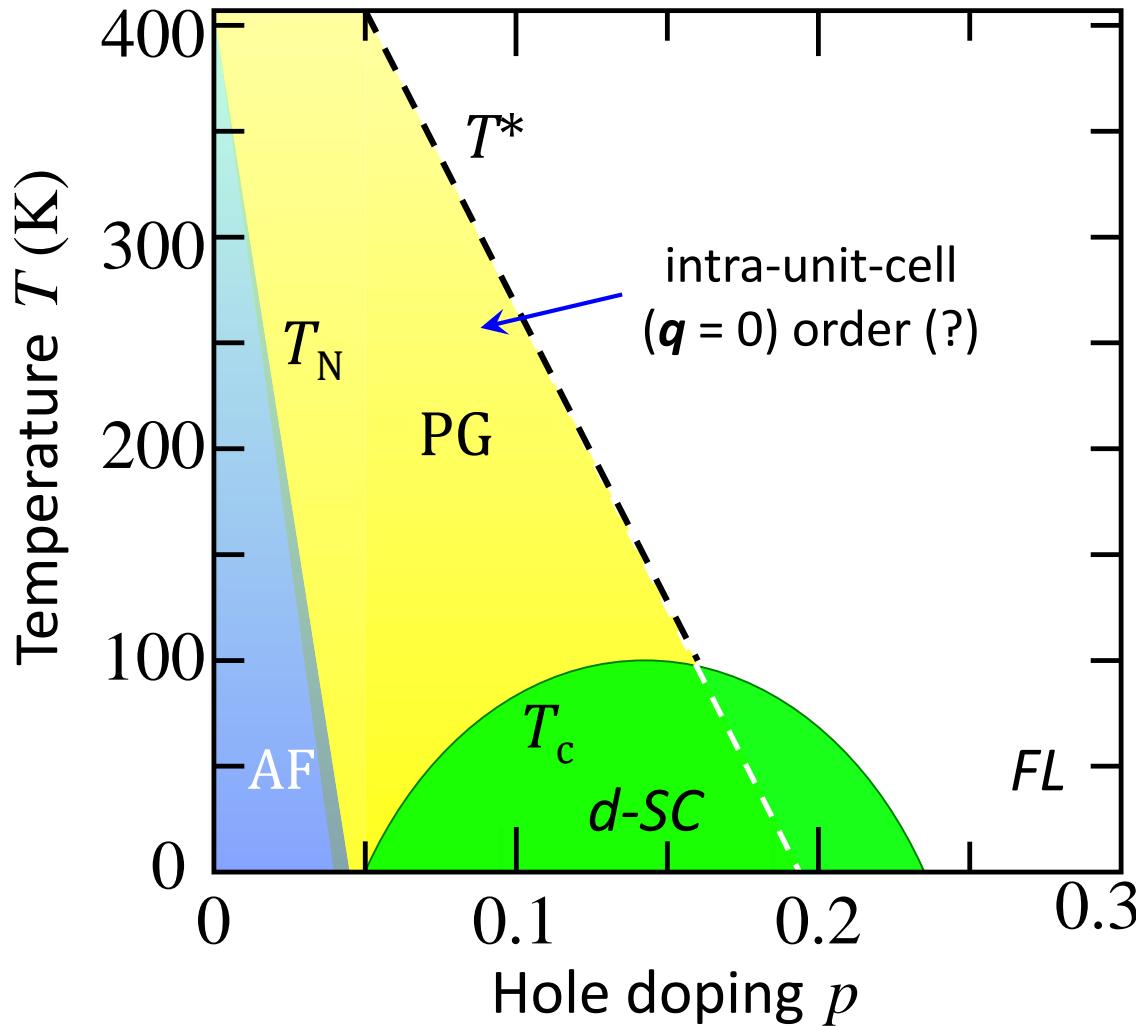
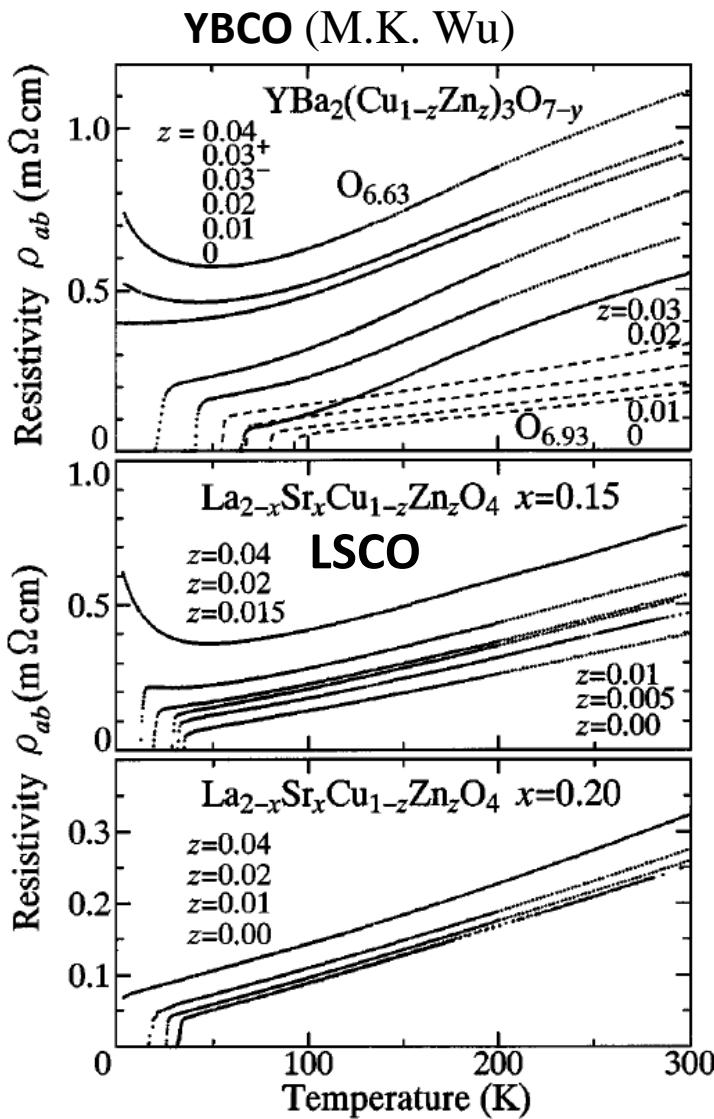


# Hole Pairs (PDW) in the PG State ?



S. Uchida  
Univ. of Tokyo  
AIST (Tsukuba)  
IOP-CAS (Beijing)

# 1. Residual resistivity produced by unitary scatterers: Zn in cuprates

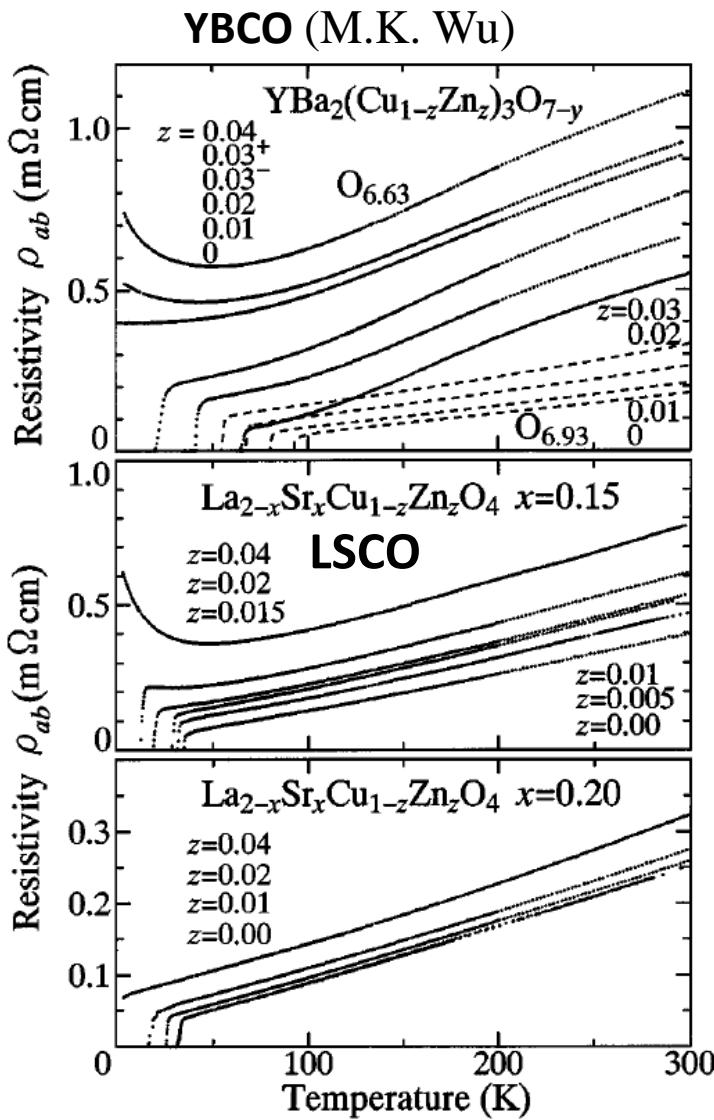


$$\rho_0^{2D} = 4(\hbar/e^2) (n_i/n) \sin^2 \delta_0$$

the unitarity limit ( $\delta_0 = \pi/2$ )

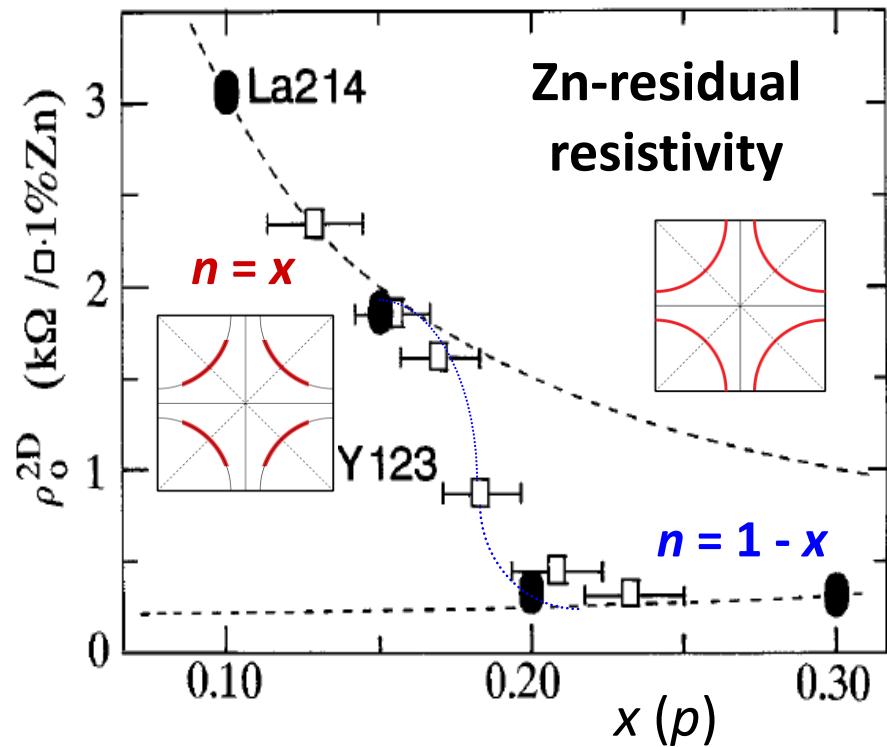
Y. Fukuzumi, SU *et al.*, PRL **76**, 5654 (1996).

# 1. Residual resistivity produced by unitary scatterers: Zn in cuprates



$$\rho_0^{2D} = 4(\hbar/e^2) (n_i/n) \sin^2 \delta_0$$

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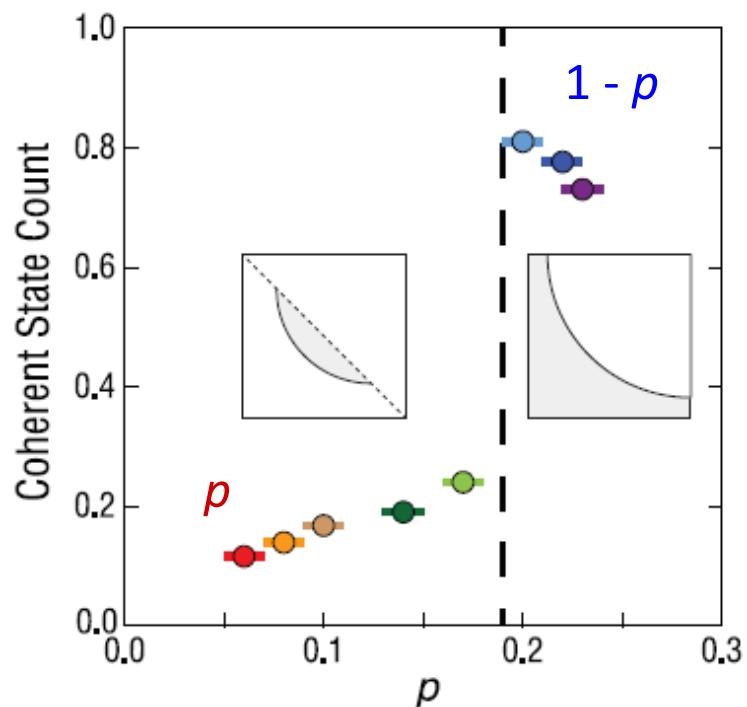
Y. Fukuzumi, SU *et al.*, PRL **76**, 5654 (1996).

# Transformation of the Fermi arc (small Fermi surface) to a large Fermi surface at $p \sim 0.2$

SI-STM:  
“Bogoliubov arc”

