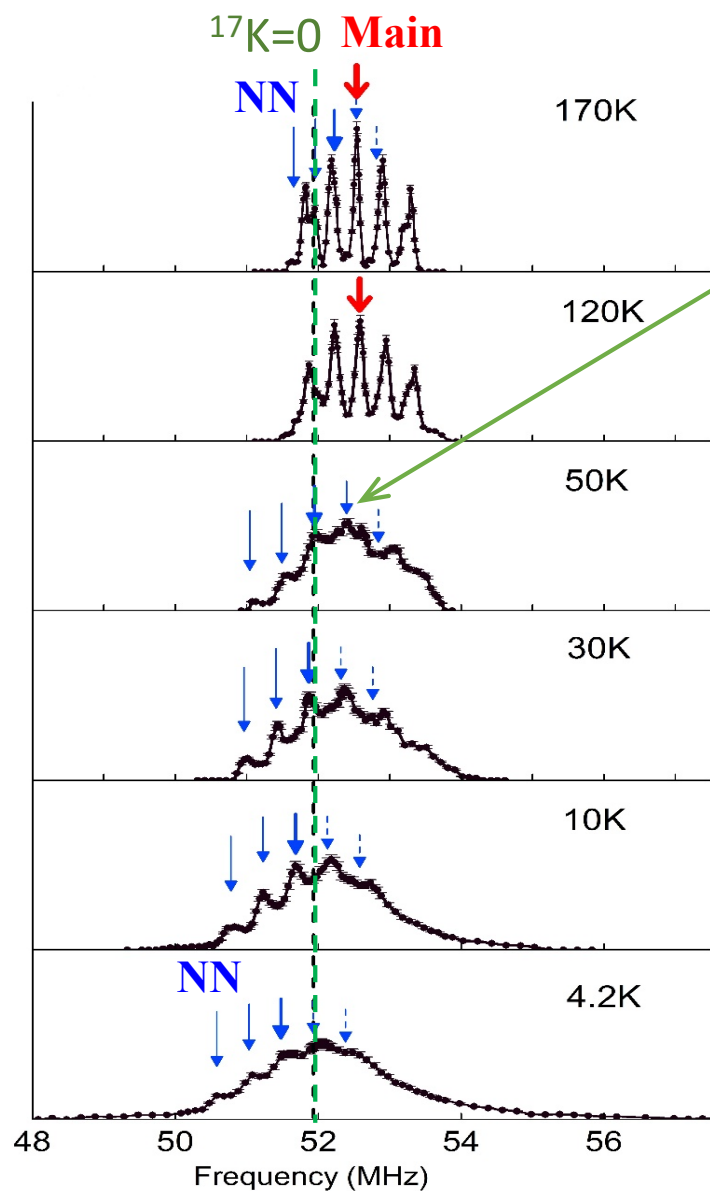
M Fu *et al.* Science (2015)



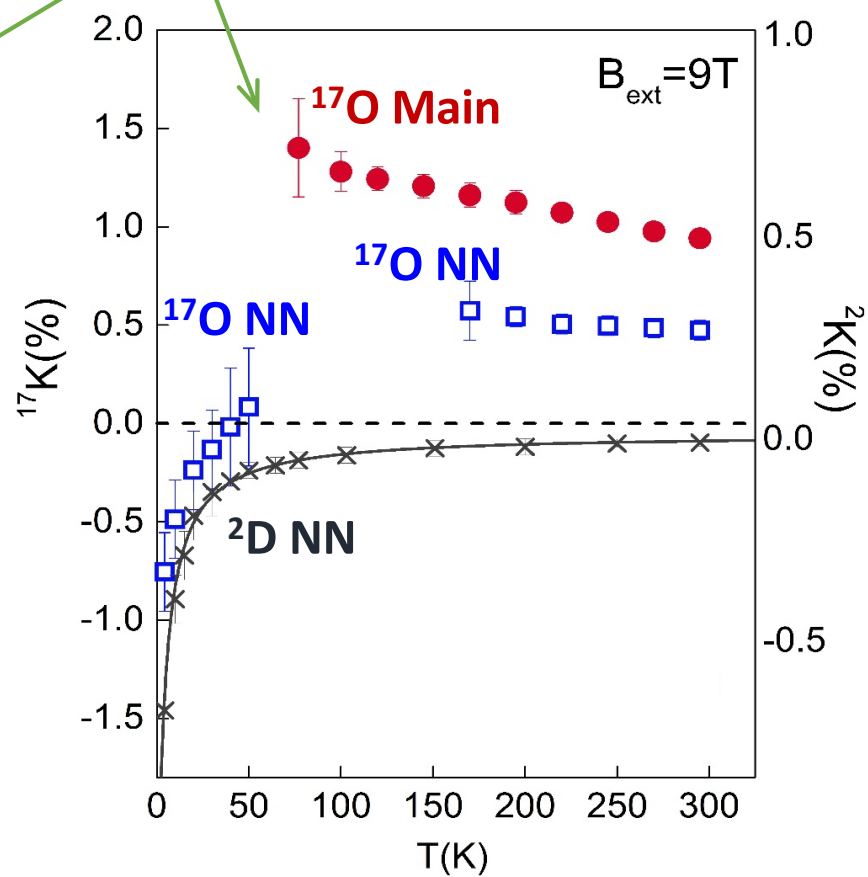
We cannot resolve the crucial center peak of the **Main sites** below $\sim 50\text{K}$

Temperature dependence of ^{17}O NMR lineshapes in $B_{\text{ext}} \parallel c$

M. Fu *et al.* Science (2015)

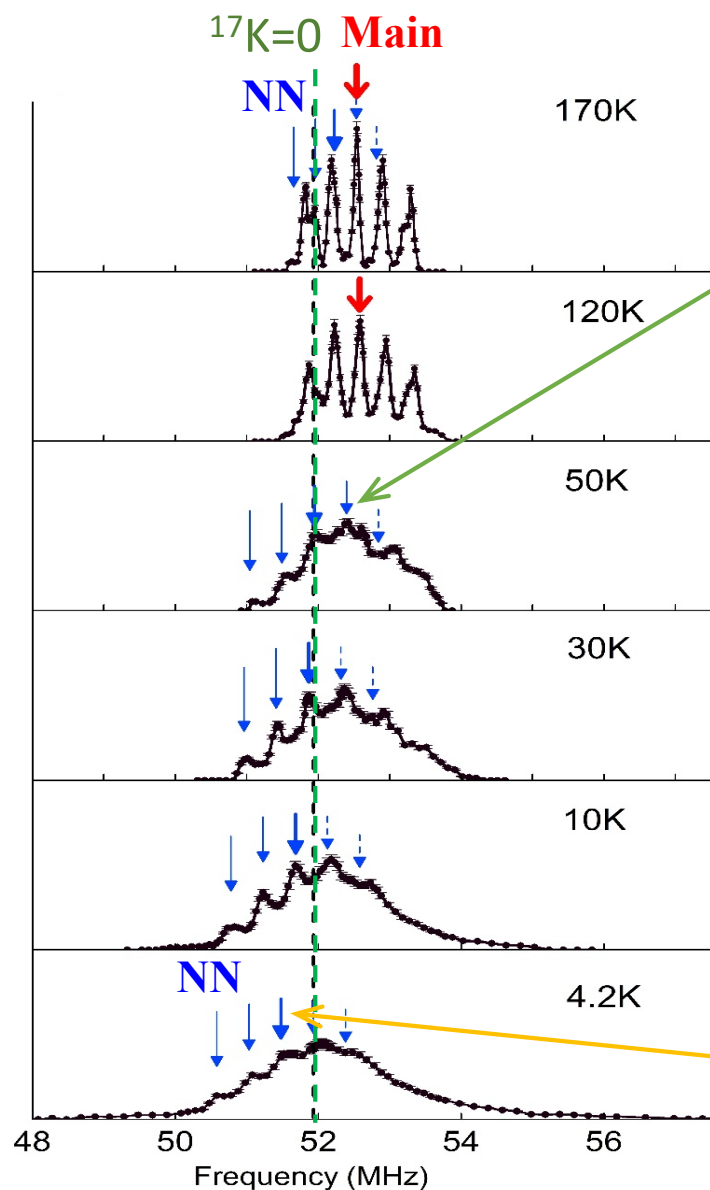


We cannot resolve the crucial center peak of the **Main sites** below $\sim 50\text{K}$

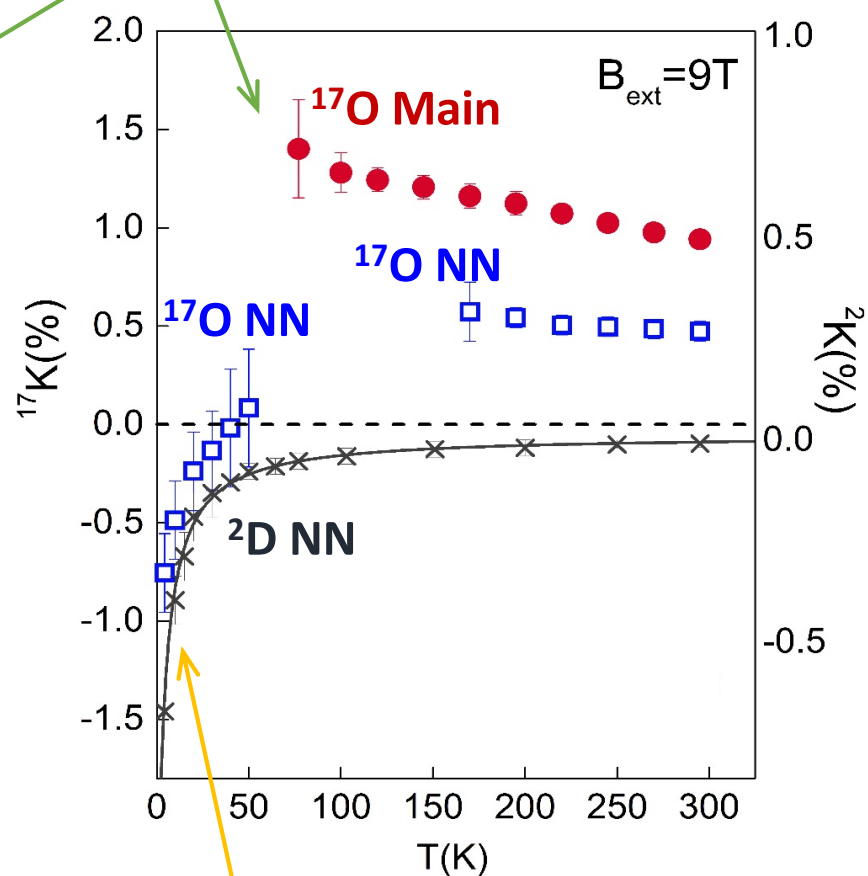


Temperature dependence of ^{17}O NMR lineshapes in $B_{\text{ext}} \parallel c$

Fu *et al.* Science (2015)



We cannot resolve the crucial center peak of the **Main sites** below $\sim 50\text{K}$



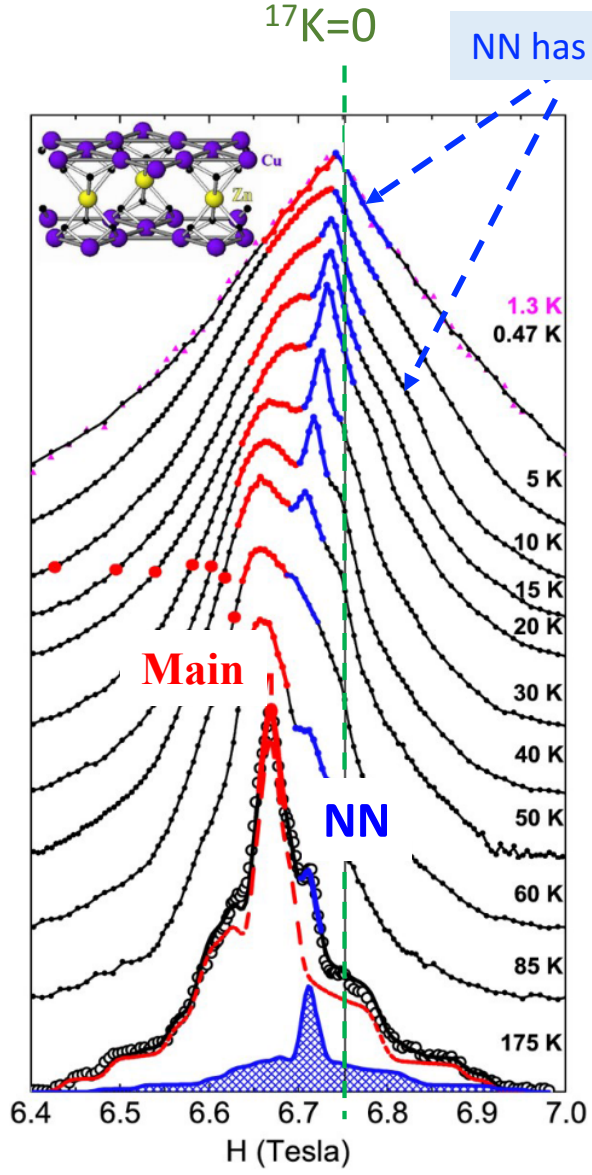
Low T behavior at ^{17}O and ^{2}D NN sites is dominated by a large Curie - Weiss contribution,

$$\chi_{\text{defect}} \sim \frac{C}{T + \theta}$$

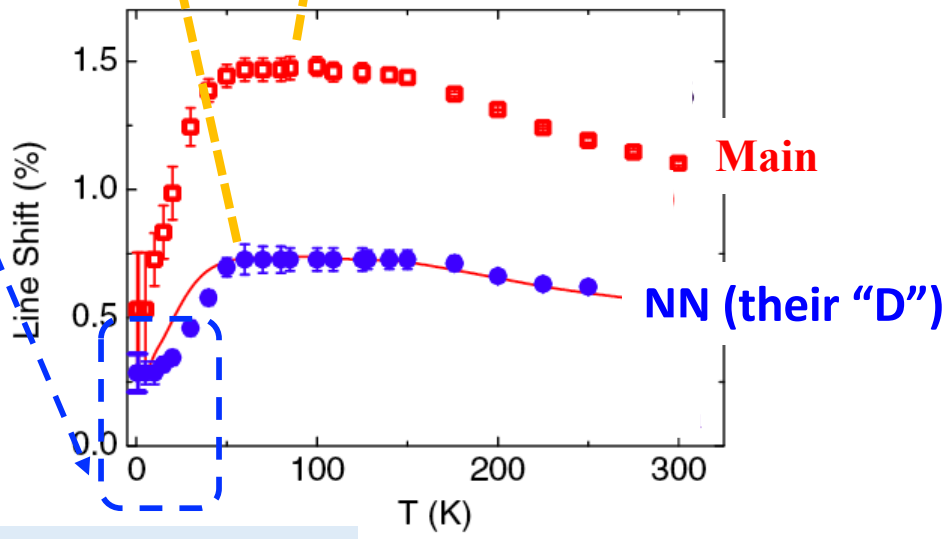
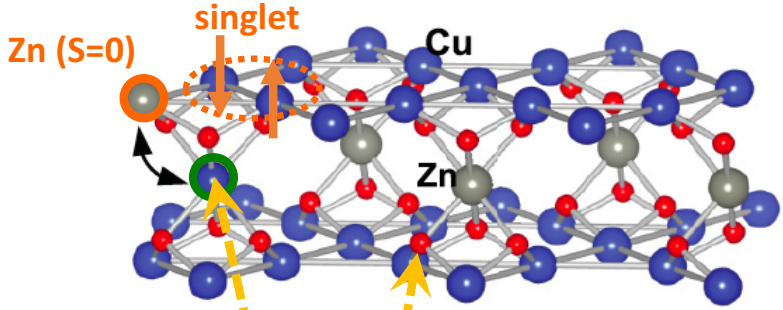
with $\theta \sim 1$ K and negative hyperfine coupling $A_{\text{hf}} < 0$

(Side) Earlier powder ^{17}O results are consistent with our data (NOT a proof of anti-site defects)

Olariu, Mendels *et al.*, PRL 100 (2008) 087202



NN has negative shifts at low T

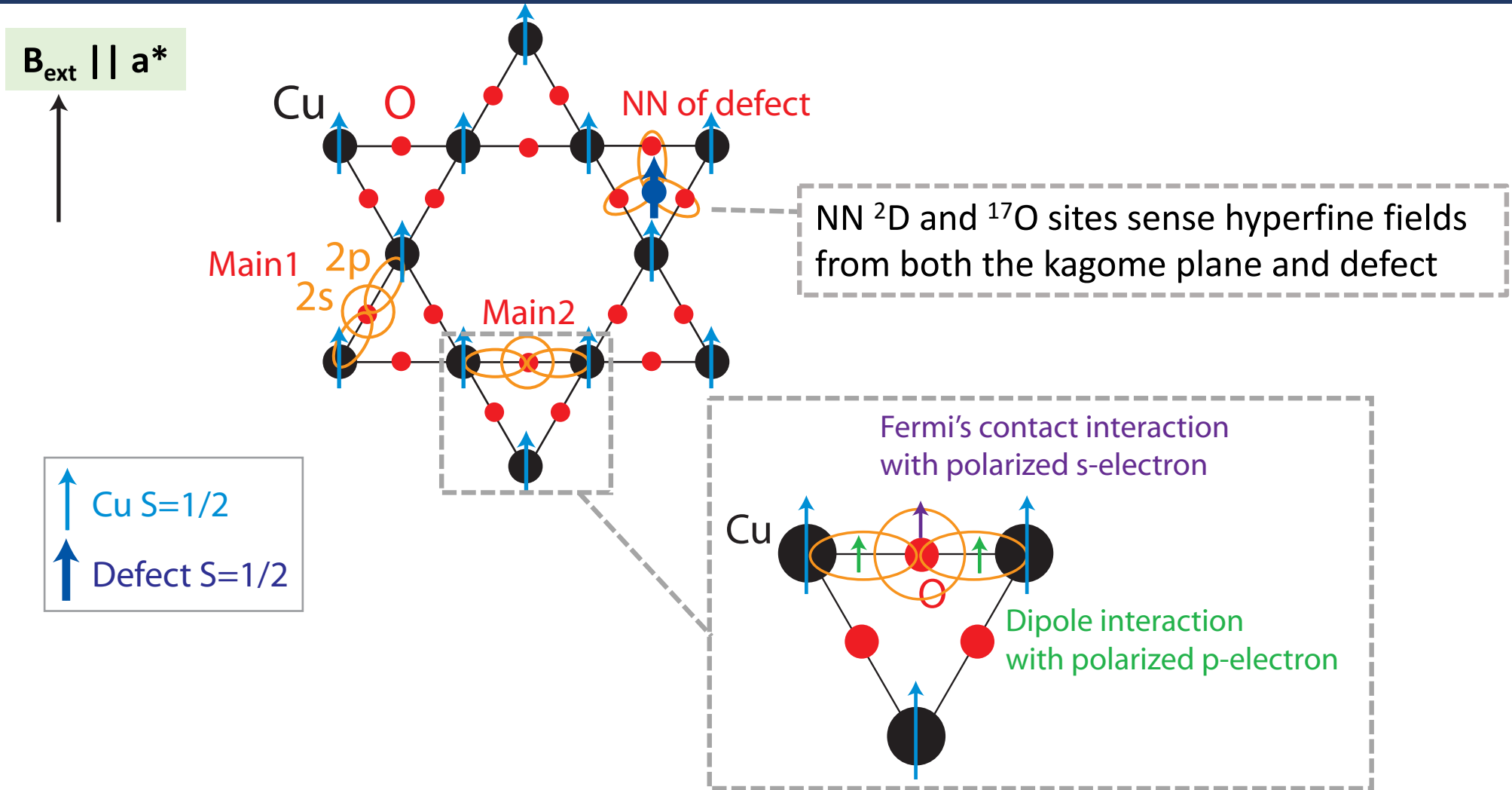


NN data points should have been negative

← Positive shift (in field swept mode)