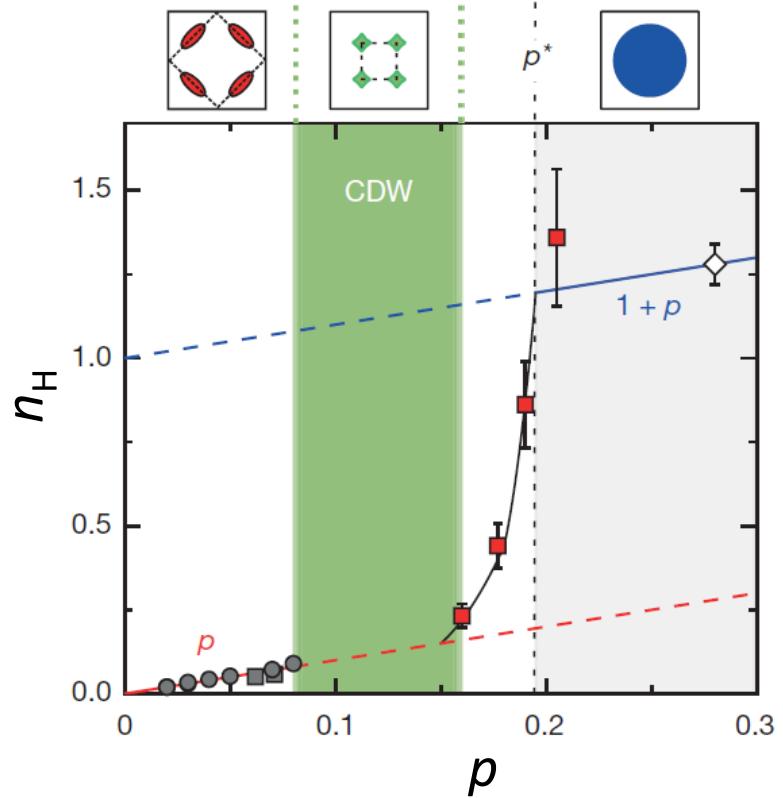
**Bi2212**

K. Fujita, J.C. Davis *et al.*,  
Science **344**, 612 (2014).



High- $B$  Hall effect

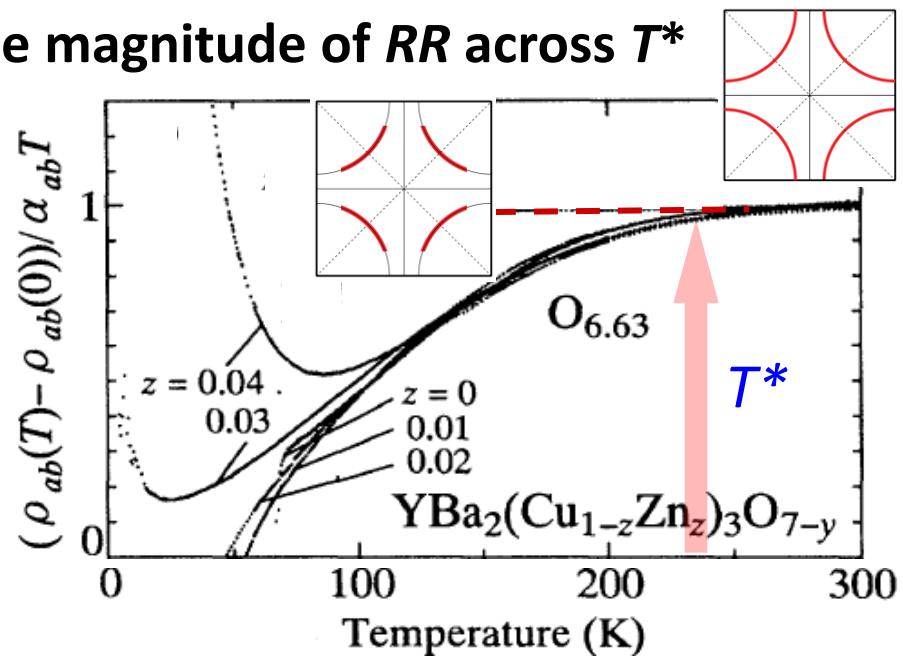
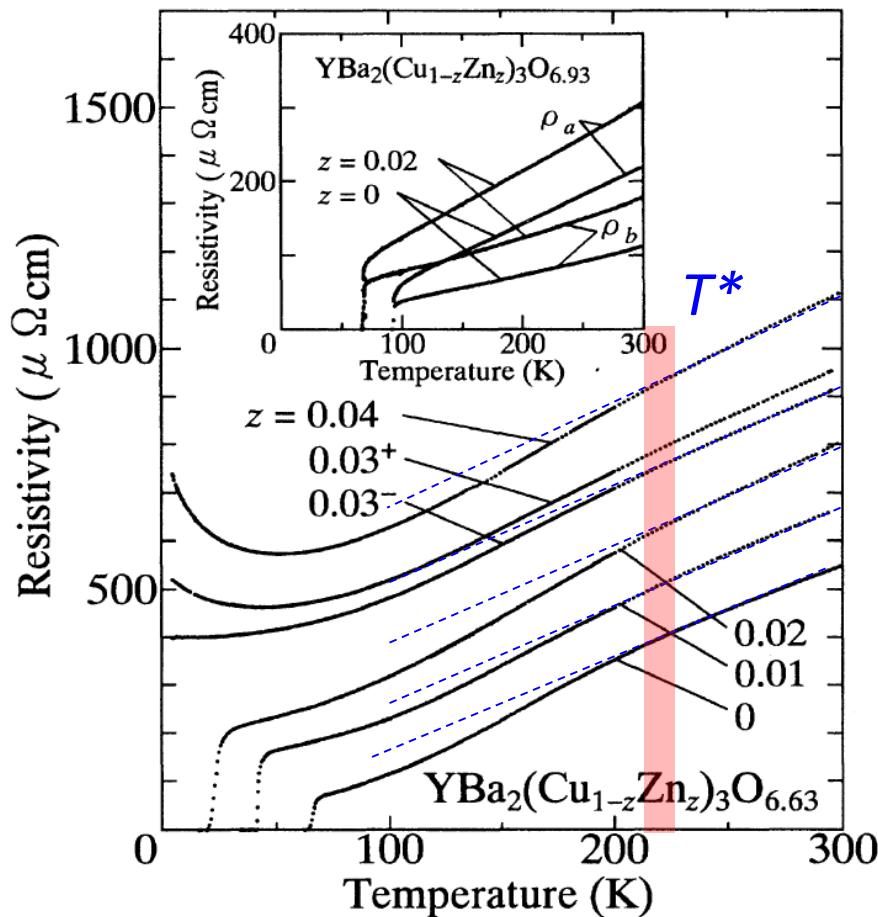
**YBCO**



S. Badoux, L. Taillefer *et al.*,  
Nature **531**, 210 (2016).

# 1. Residual resistivity produced by unitary scatterers: Zn in cuprates

No significant change in the magnitude of *RR* across  $T^*$



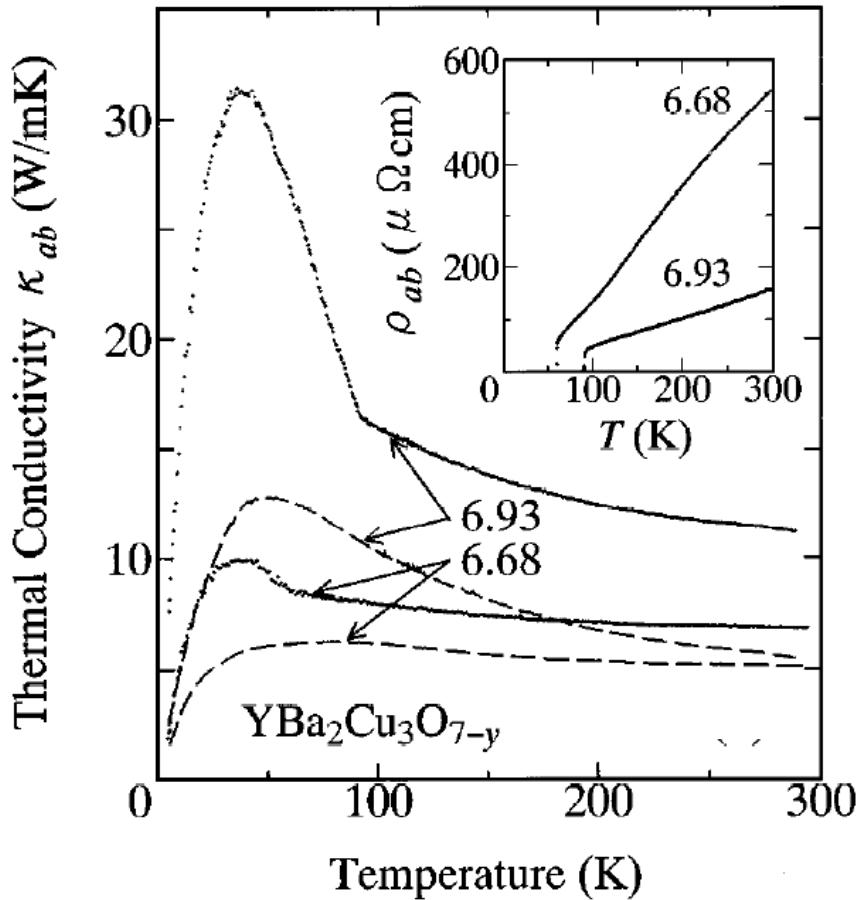
$$\rho_0^{2D} = 4(\hbar/e^2) (n_i/n) \sin^2 \delta_0$$

the unitarity limit ( $\delta_0 = \pi/2$ )

Y. Fukuzumi, K. Mizuhashi, K. Takenaka, SU, PRL **76**, 5654 (1996).

## 2. Electronic thermal conductivity: Lorenz number

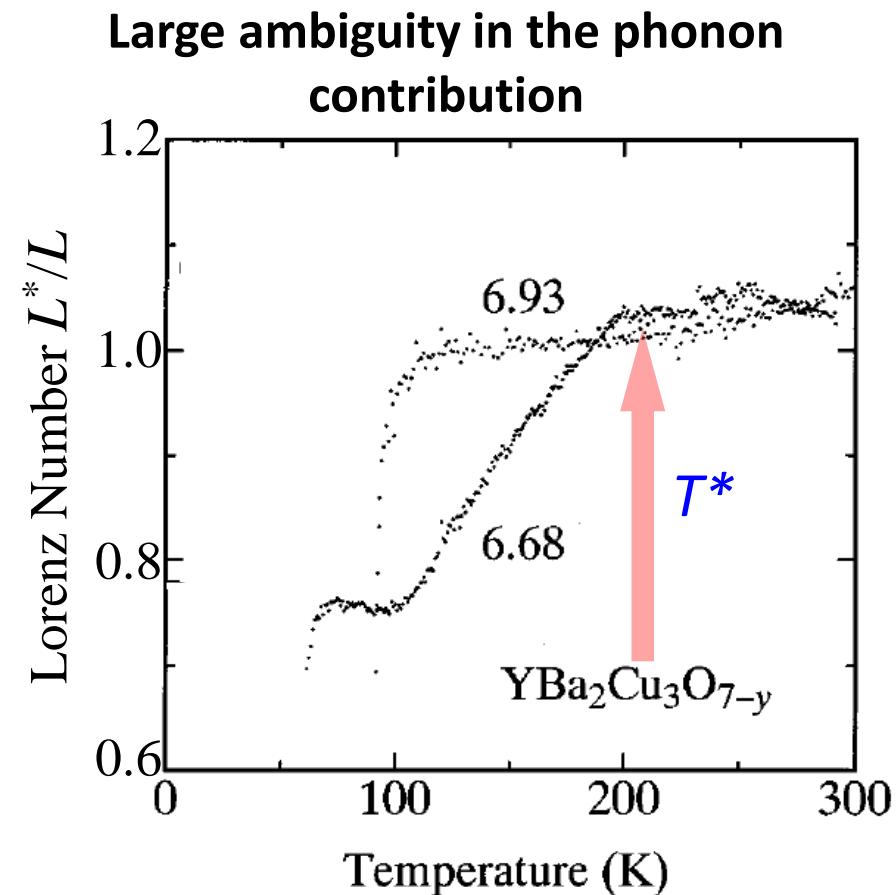
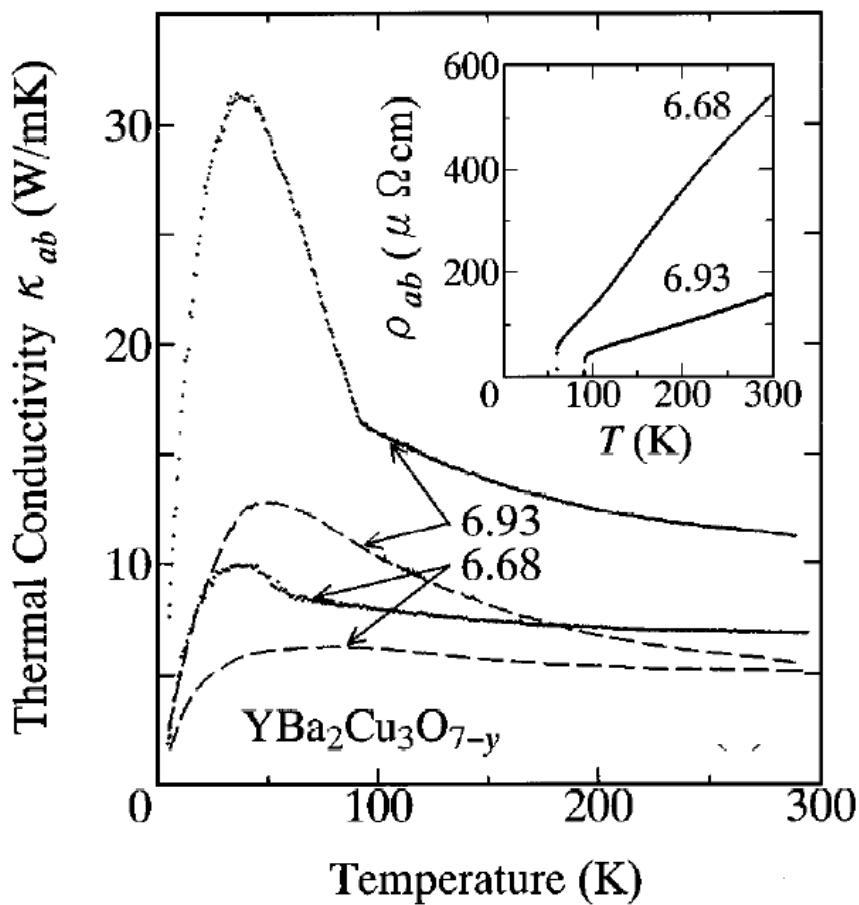
$$L = \kappa / \sigma T = (\pi^2/3) (k_B/e)^2 \rightarrow L^* = (\pi^2/3) (k_B/2e)^2 = L/4$$



K. Takenaka, SU *et al.*, PRB **56**, 5654 (1997).

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$$L = \kappa / \sigma T = (\pi^2/3) (k_B/e)^2 \rightarrow L^* = (\pi^2/3) (k_B/2e)^2 = L/4$$



# Various signatures of Pair Formation above $T_c$

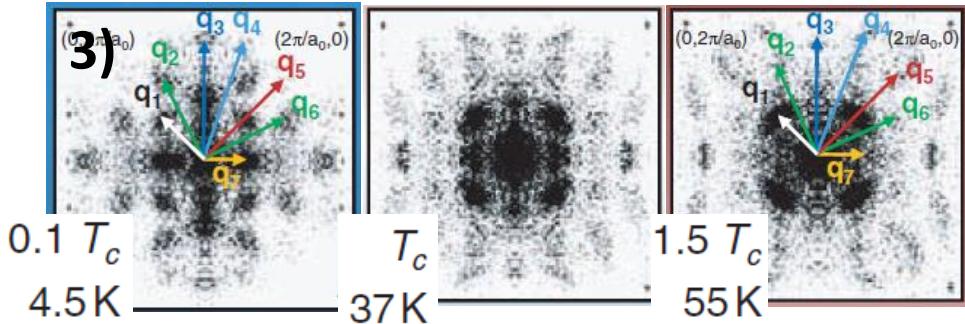
## 1) Transverse Josephson plasmon above $T_c$

A. Dubroka, C. Bernhard, PRL **106**, 047006 (2011)

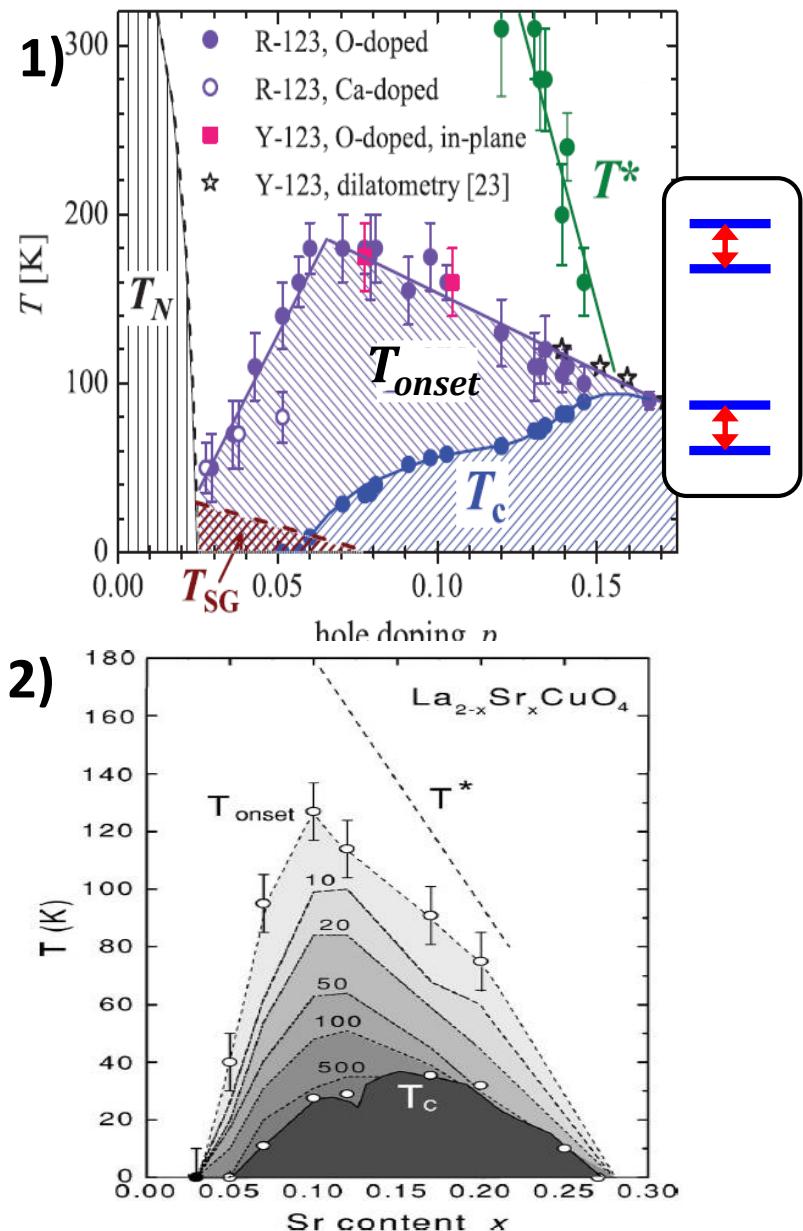
## 2) Diamagnetic signal above $T_c$ / Vortex Nernst effect

Z.A. Xu, N.P. Ong, SU, Nature **406**, 486 (2000)

## 3) Bogoliubov QP interference above $T_c$



Jhinhwang Lee *et al.*, Science **325**, 1099 (2009)



# Various signatures of Pair Formation above $T_c$

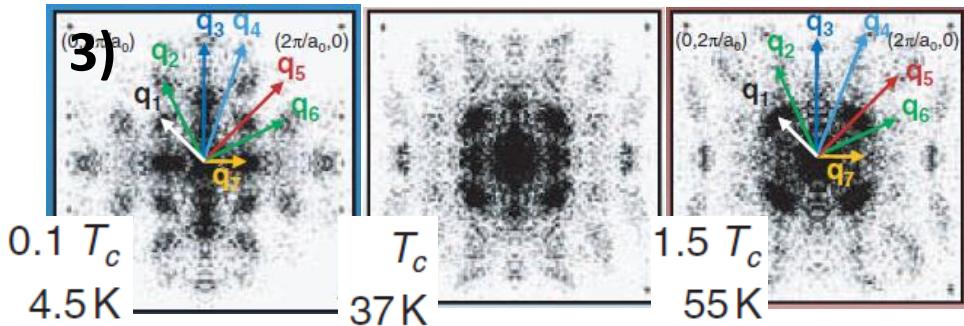
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A. Dubroka, C. Bernhard, PRL **106**, 047006 (2011).