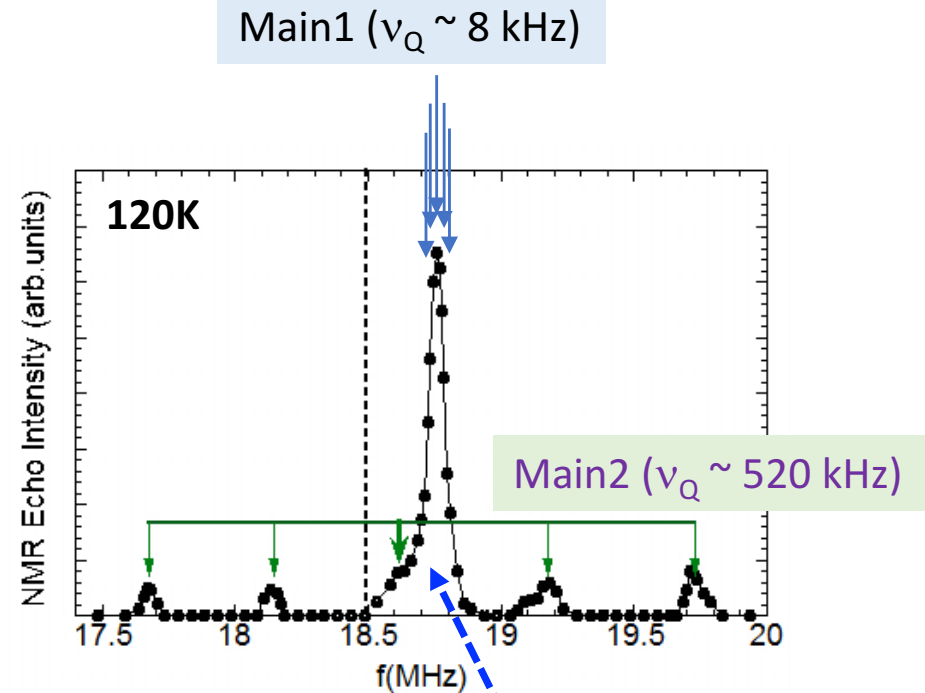
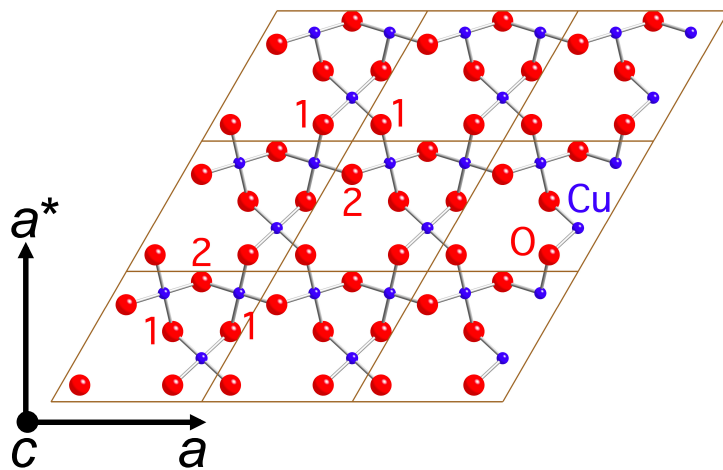
Try a different field geometry : $B_{\text{ext}} \parallel a^*$

(which we initially thought would be hopelessly complicated)



- Hybridization between O 2s & 2p orbitals and Cu 3d orbital(s) transfers spin polarization to O sites.
- The latter interacts with the ^{17}O nuclear spin.
- *Main1, Main2, NN sites have different hyperfine fields from Cu sites, hence each of 5 NMR transitions split*

Intrinsic susceptibility χ_{kagome} of the kagome plane as determined from the ^{17}O Knight shift in $B = 3.2 \text{ T} \parallel a^*$



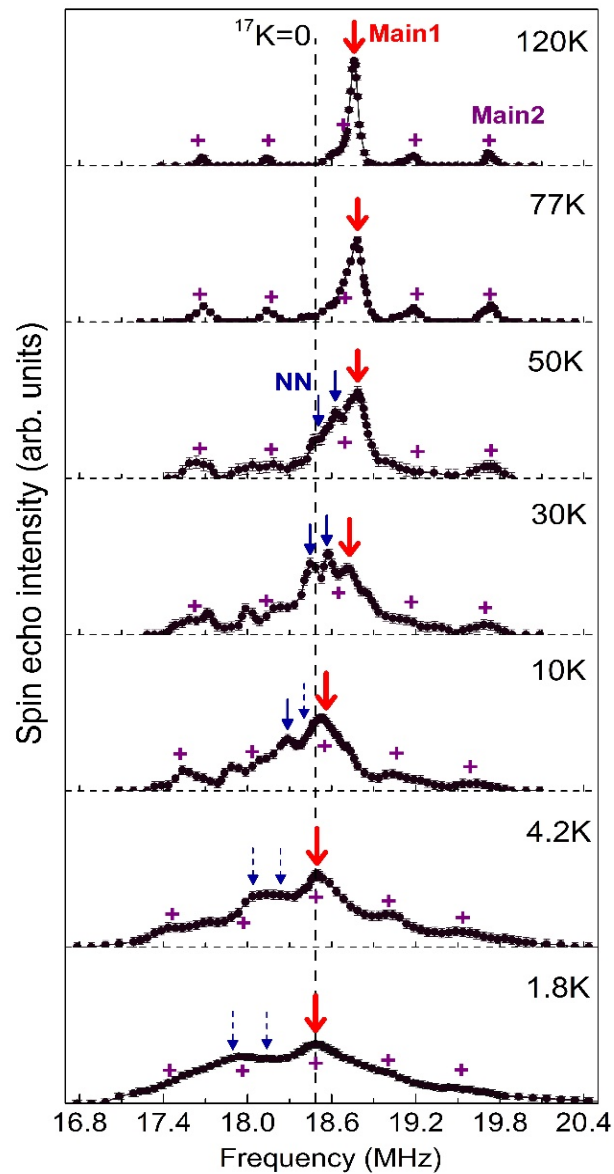
Hyperfine tensors depend on the relative orientation of the magnetic field B with respect to the Cu-O-Cu bond axis.




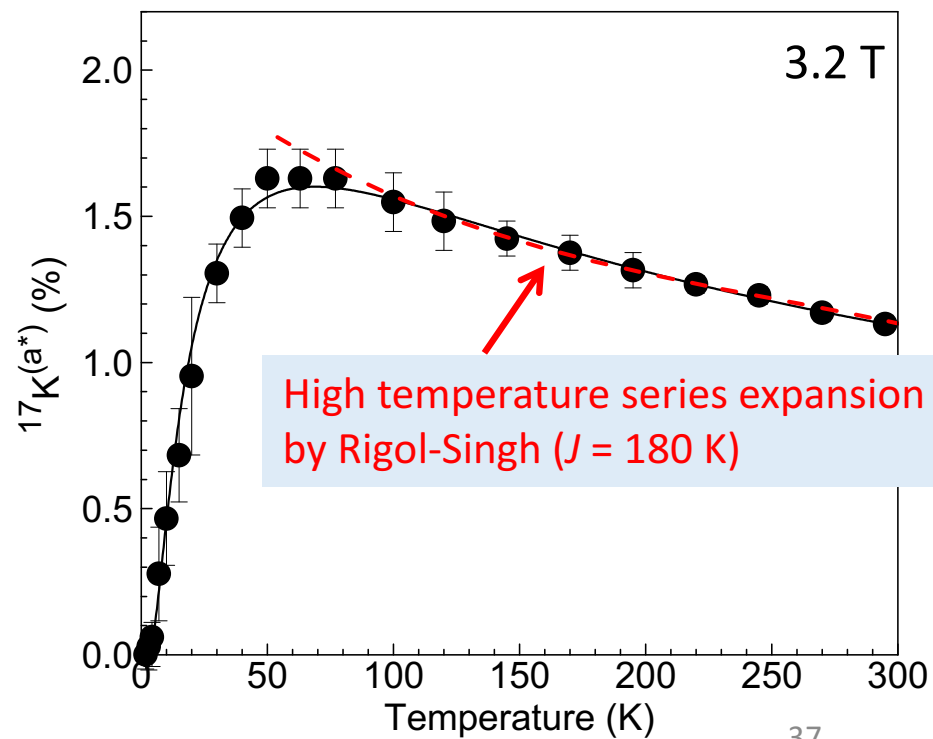
^{17}O NMR signals at “**Main1**” and “**Main2**” sites appear separately with the intensity ratio $\sim 2 : 1$.

“**Main1**” sites happen to have $\nu_Q \sim 0$ for $B \parallel a^*$. All 5 transitions appear together as a **gigantic peak!!**

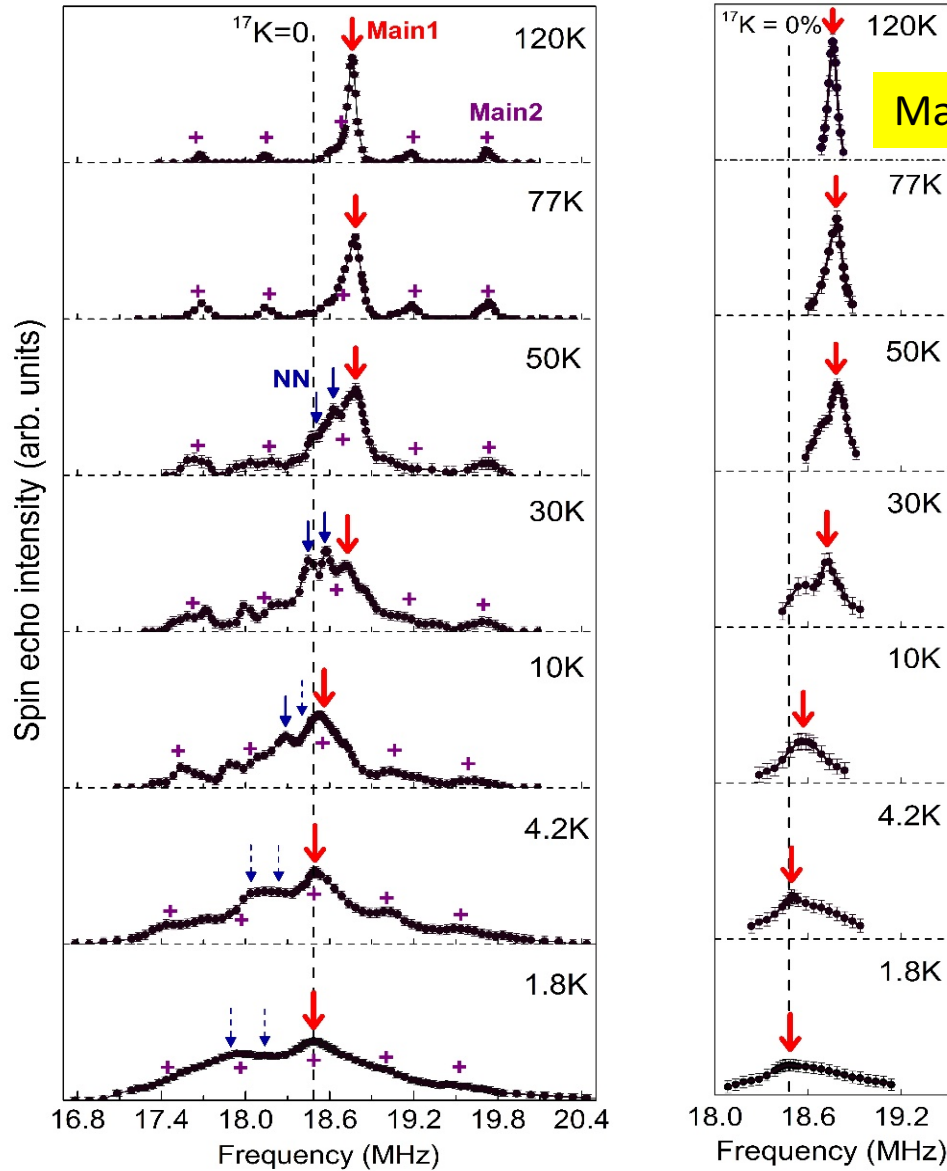
Intrinsic susceptibility χ_{kagome} of the kagome plane as determined from the ^{17}O Knight shift at the main sites measured with $B = 3.2 \text{ T} \parallel a^*$




 Larger frequency shift
 Larger ^{17}K and χ_{kagome}



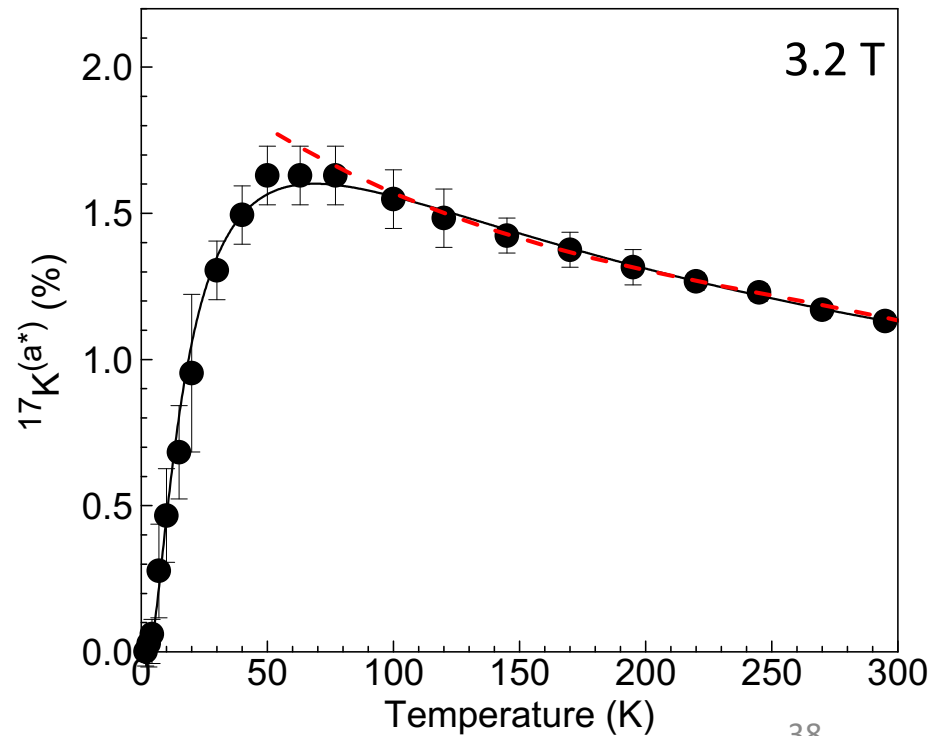
Intrinsic susceptibility χ_{kagome} of the kagome plane as determined from the ^{17}O Knight shift at the main sites measured with $B = 3.2 \text{ T} \parallel a^*$



Main1 only (measured with long RF pulses)

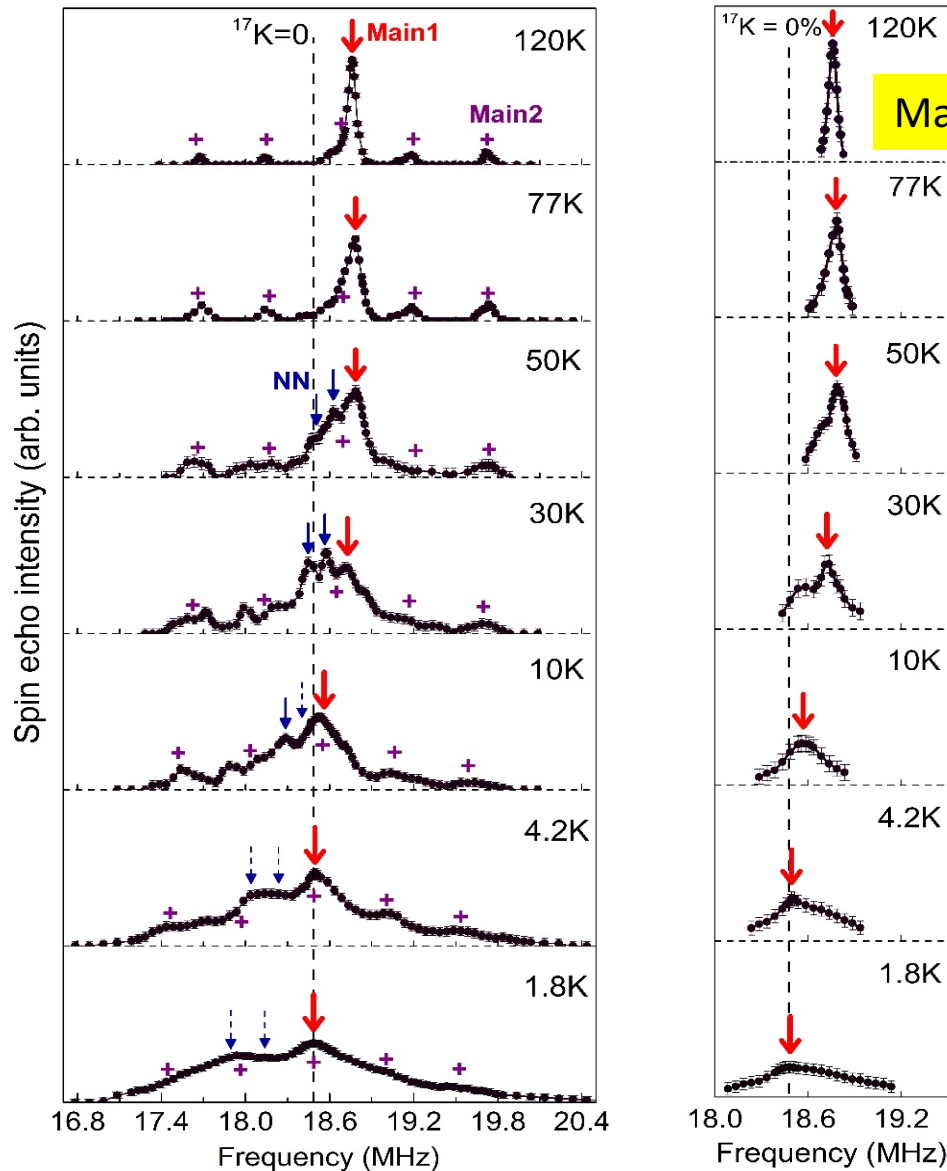
The optimal RF pulse width for Main1 is factor 2 ~ 3 times broader (because we flip all 5 transitions at the same time).