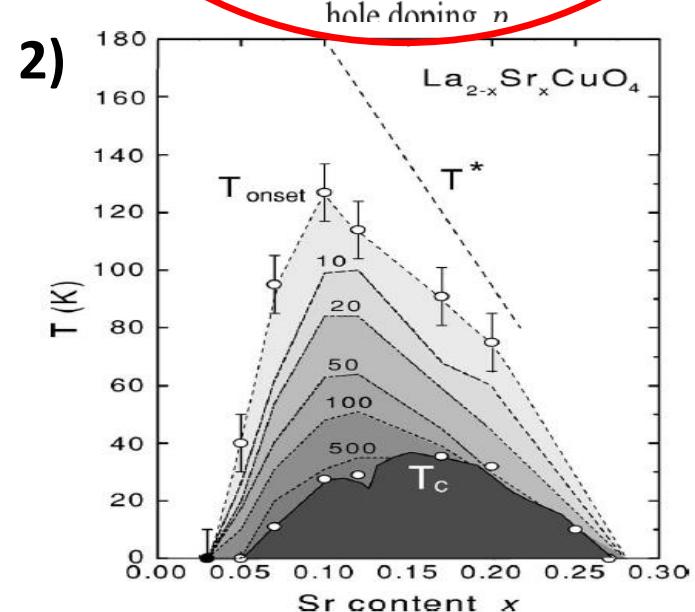
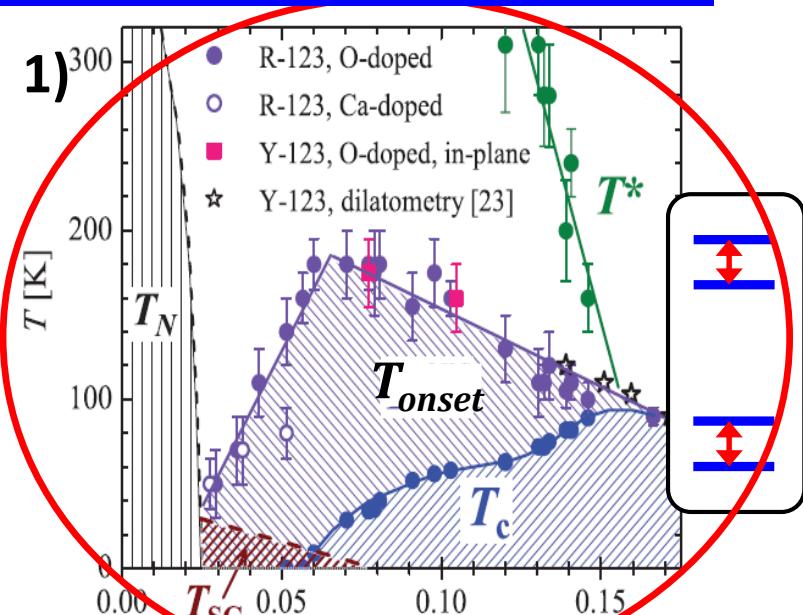
## 2) Diamagnetic signal above $T_c$ / Vortex Nernst effect

Z.A. Xu, N.P. Ong, SU, Nature **406**, 486 (2000).

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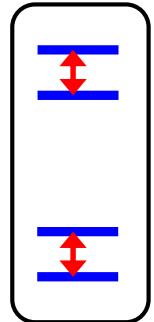


Jhinhwang Lee *et al.*, Science **325**, 1099 (2009).

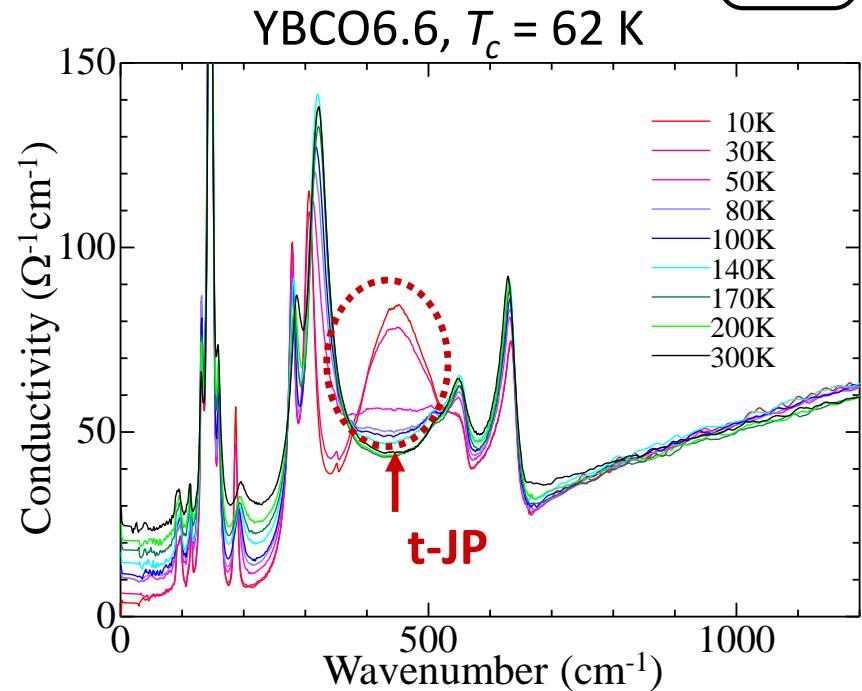
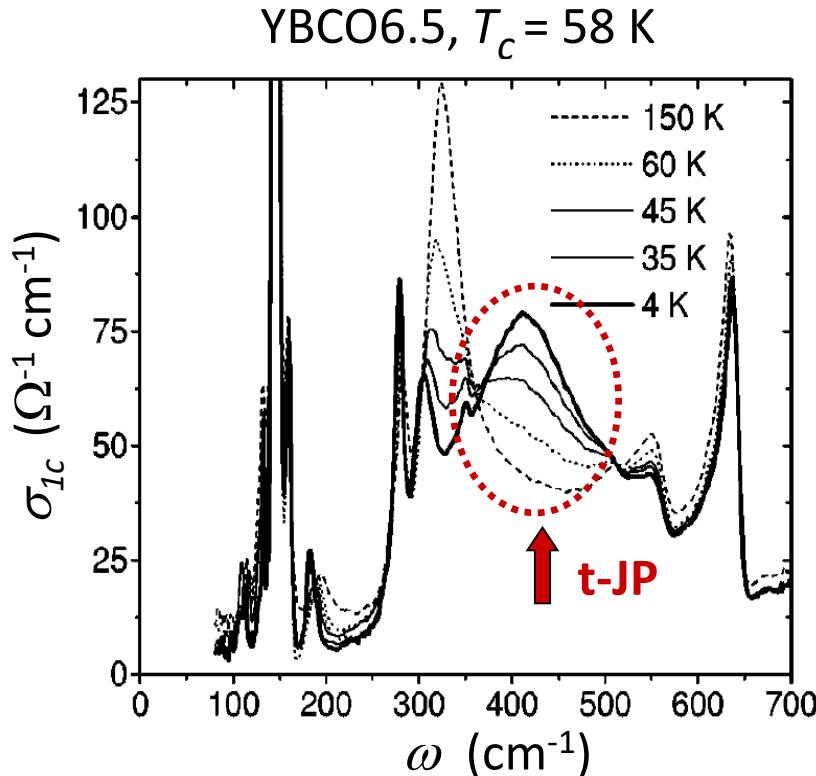


# Intra-bilayer Josephson plasma mode persists above $T_c$

Emergence of a transverse Josephson plasma (t-JP) mode  
at  $T_{onset}$ , well above  $T_c$ :



*Establishment of intra-bilayer phase coherence*

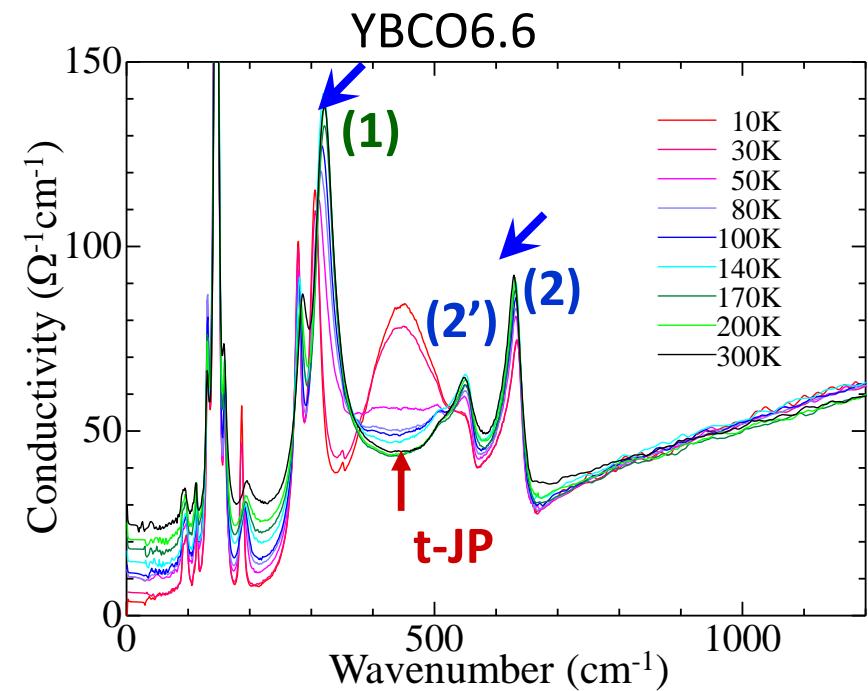
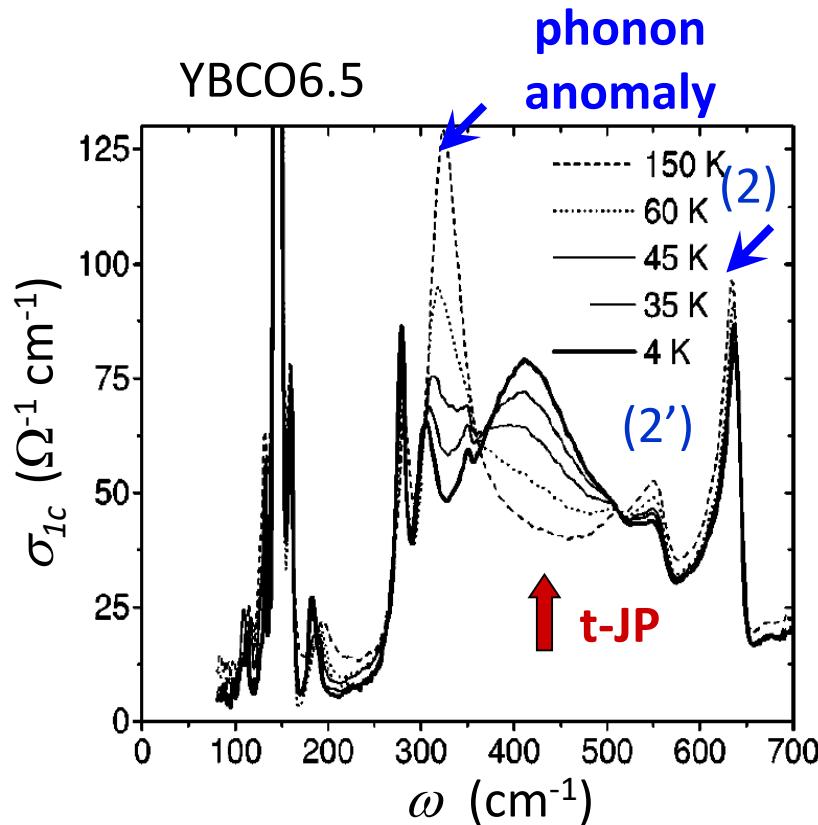


A. Dubroka, C. Bernhard *et al.*,  
PRL 106, 047006 (2011).

K.M. Kojima, M. Nakajima, S. Tajima,  
SU, *unpublished results*.

# Anomalous optical phonon modes

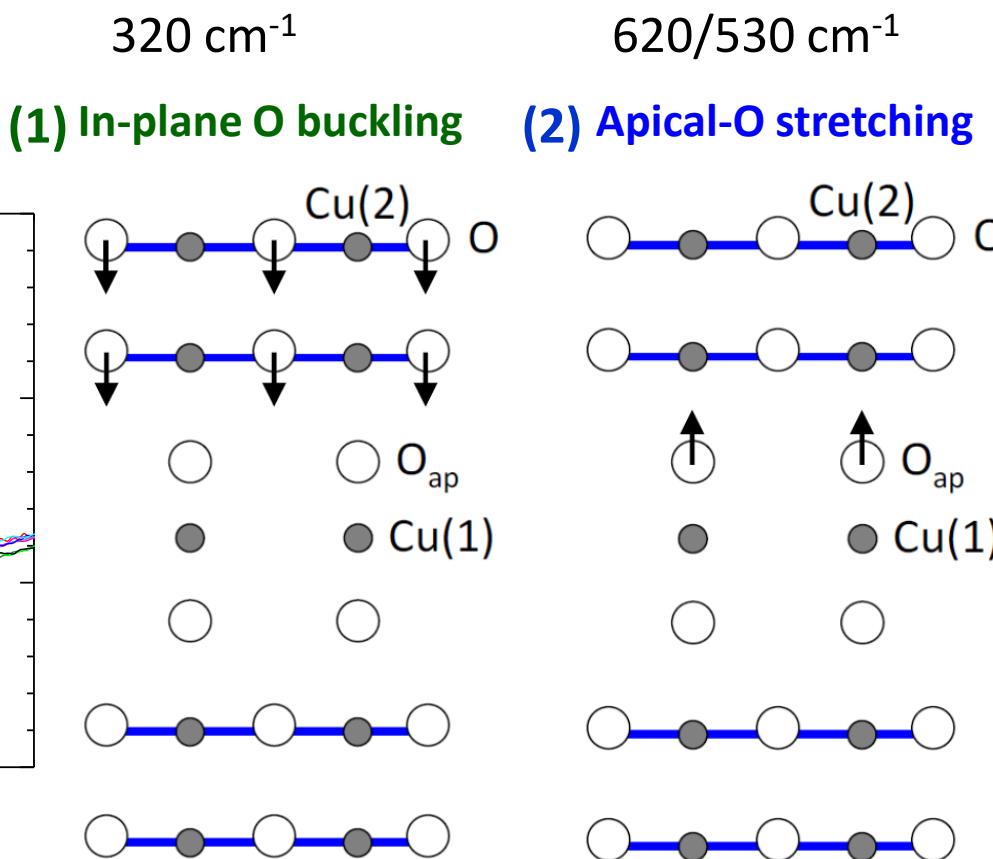
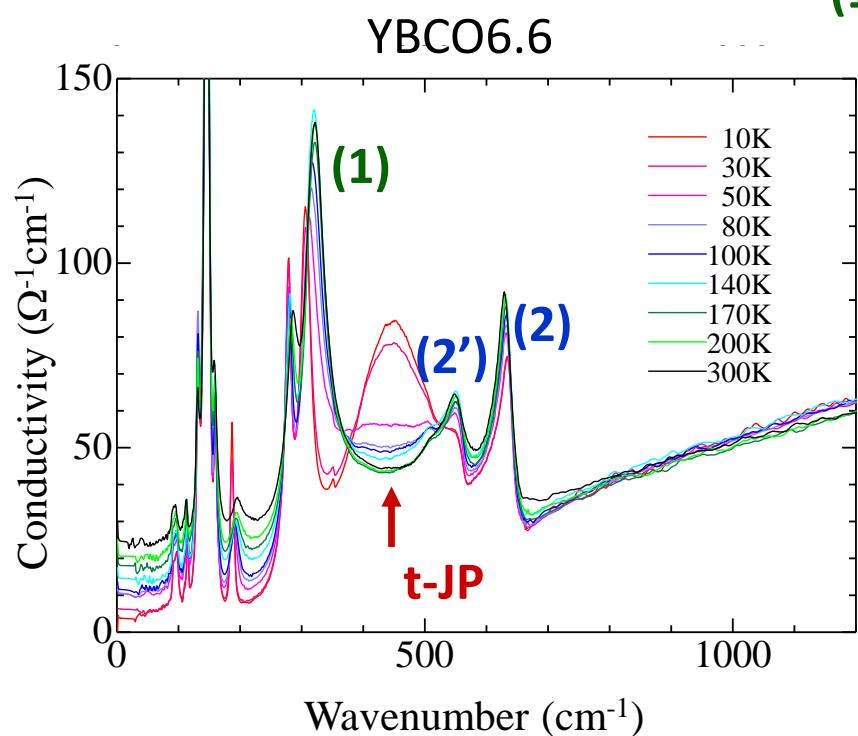
Weights of two optical phonon modes decrease with lowering  $T$ , associated with the development of t-JP