We can measure Main1 peak **selectively**, and observed the same results for ^{17}K .



→
Larger frequency shift
Larger ^{17}K and χ_{kagome}

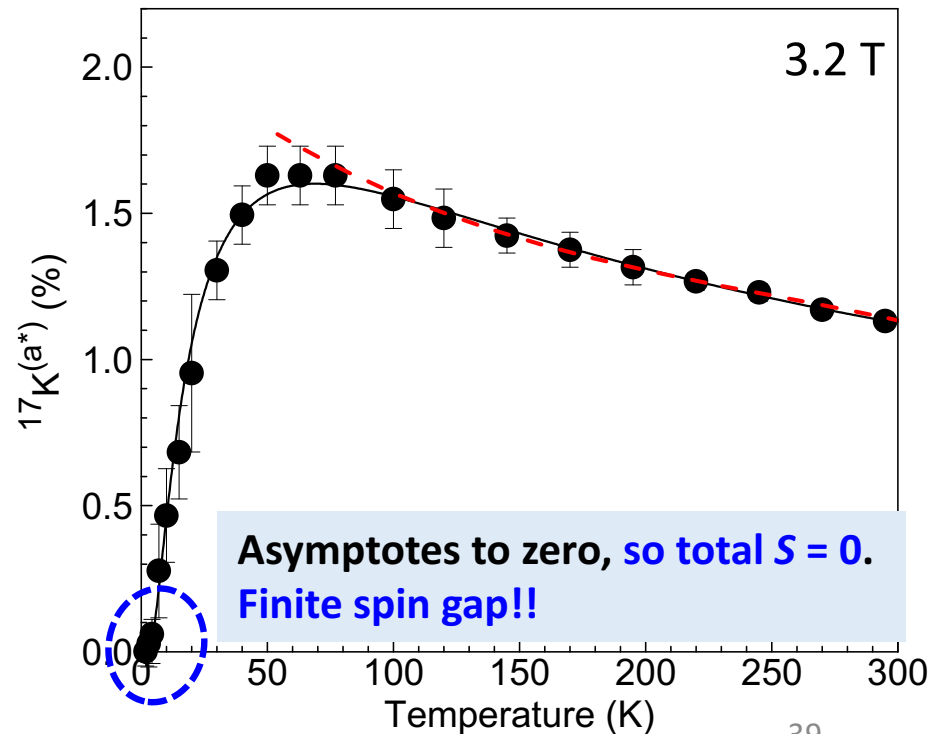
Intrinsic susceptibility χ_{kagome} of the kagome plane as determined from the ^{17}O Knight shift at the main sites measured with $B = 3.2 \text{ T} \parallel a^*$



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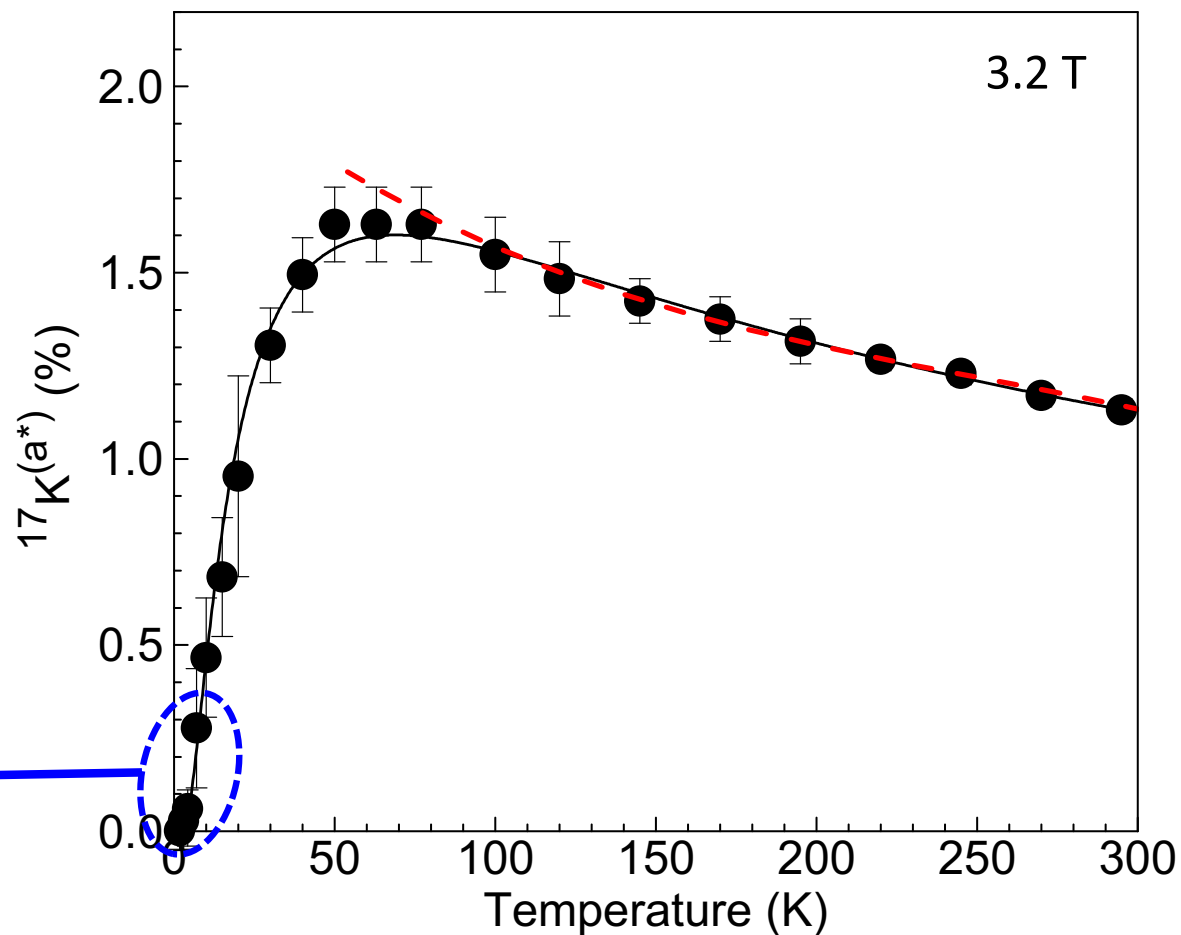
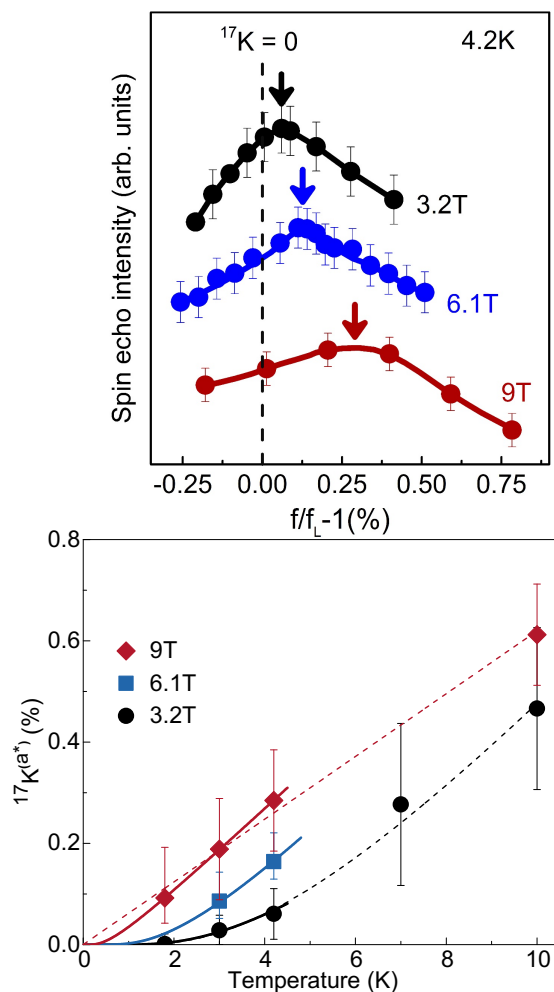


Asymptotes to zero, so total $S = 0$.
Finite spin gap!!