A. Dubroka, C. Bernhard *et al.*,  
PRL 106, 047006 (2011).

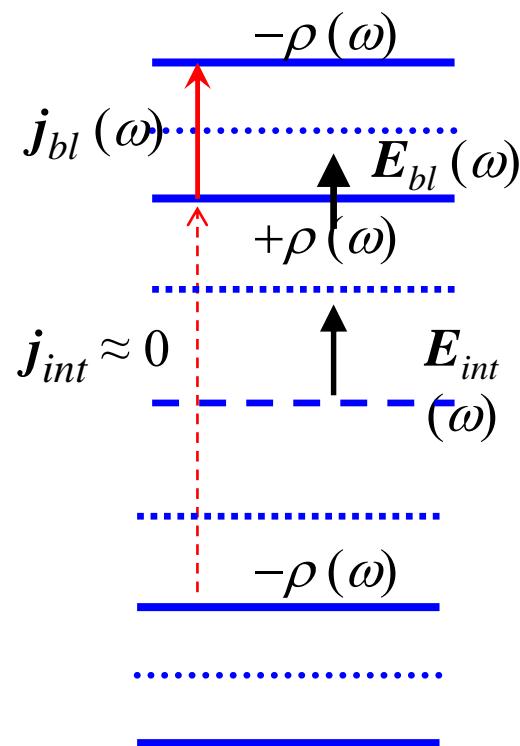
K.M. Kojima, M. Nakajima, S. Tajima,  
SU, *unpublished results*.

# Phonon anomalies associated with the development of t-JP

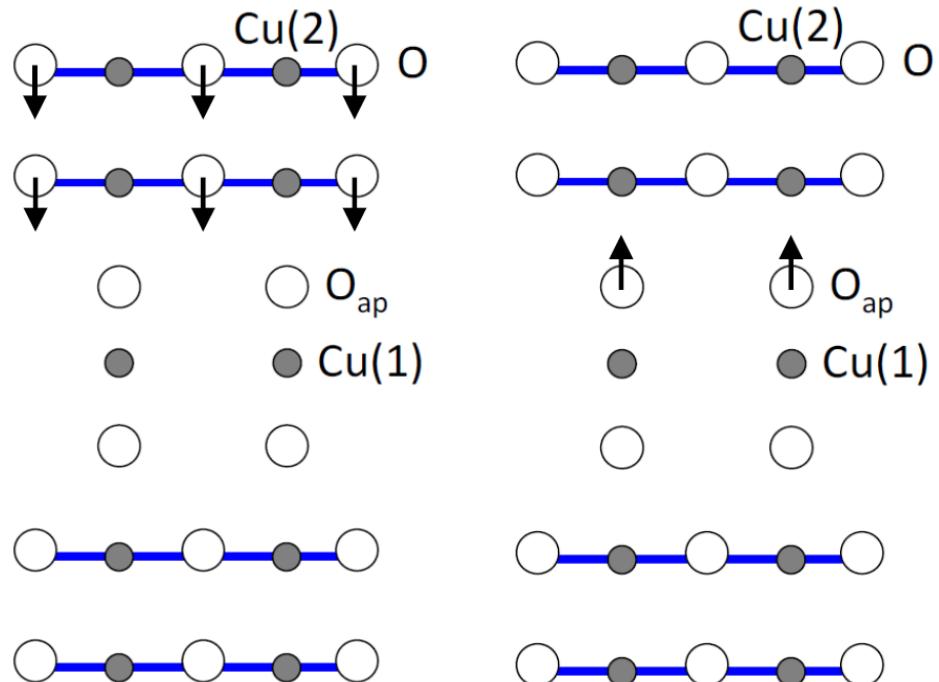


# Phonon anomalies associated with the development of t-JP

The phonon anomalies can be explained by changes of the local electric fields acting on the ions upon the onset of intra-bilayer Josephson tunneling.



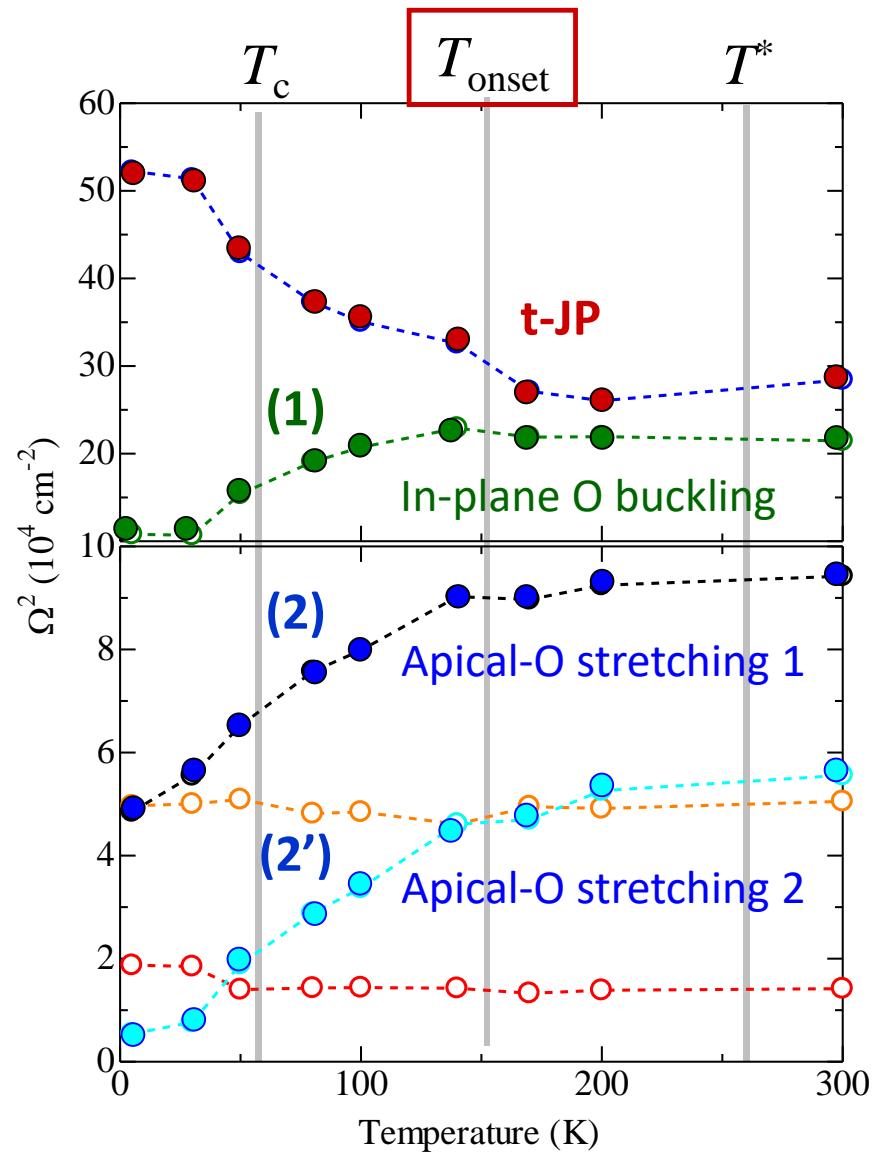
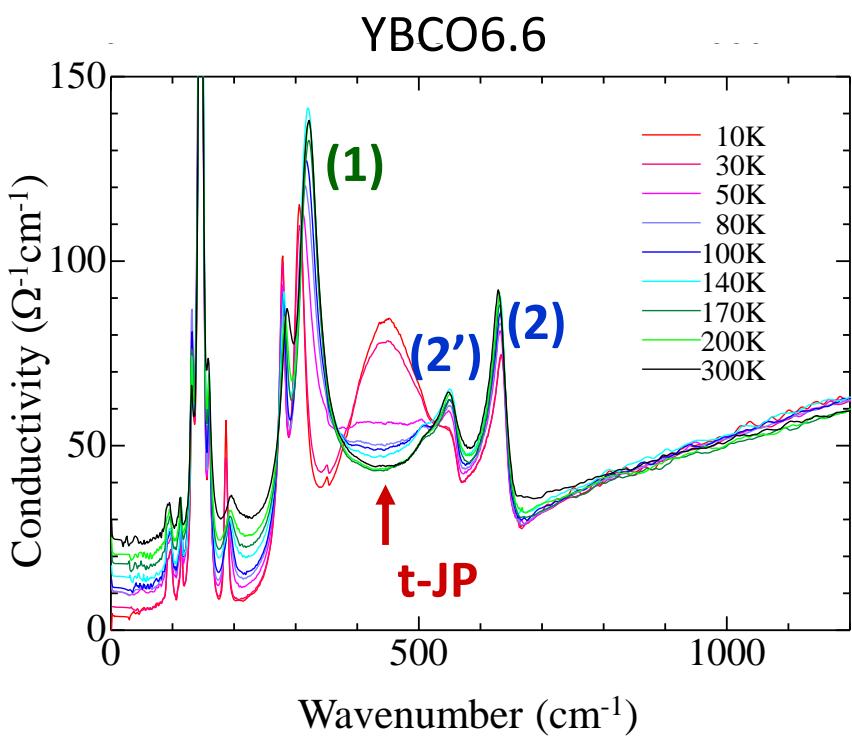
(1) In-plane O buckling    (2) Apical-O stretching



D. Munzar, C. Bernhard *et al.*, Solid State Commun. **112**, 365 (1999).

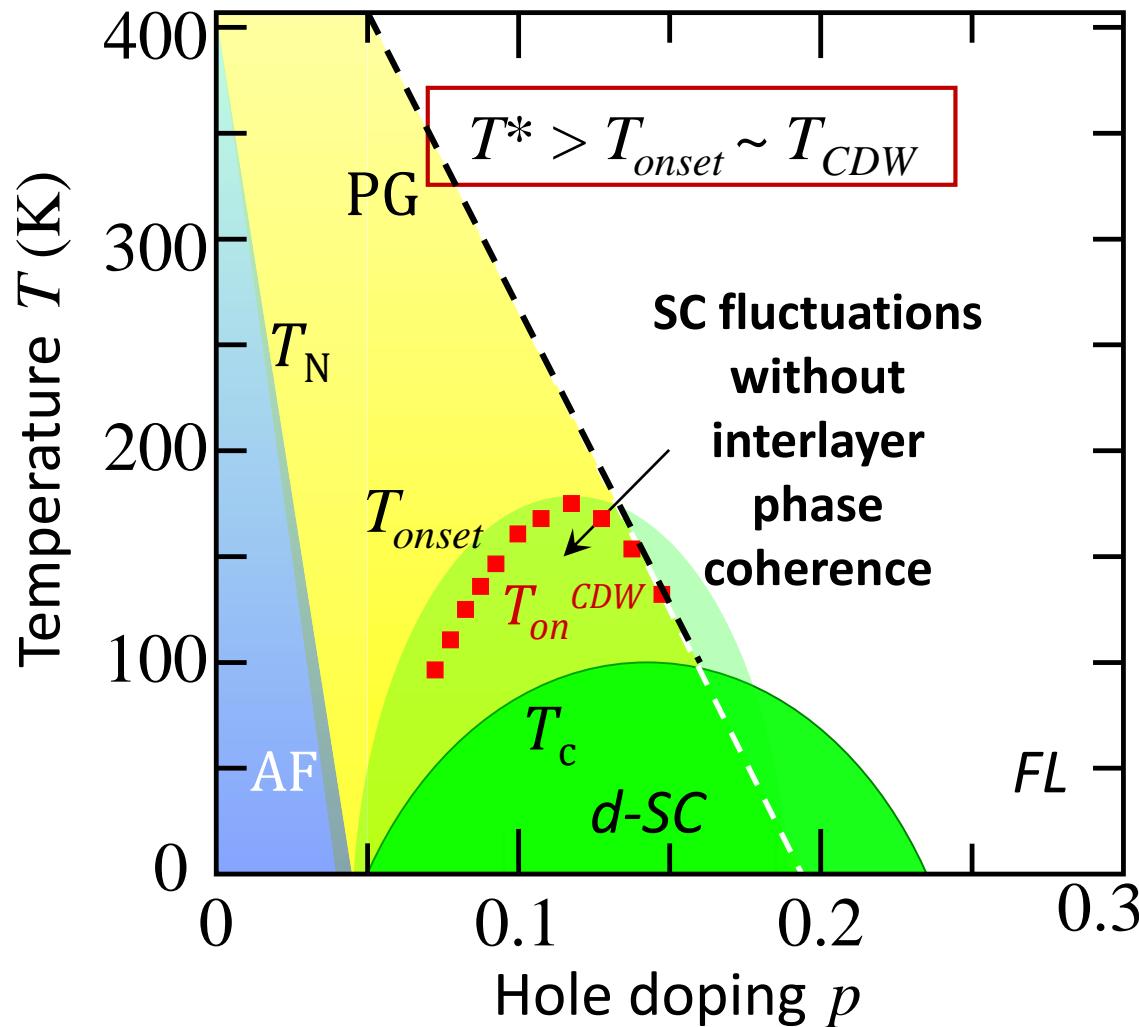
A.V. Boris, D. Munzar *et al.*, PRL **89**, 277001 (2002).

# $t$ -JP & phonon anomaly in the bilayer cuprate

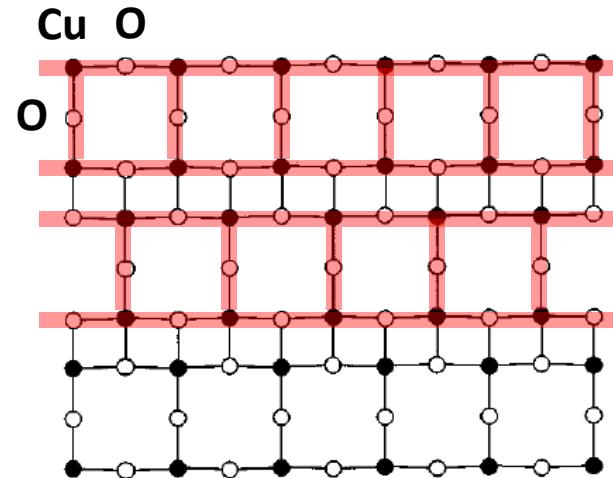
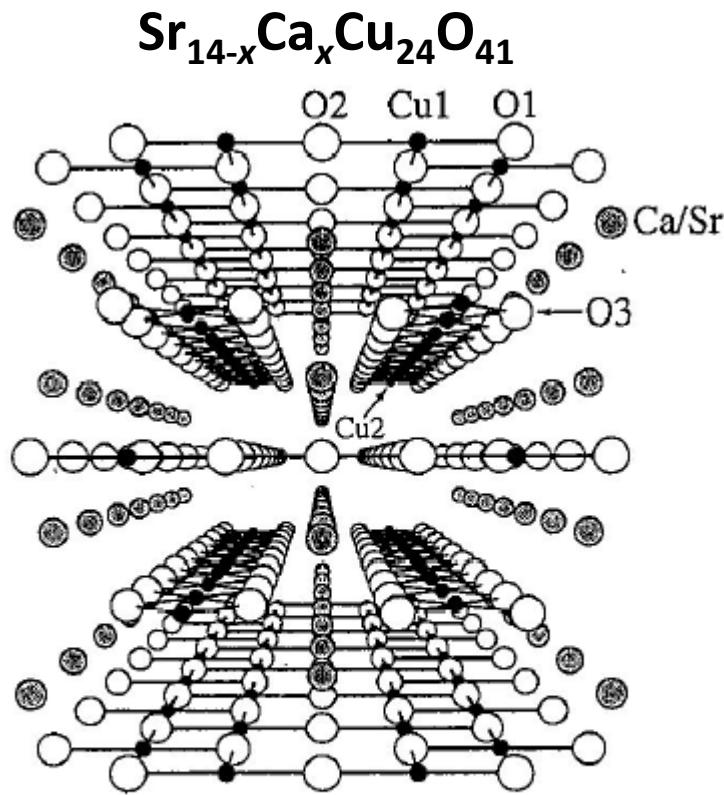


K.M. Kojima, M. Nakajima, S. Tajima,  
SU, *unpublished results.*

$T_{onset} \sim T_{CDW} < T^*$  in underdoped cuprates



# Pair formation and charge order (CDW) in hole-doped two-leg ladder cuprate



# Pseudogap (spin gap)

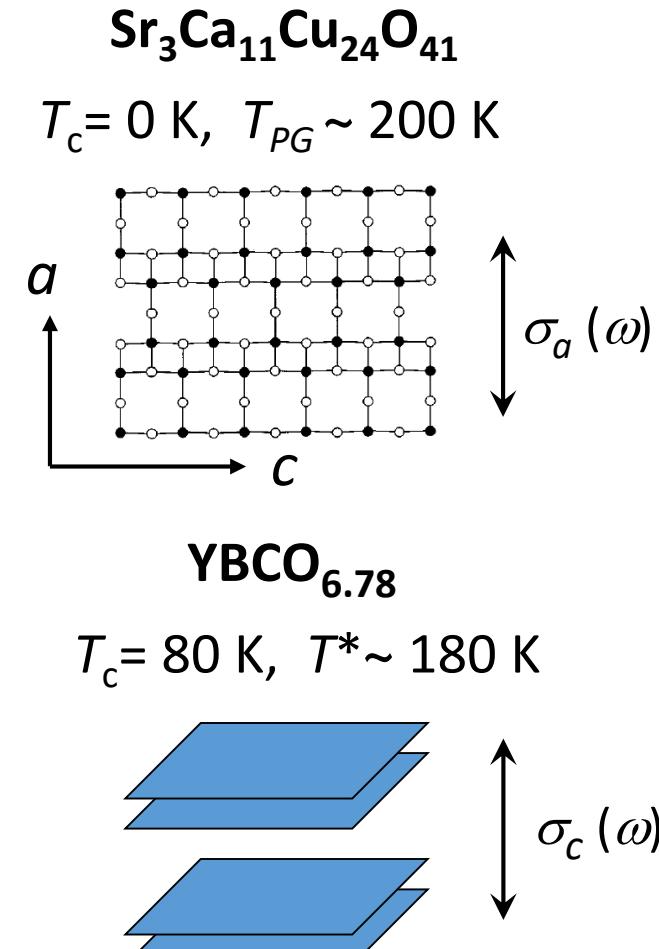
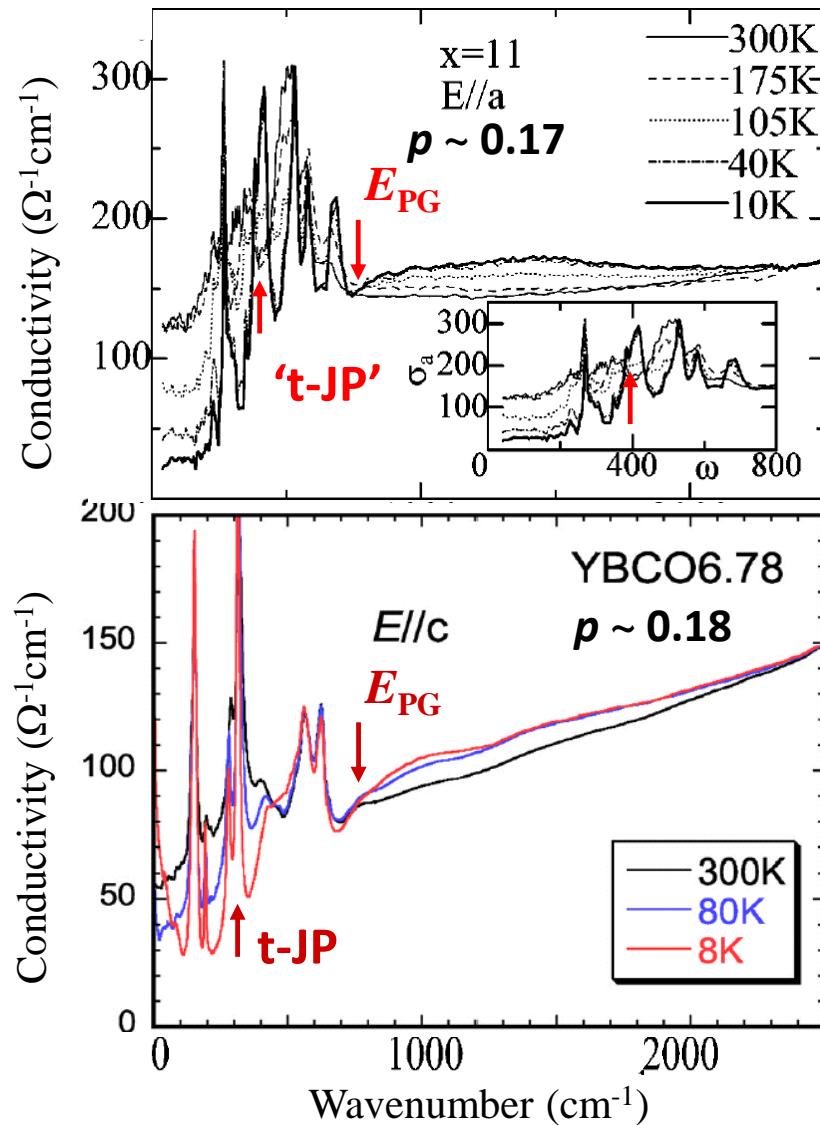
# Hole pairs

# Charge order (PDW)

# Phonon anomaly

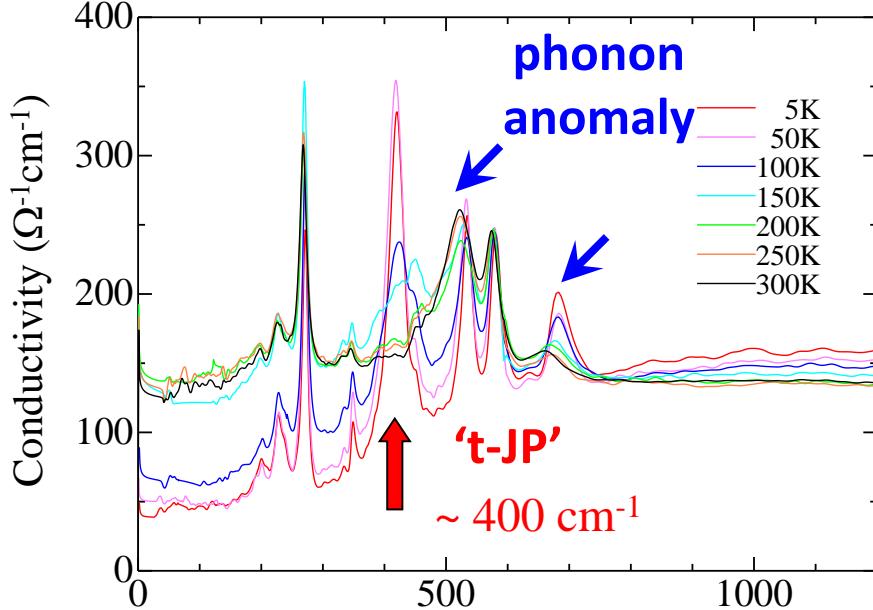
# Superconductivity @ P

# Similarity of the optical spectrum between bilayer cuprate and two-leg ladder cuprate

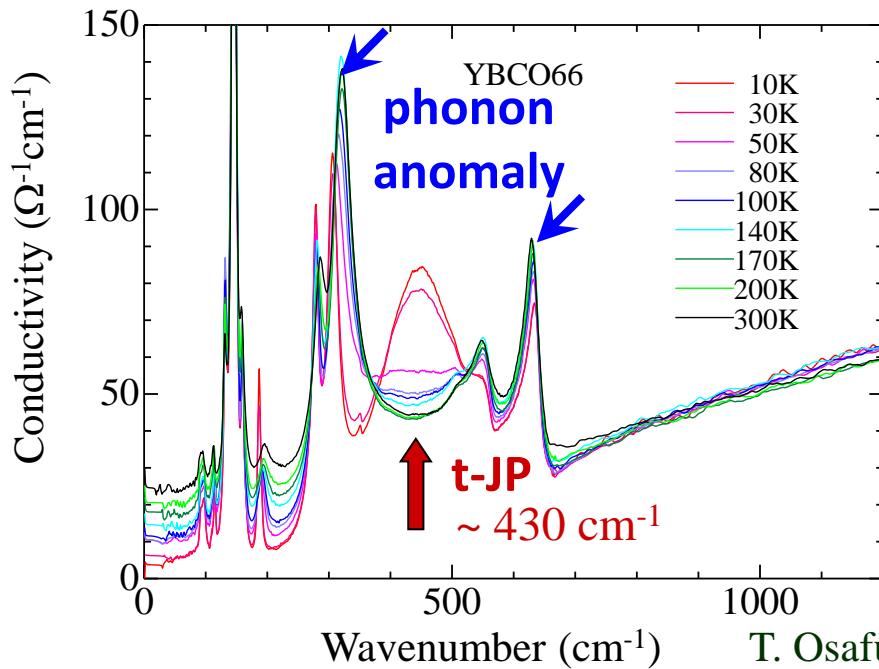
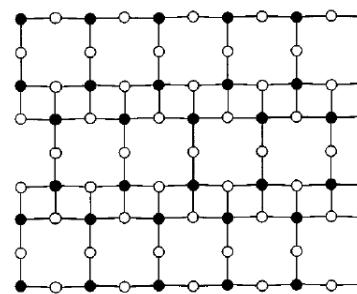


K.M. Kojima, M. Nakajima, S. Tajima,  
SU, *unpublished results*.

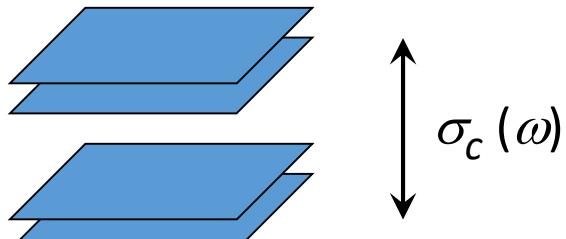
# Transverse Josephson plasma & phonon anomaly



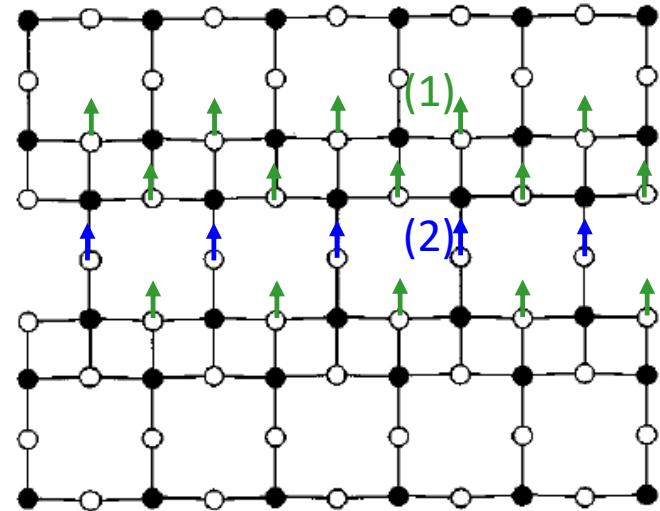
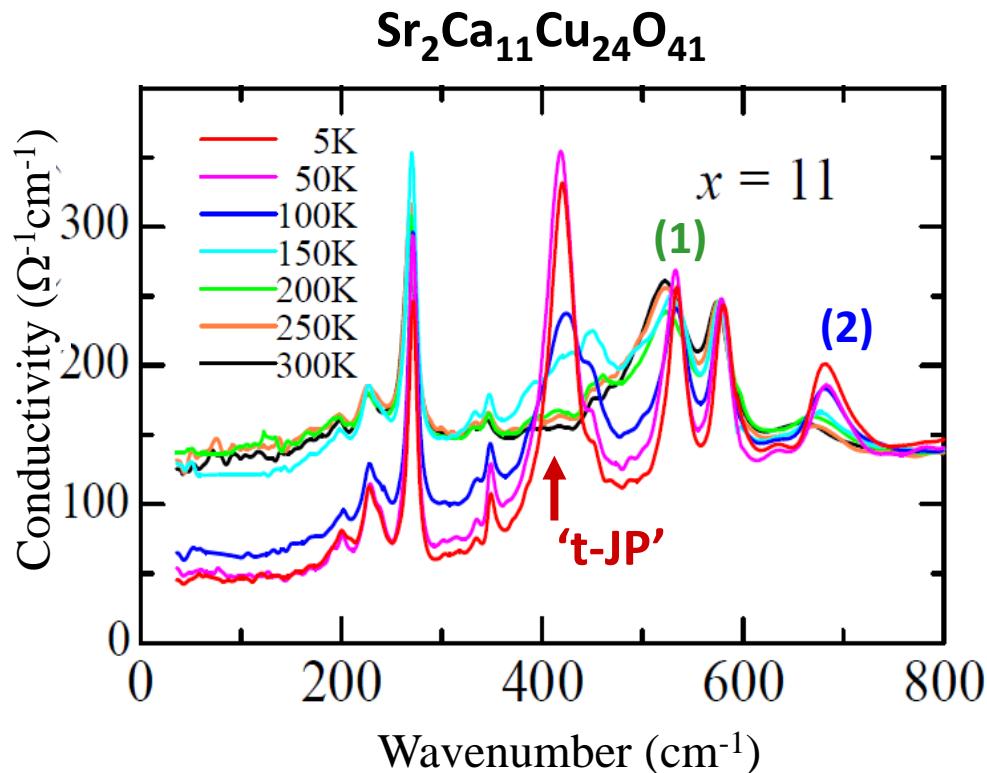
2-leg ladder cuprate:



Underdoped cuprate:



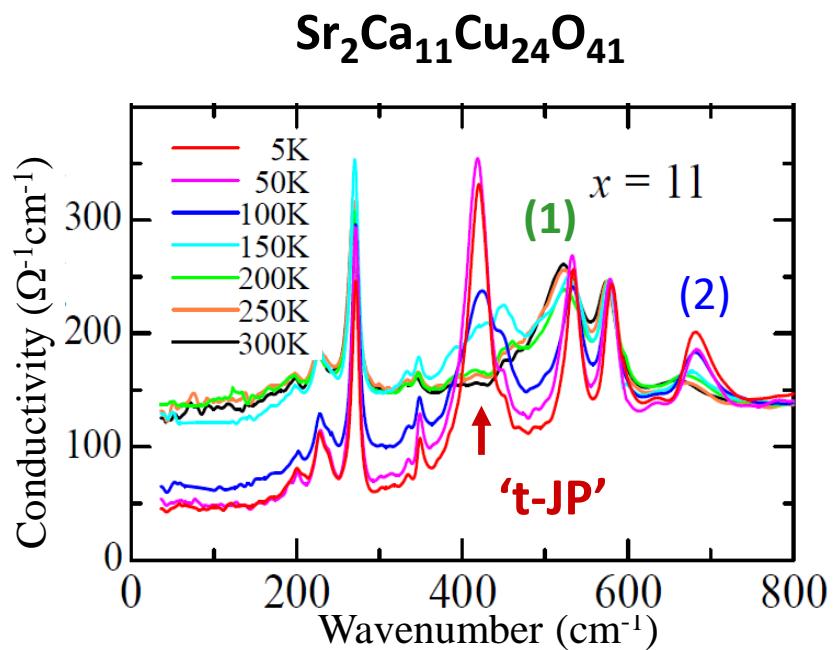
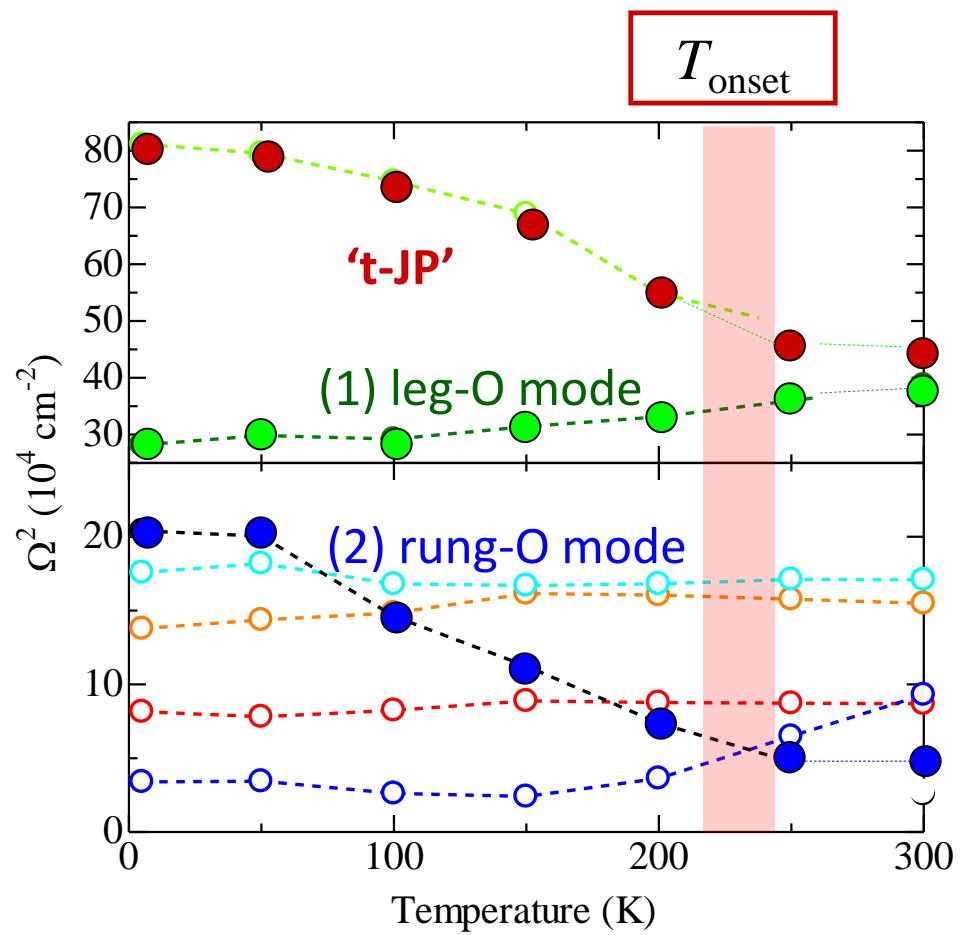
# Phonon modes showing an anomaly in the ladder cuprate