→
Larger frequency shift
Larger ^{17}K and χ_{kagome}

Magnetic field dependence of the gap

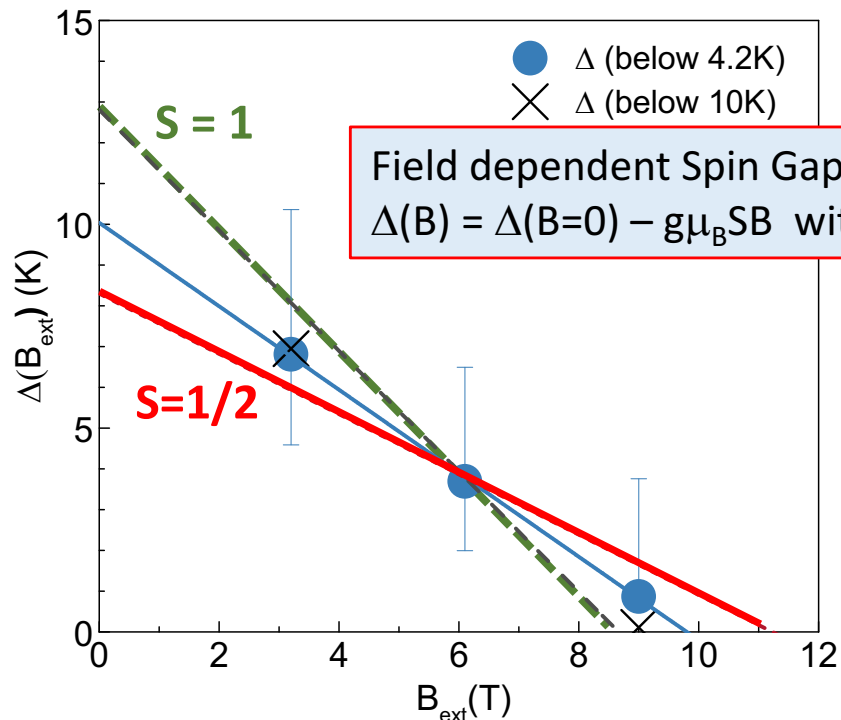
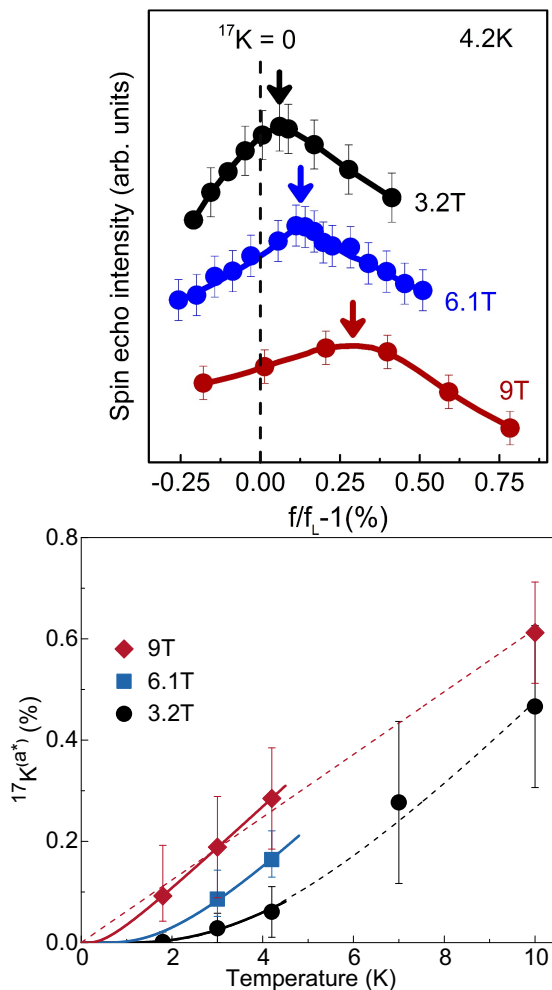
$^{17}\text{K}(\text{a}^*)$ depends on $|B|$ below $\sim 10\text{K}$



Solid (dashed) lines:
 best fit to $^{17}\text{K}(\text{a}^*) \sim T \cdot \exp(-\Delta/T)$ below 4.2 K (10 K).
 Pre-factor T: to account for the expected decrease caused by SRO
 (also arises in Dirac Fermion Model, P.A. Lee, private communications).

Magnetic field dependence of the gap: $\Delta(B_{\text{ext}} \rightarrow 0) \sim 0.05J$

$^{17}\text{K}^{(a^*)}$ depends on $|B|$ below $\sim 10\text{K}$



$\Delta(0) \sim 10\text{ K}$, hence $\Delta(0) \sim 0.05\text{ J}$

Consistent with DMRG calculations, Yan *et al.*, *Science* (2011)

Note: we cannot entirely rule out $S=1$ excitations.

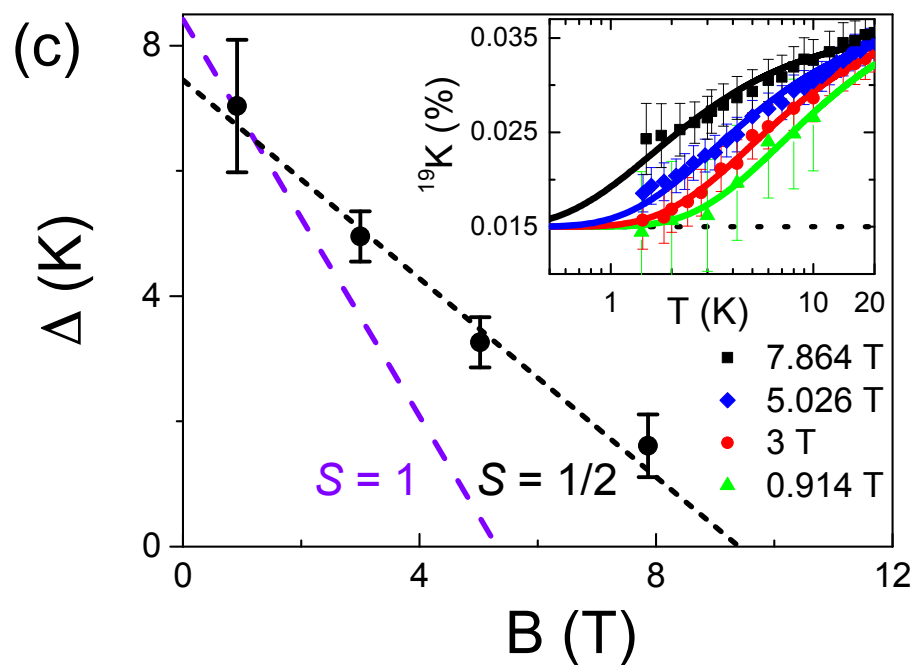
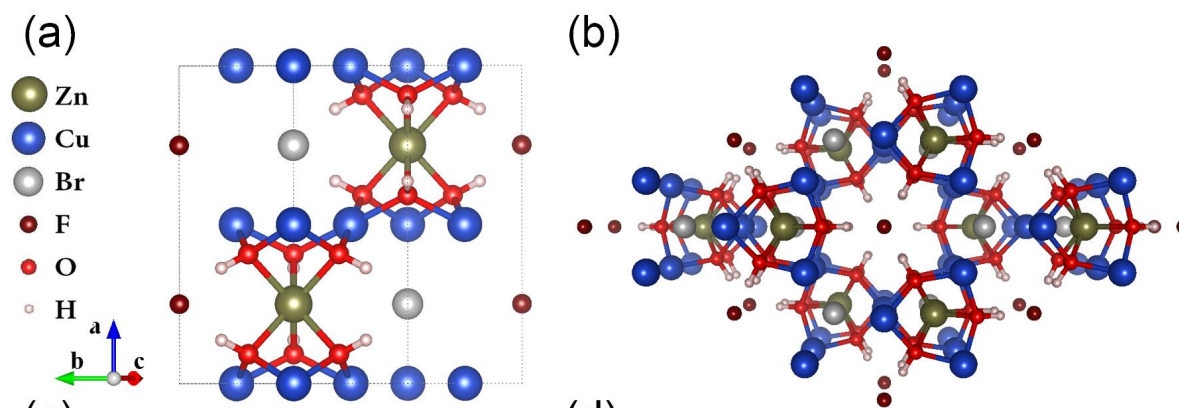
Solid (dashed) lines:

best fit to $^{17}\text{K}^{(a^*)} \sim T * \exp(-\Delta/T)$ below 4.2 K (10 K).

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Spin $\frac{1}{2}$ excitations in Barlowite $\text{Cu}_3\text{Zn}(\text{OH})_6\text{FBr}$ from ^{19}F NMR (?)

Z. Feng, G.-q. Zheng et al.
arXiv:1702.01658



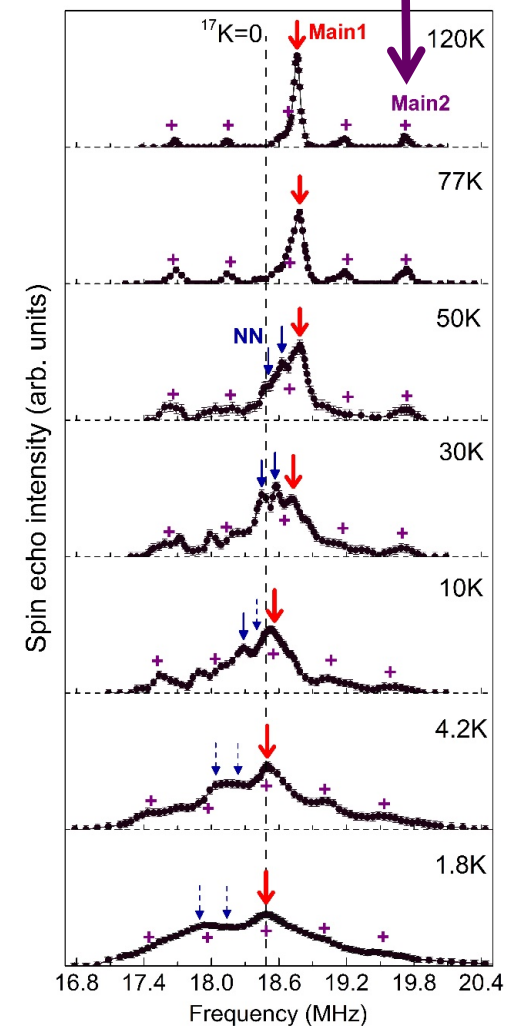
Additional evidence for a finite gap Δ based on low-frequency spin dynamics

^{17}O nuclear spin-lattice relaxation rate $1/T_1$ at Main2 sites

We measured $1/T_1$ in $B = 3.2$ or 9 T using the isolated, clean, upper-most Main2 satellite peak for the $I_z = 3/2$ to $5/2$ transition to obtain reliable results.

$$\frac{M(t)}{M(\infty)} = 1 - [0.0714 \cdot e^{-15t/T_1} + 0.2857 \cdot e^{-10t/T_1} + 0.4 \cdot e^{-6t/T_1} + 0.2143 \cdot e^{-3t/T_1} + 0.0286 \cdot e^{-t/T_1} +]$$