520  $\text{cm}^{-1}$       (1): leg-O phonon (chain-O buckling)

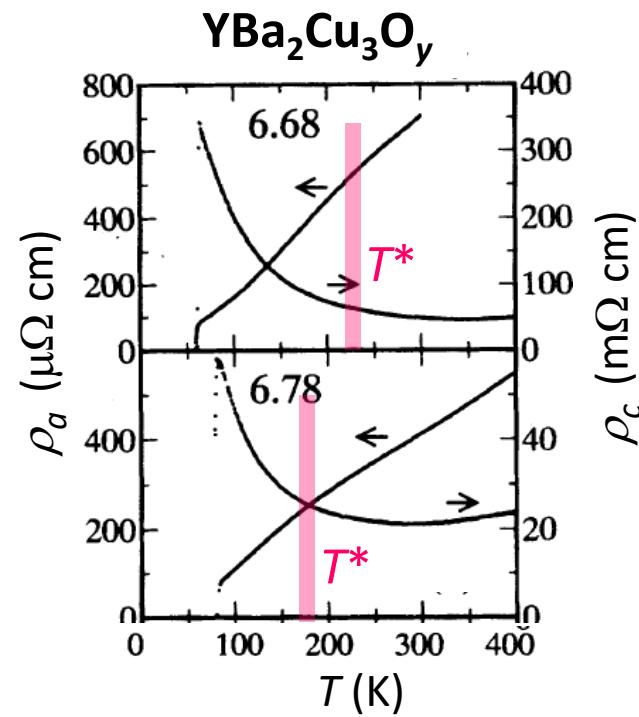
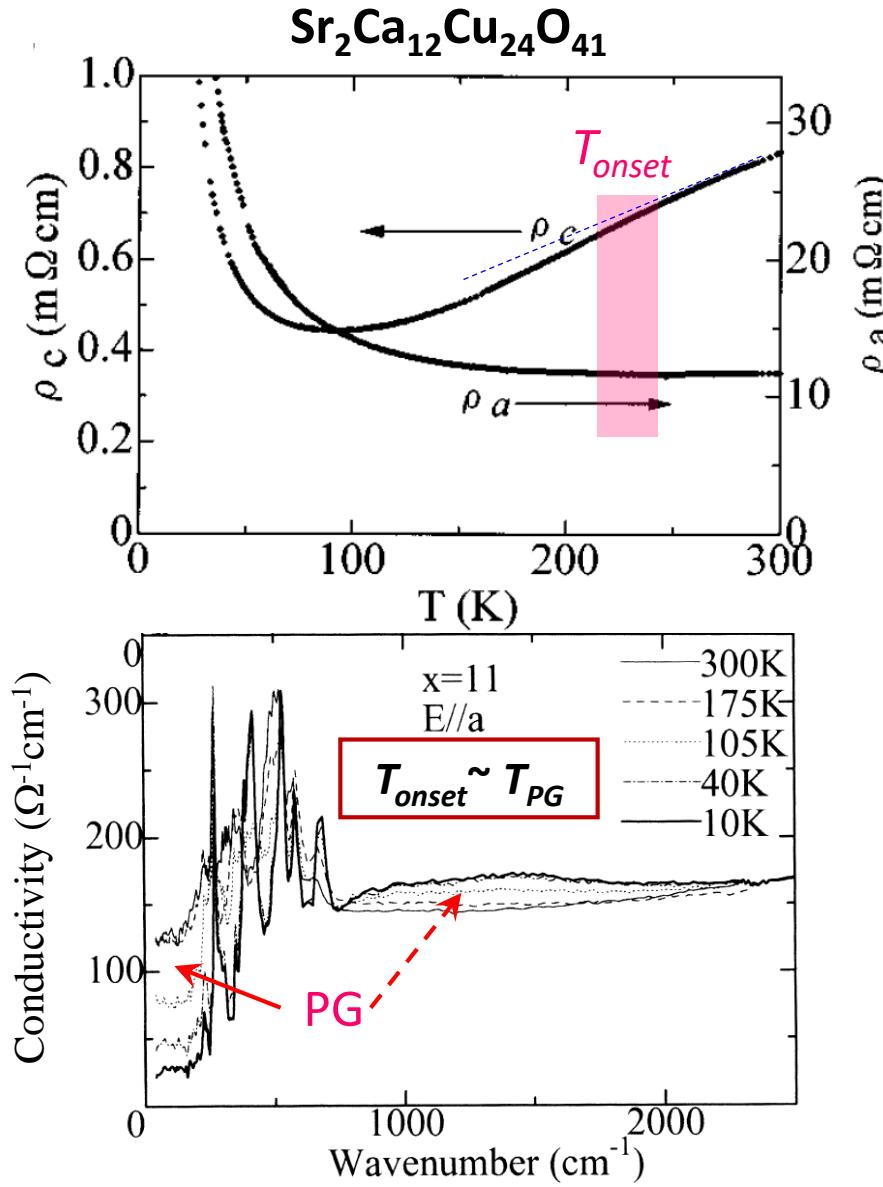
630  $\text{cm}^{-1}$       (2): rung-O phonon ('apical'- O)

# Onset of t-JP & phonon anomaly



K.M. Kojima, M. Nakajima, S. Tajima,  
SU, *unpublished results.*

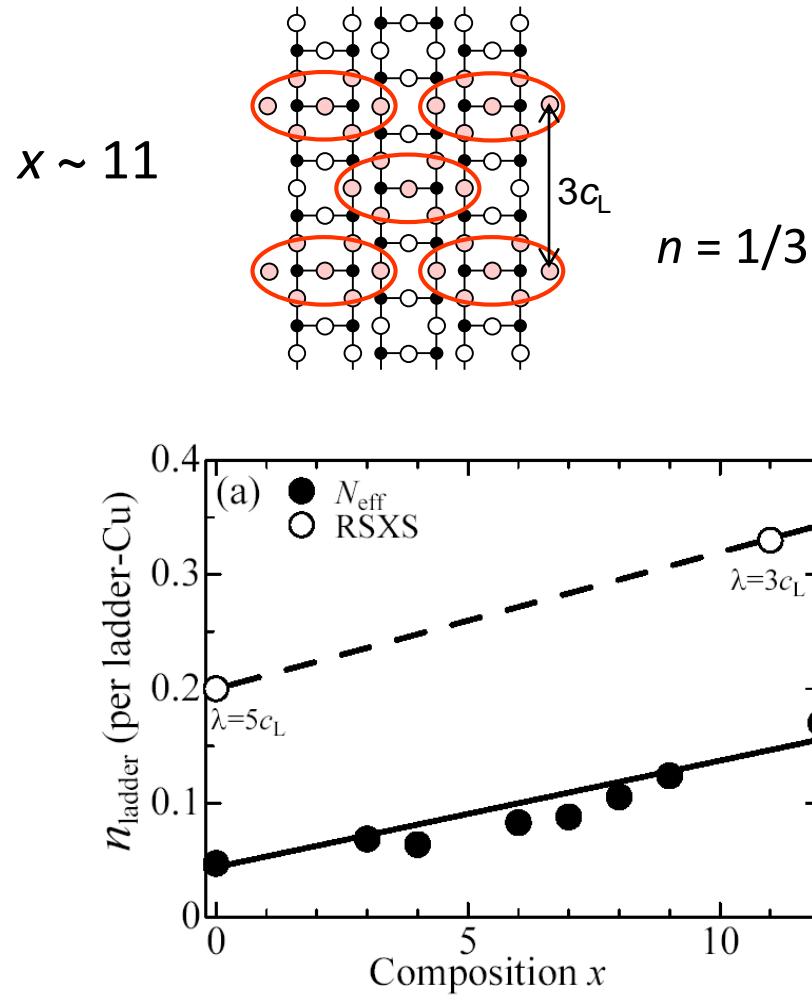
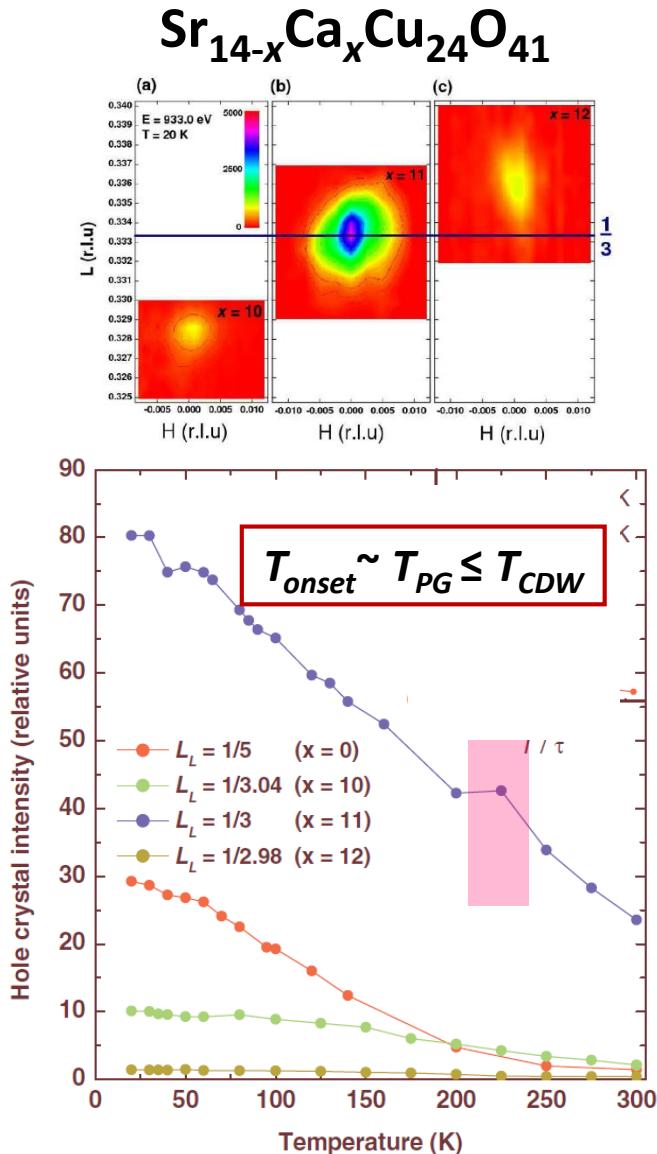
# Onset temperature of t-JP & phonon anomaly



K. Takenaka, H. Takagi,  
SU, PRB **50**, 6534(R)  
(1994).

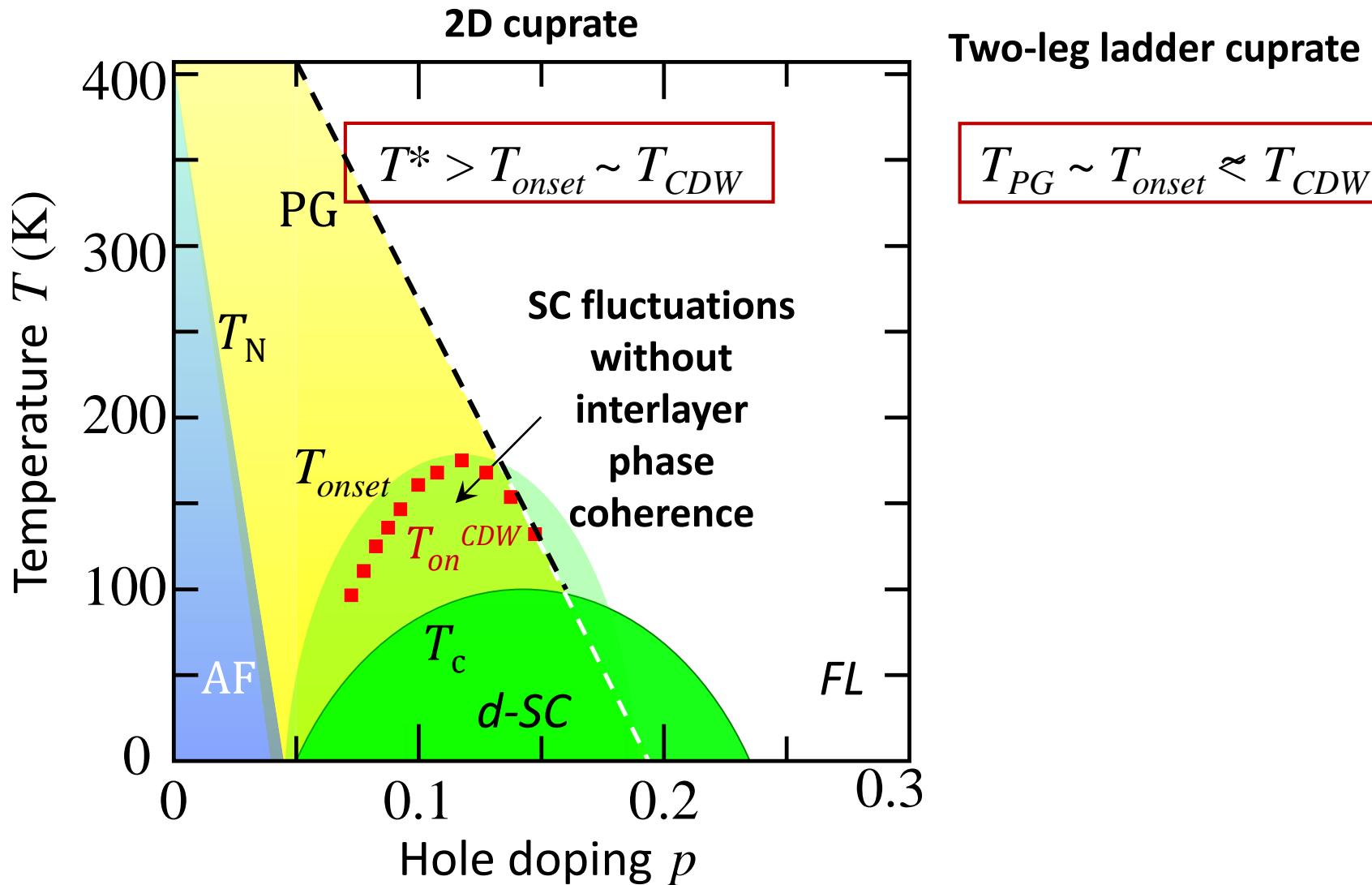
# Charge (hole-pair) order in two-leg ladder cuprate

A. Rusydi, P. Abbamonte *et al.*, Phys. Rev. Lett. **97**, 016403 (2006).



T. Osafune, N. Motoyama, H. Eisaki,  
SU; PRL **78**, 1980 (1997).

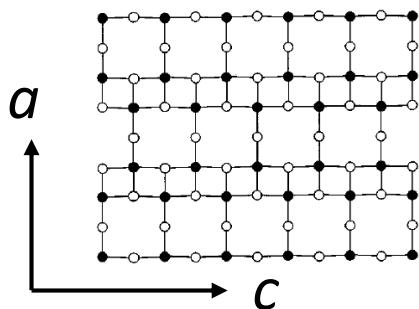
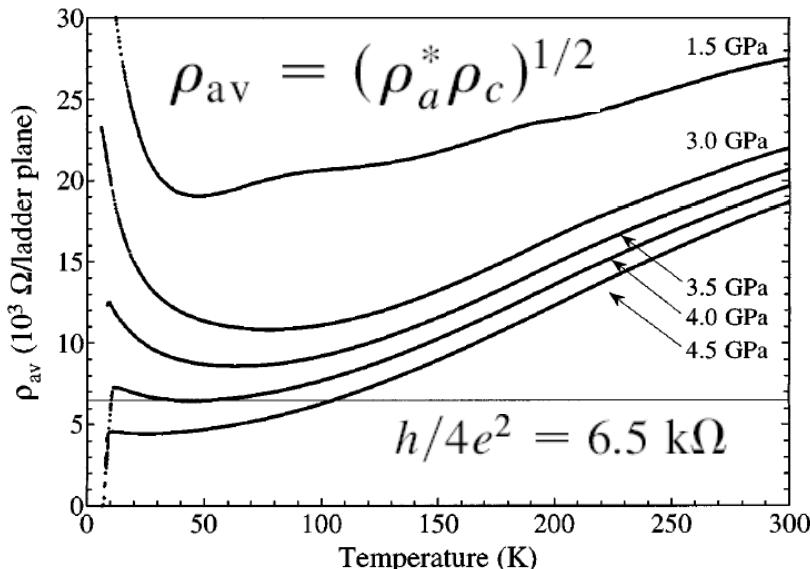
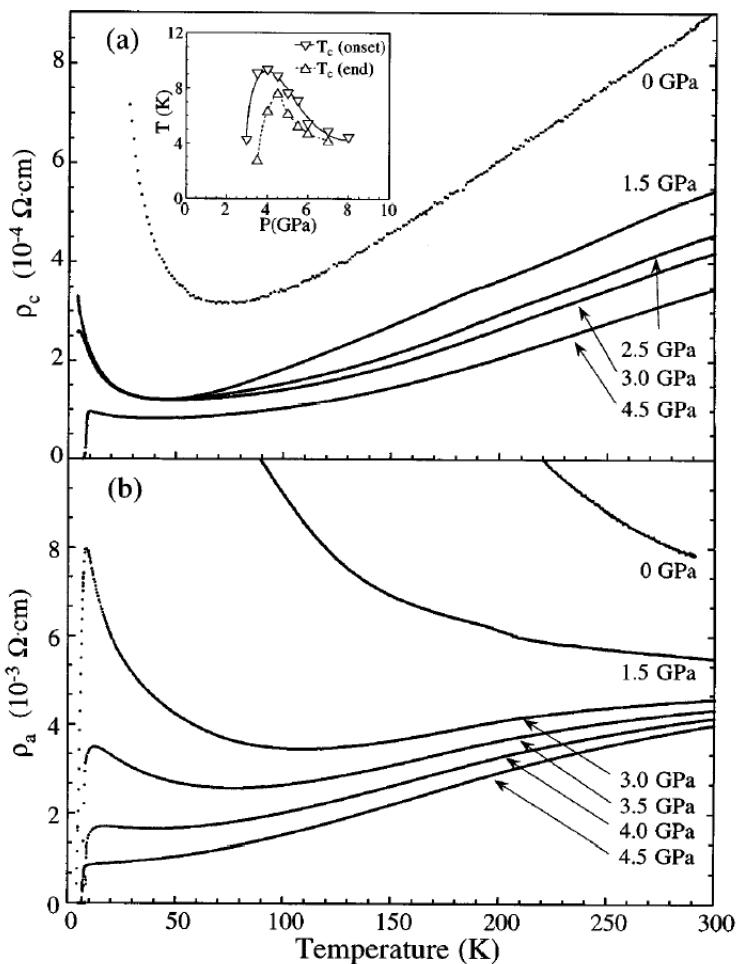
# Underdoped cuprate vs Ladder cuprate



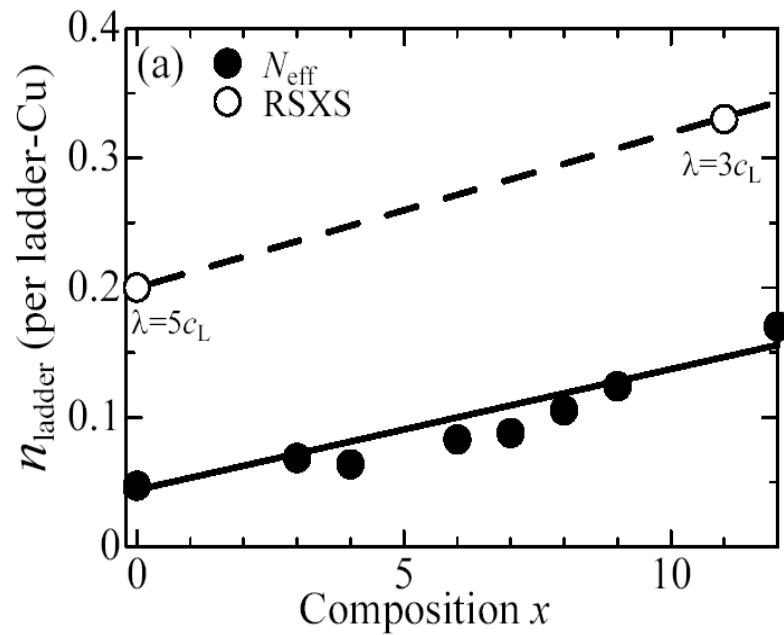
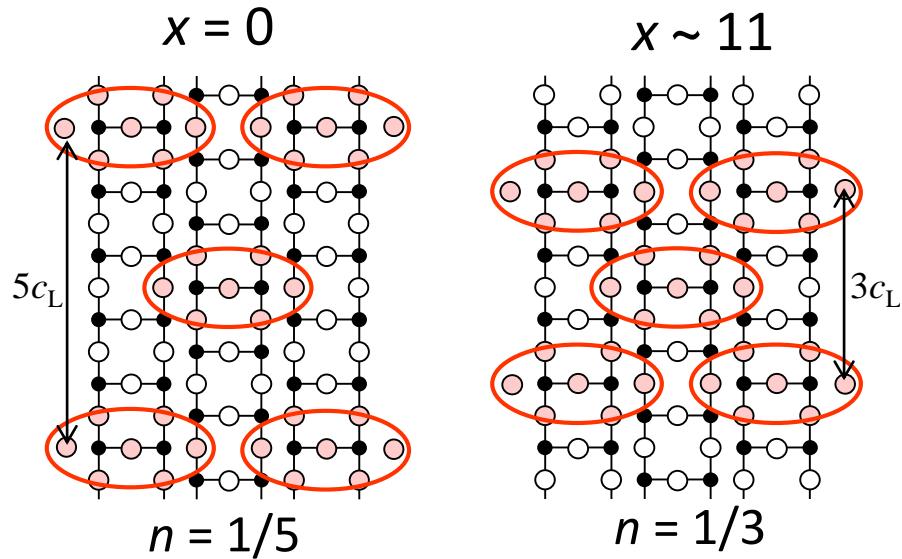
Congratulations to KITS,  
Fu-Chun Zhang, Jiang-Ping Hu,  
and other members

# Pressure-Induced Dimensional Crossover and Superconductivity in the Hole-Doped Two-Leg Ladder Compound $\text{Sr}_{14-x}\text{Ca}_x\text{Cu}_{24}\text{O}_{41}$

T. Nagata,<sup>1</sup> M. Uehara,<sup>1</sup> J. Goto,<sup>1</sup> J. Akimitsu,<sup>1</sup> N. Motoyama,<sup>2</sup> H. Eisaki,<sup>2</sup> S. Uchida,<sup>2</sup> H. Takahashi,<sup>3</sup> T. Nakanishi,<sup>3</sup> and N. Mori<sup>4</sup> Phys. Rev. Lett. **58**, 758 (2002).



# Controversy in the doped hole density



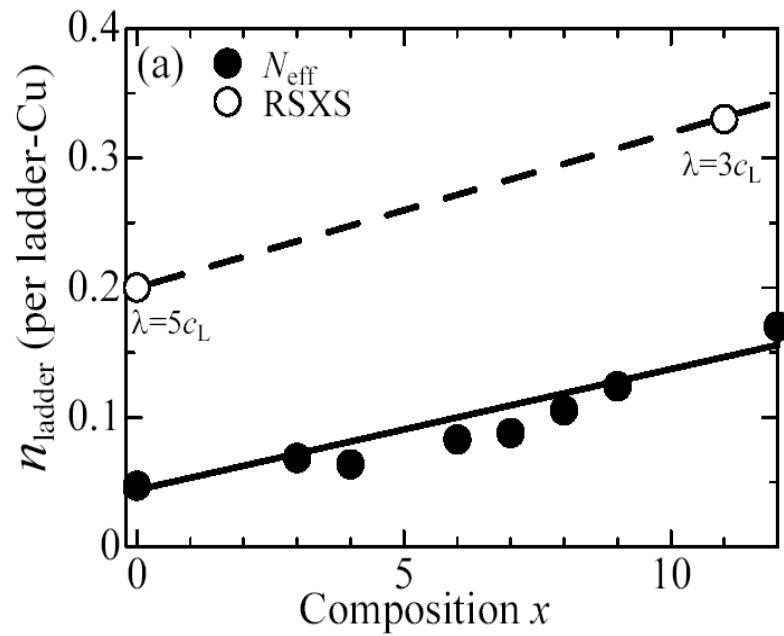
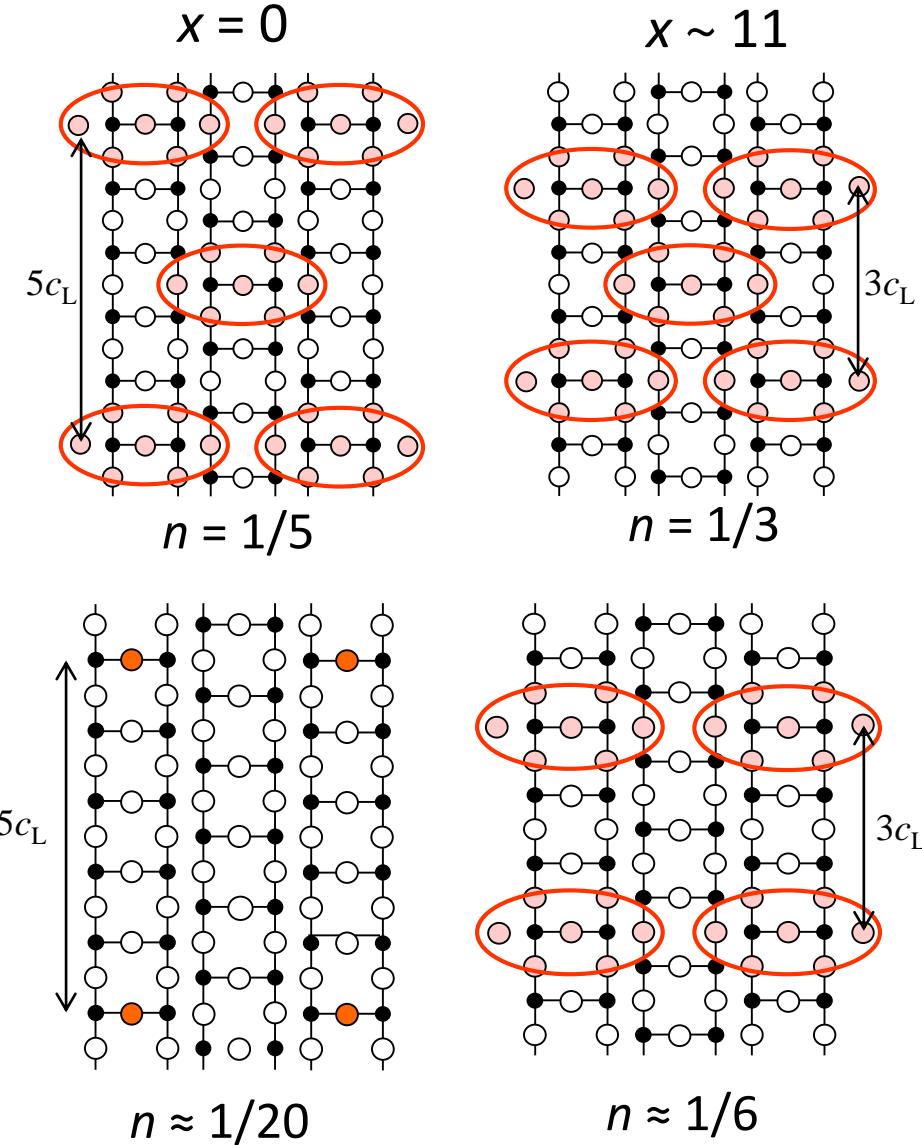
T. Osafune, N. Motoyama, H. Eisaki,  
SU; PRL **78**, 1997 (1997).

A. Rusydi, P. Abbamonte *et al.*, Phys. Rev. Lett. **97**, 016403 (2006).

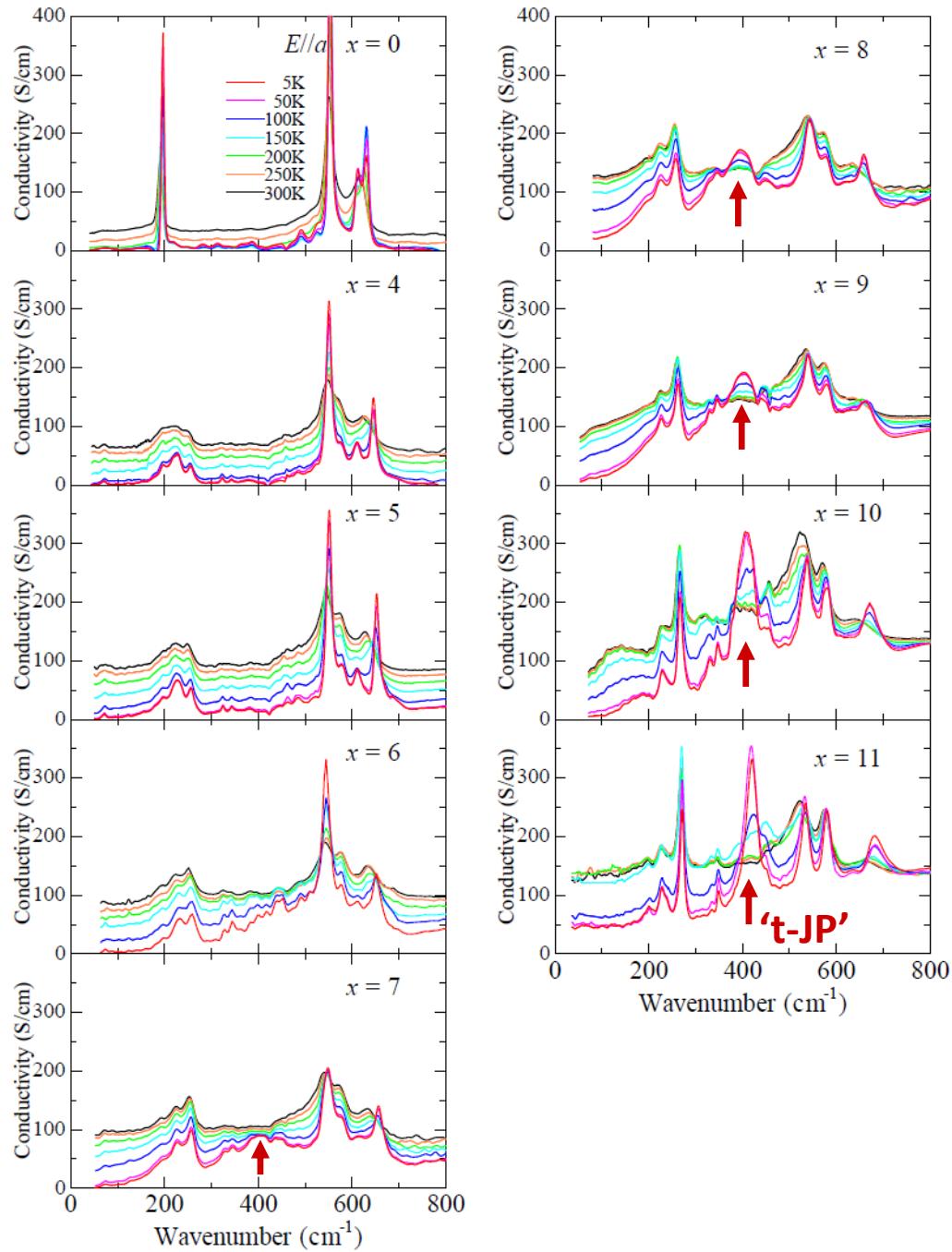
K. Wohlfeld, A. Oles, G.A. Sawatzky, PRB **75**, 180501(R) (2007).