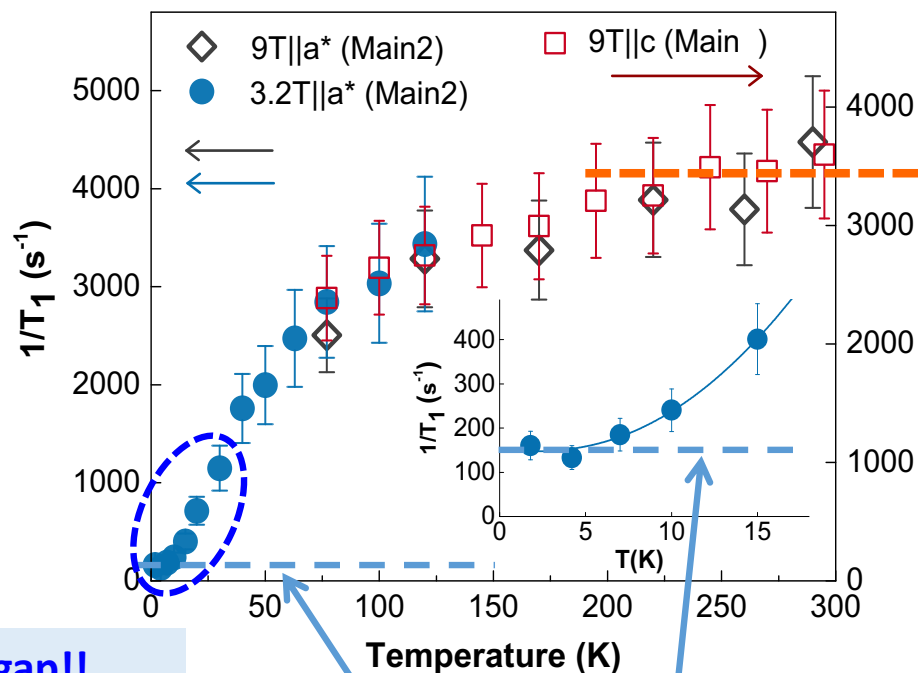
Note: this is the only way to measure $1/T_1$ accurately at the ^{17}O sites, even though the signal intensity is miserably small!



Additional evidence for a finite gap Δ based on low-frequency spin dynamics

^{17}O nuclear spin-lattice relaxation rate $1/T_1$ at the Main site

$$\frac{1}{T_1} \propto T \cdot \sum_{\vec{q}} |A_{hf}(\vec{q})|^2 \frac{\chi''(\vec{q}, f_{NMR})}{f_{NMR}} \sim \sum_{\vec{q}} |A_{hf}(\vec{q})|^2 S(\vec{q}, f_{NMR})$$

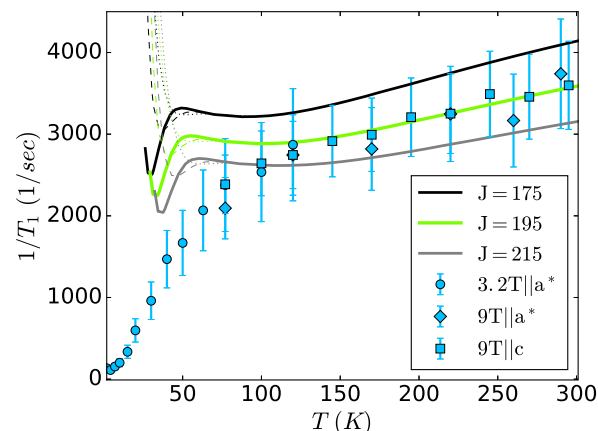


Spin gap!!
 $\Delta \sim 7$ K in 3.2T

Defect contribution
 (in-gap excitations)

$$\left(\frac{1}{T_1}\right)_\infty \sim \frac{A_{hf}^2}{J} \sim 3,300 \text{ sec}^{-1}$$

Parameter-free theoretical estimation in the high temperature limit ($T \gg J$) based on Moriya's Gaussian approximation applied to kagome Heisenberg model ($J = 180$ K)



N.Sherman, T.I., R.R.P. Singh
 PRB 94 (2016) 140415(R).

A comparable gap Δ deduced from inelastic neutron scattering

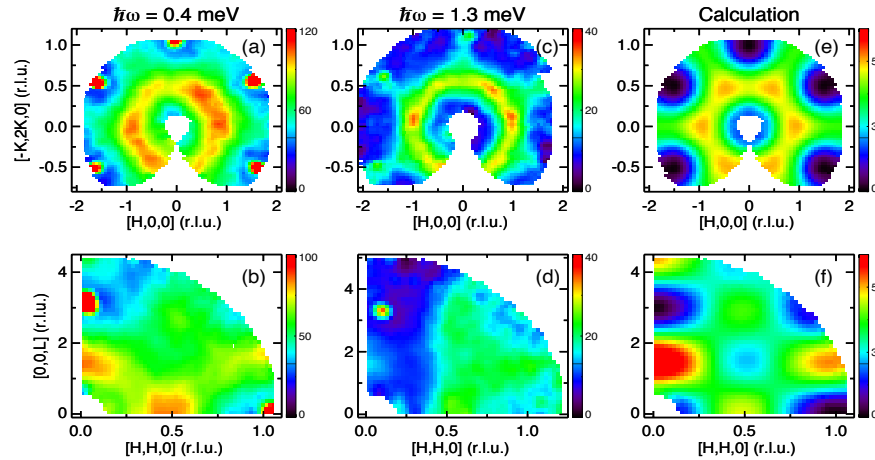
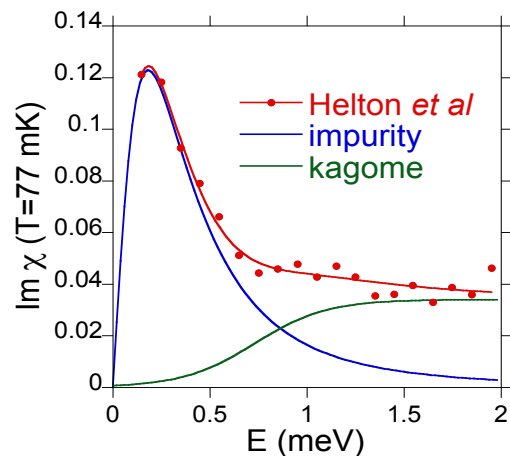


FIG. 12 (Color online) Momentum structure of the INS data at 0.4 meV and 1.3 meV for single crystal herbertsmithite at 2 K in the (HK0) scattering plane (top row) and (HHL) scattering plane (bottom row) (Han *et al.*, 2015). The plots in the right column are the calculated structure factor for near neighbor AF correlations between copper defects on the zinc sites, taking into account the copper form factor. These correspond to correlations between the brown and the gray sites of Fig. 1, which sit in successive triangular planes.

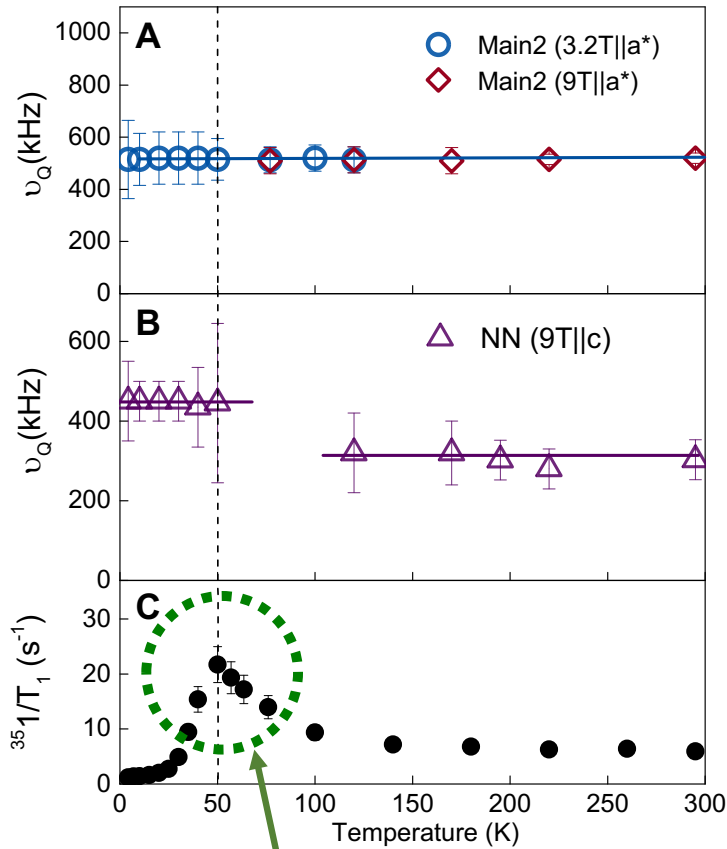


Magnitude of gap comparable to NMR results

T.-H. Han, M. Norman, Y.S. Lee *et al.*
PRB (2016). Arxiv:1604.03048

Additional complications caused by defects

Supplementary Materials, Science (2015) Fu, T.I. et al



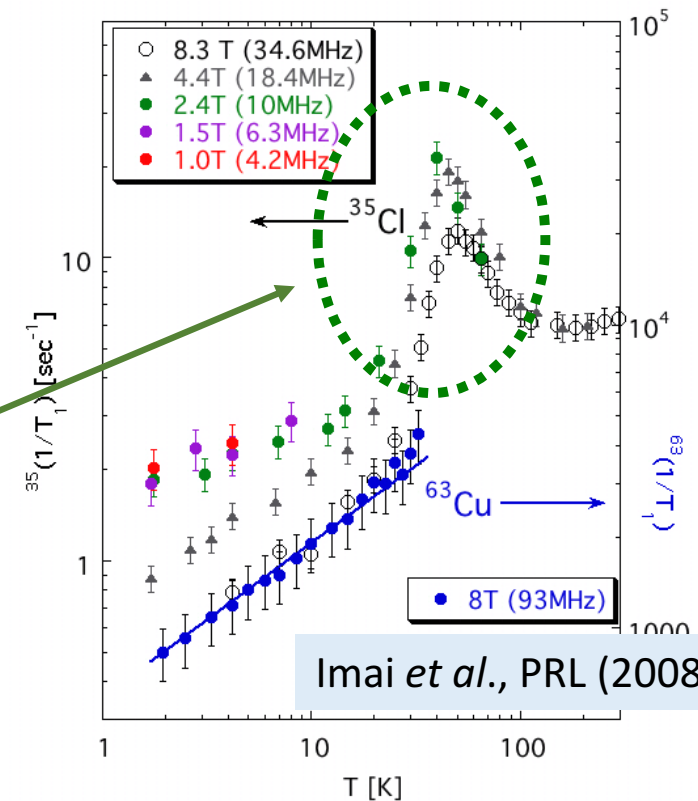
ν_Q stays constant for the Main ^{17}O sites

Average structure of the kagome plain remains unchanged

ν_Q changes for the NN ^{17}O sites

Local structure deforms near the defects.

Bump of $1/T_1$ at ^{35}Cl sites; depends on frequency.
Something is slowly freezing below 50K.



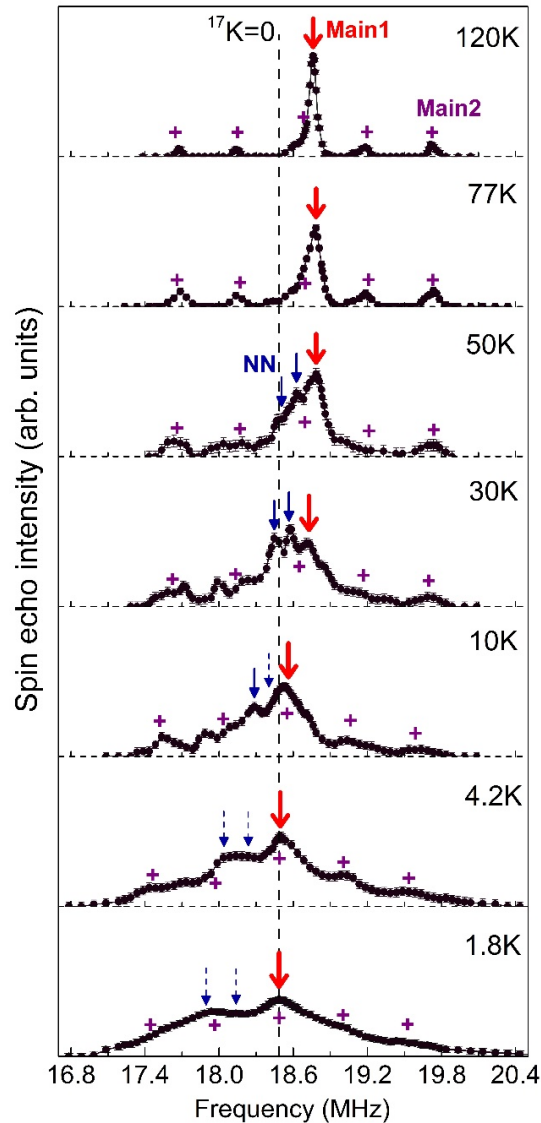
Imai et al., PRL (2008)

Key Conclusions

- Cu^{2+} defect spins occupy the Zn sites with $\sim 15\%$ probability; $(\text{Zn}_{0.85}\text{Cu}_{0.15})\text{Cu}_3(\text{OH})_6\text{Cl}_2$.
- Defect spins exhibits Curie-Weiss behavior: $\chi_{\text{defect}} \sim C/(T + \theta)$ with $\theta \sim +1$ K.
- No evidence for Zn anti-site defects at the kagome Cu sites in anomalous X-ray, powder Rietveld refinement, ^2D single-crystal NMR, nor ^{17}O single crystal NMR.
- kagome spin susceptibility $\chi_{\text{kagome}} \rightarrow 0$ at $T = 0$ with a small, field-dependent gap; $\Delta \sim 0.05\text{J}$.
- Lattice deformation freezes in the immediate vicinity of defects below ~ 50 K;
(Open question) effects on the overall magnetism of the kagome planes?

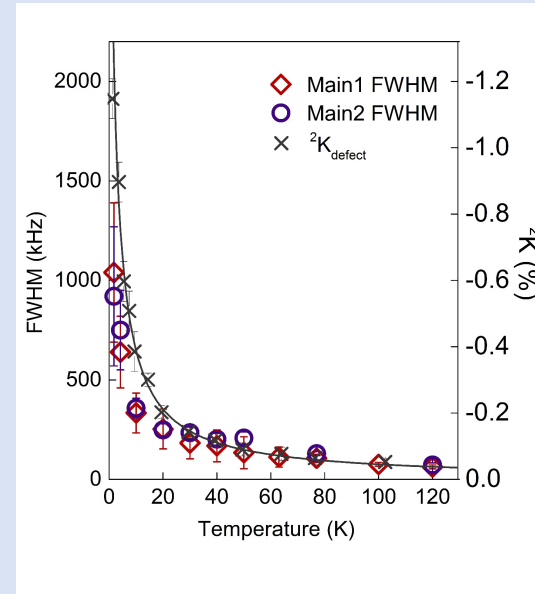
Thank you for your attention!

Intrinsic susceptibility χ_{kagome} of the kagome plane as determined from the ^{17}O Knight shift at the main sites measured with $B = 3.2 \text{ T} \parallel a^*$



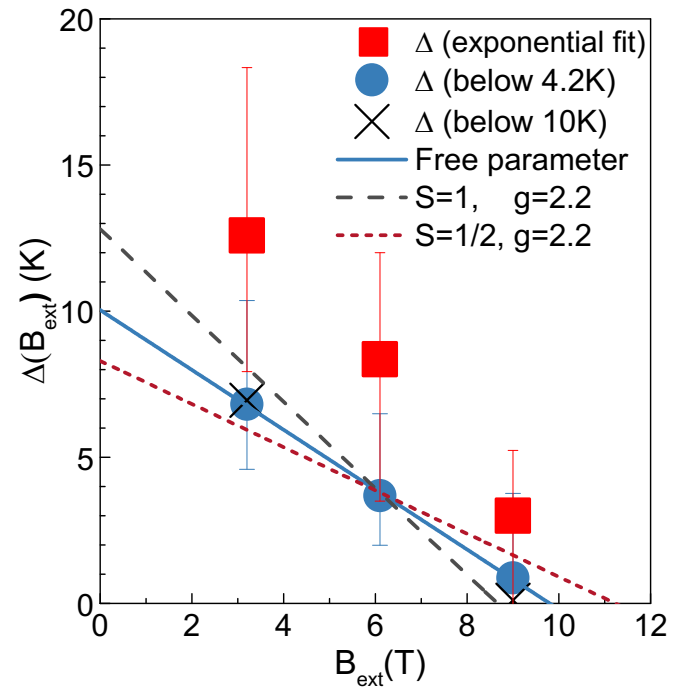
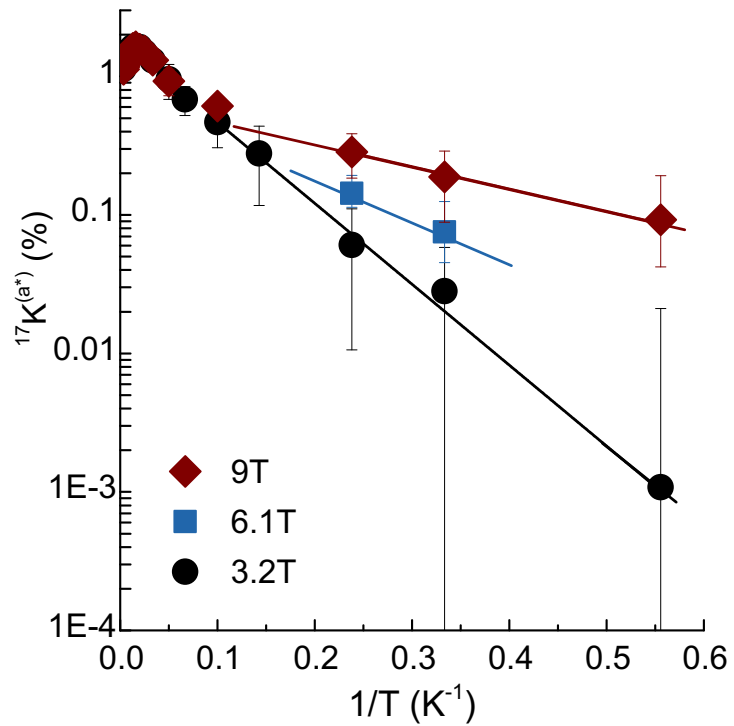
Larger frequency shift
 Larger ^{17}K
 Larger χ_{kagome}

- All NMR lines broaden in proportion to χ_{defect} .



- But we can trace the Main1 peak down to 1.8 K ($\sim 0.01\text{J}$), because it is singularly larger than all other peaks.
- Main1 peak frequency reaches a maximum at $\sim 60\text{K}$, then **shifts back to the zero Knight shift position at low temperatures.**
- We cannot resolve the central peak of Main2, but its uppermost satellite peak displays qualitatively the same trend.

Magnetic field dependence of the gap --- alternate fits with a simple exponential function



Semi-quantitatively the same results for Δ