J. Almeida, G. Roux, D. Poilblanc, PRB **82**, 041102(R) (2010).

# Controversy in the doped hole density

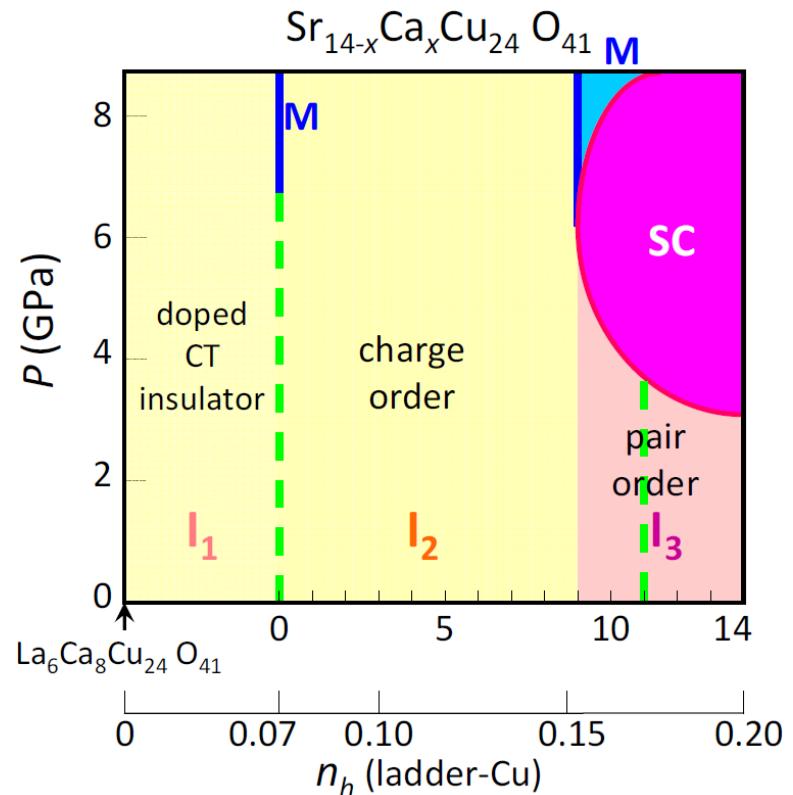


Y. Fujimaki, M. Nakajima, SU;  
*unpublished*

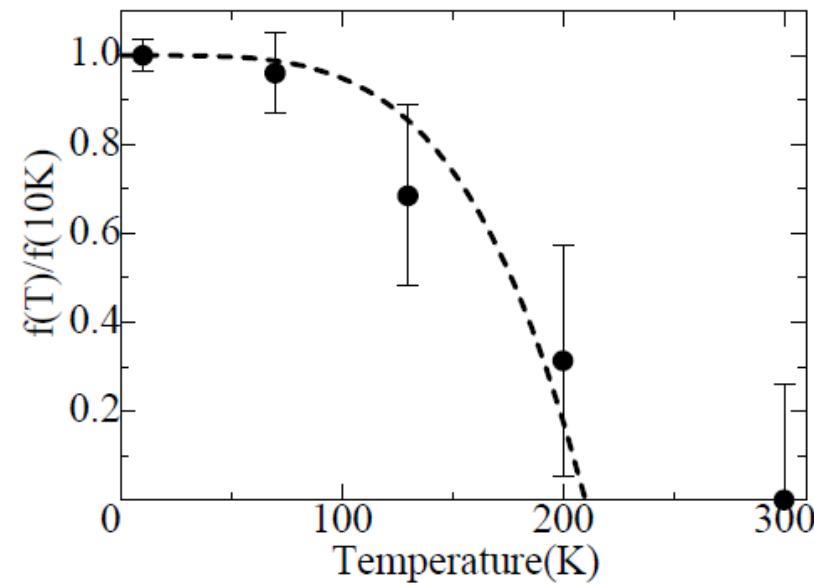
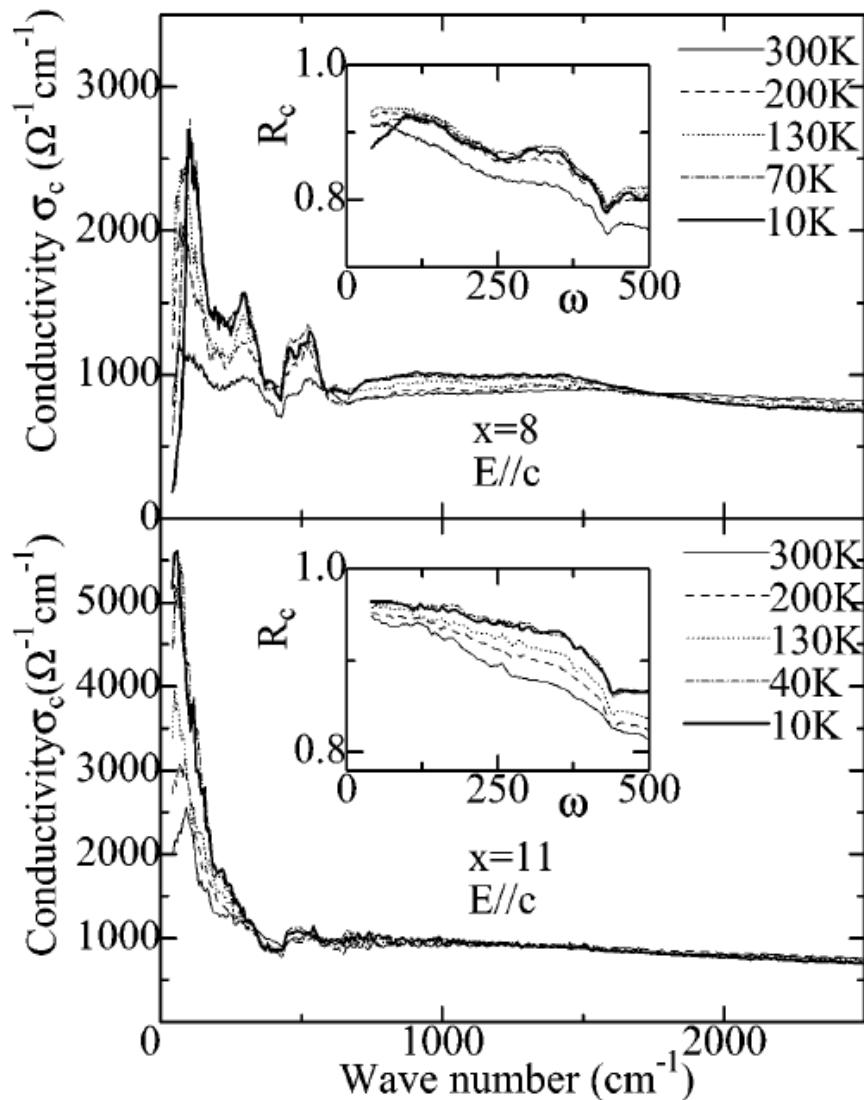


t-JP & phonon anomaly  
are observed for highly  
hole-doped 14-24-41

$x$ - $P$  phase diagram ( $T = 0$ )



# Spectroscopic signature of the charge order



T. Osafune, SU, S. Tajima *et al.*; PRL **82**, 5654 (1999).

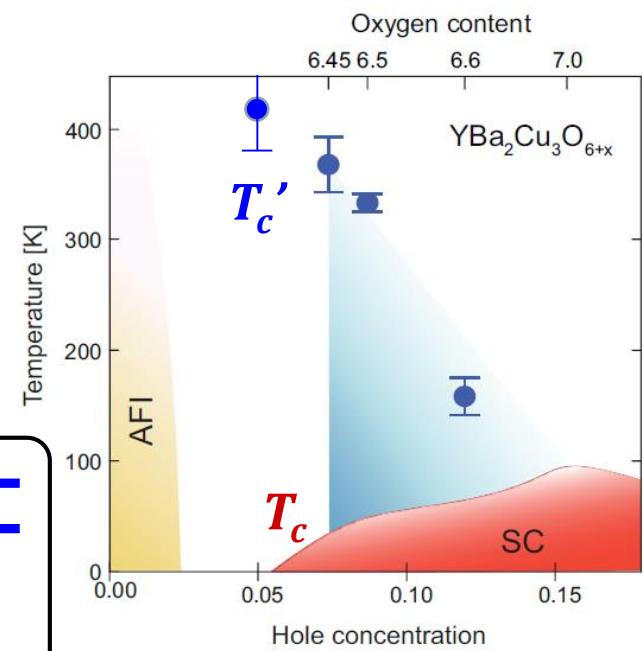
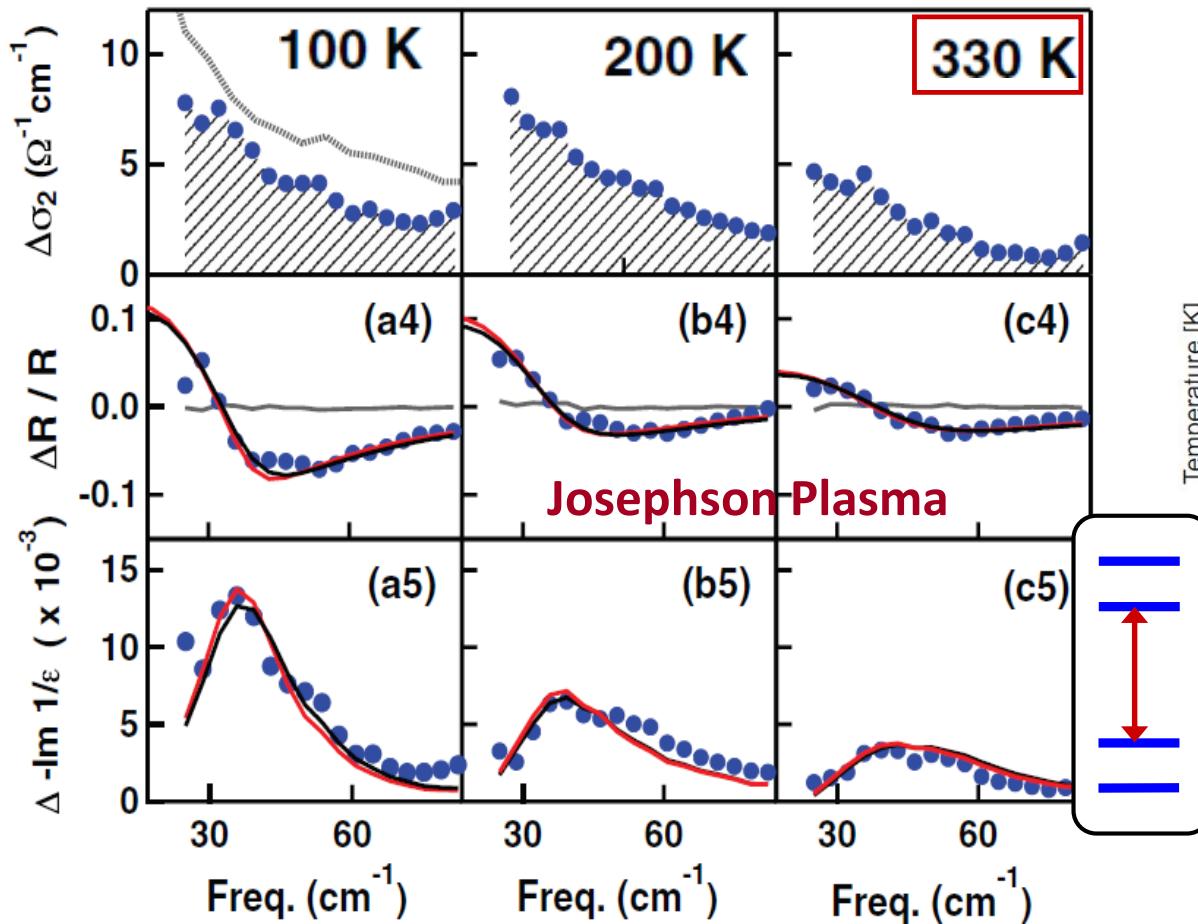
# Transient SC- $T_c'(p)$ follows $T^*(p)$ .

S. Kaiser, A.Cavalleri *et al.*; PRB **89**, 184516 (2014).

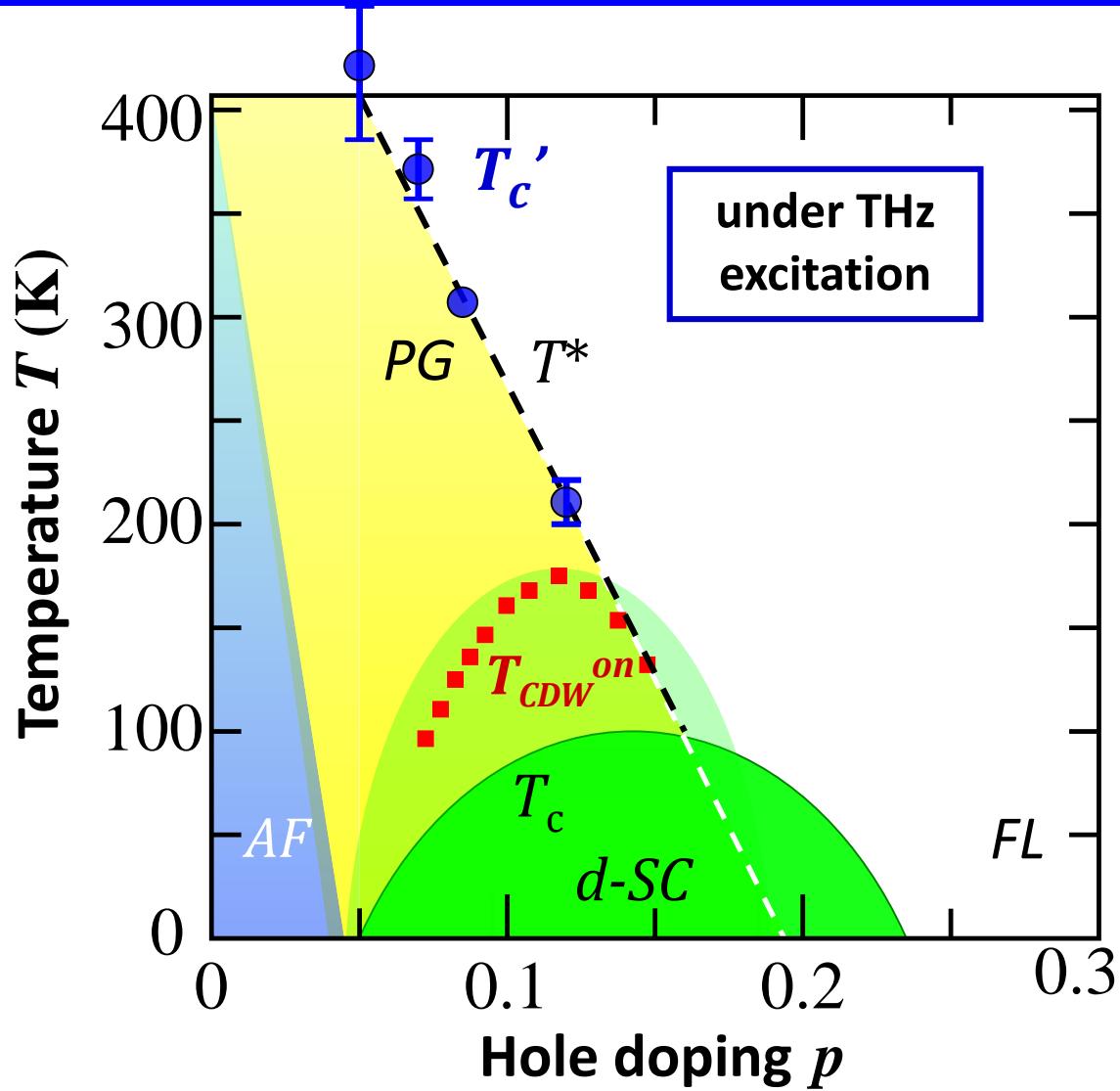
C.R. Hunt, A.Cavalleri *et al.*; PRB **94**, 224303 (2016).

***Interbilayer coherence is transiently established.***

YBCO6.45 excited by  $\sim 20$  THz pulsed laser

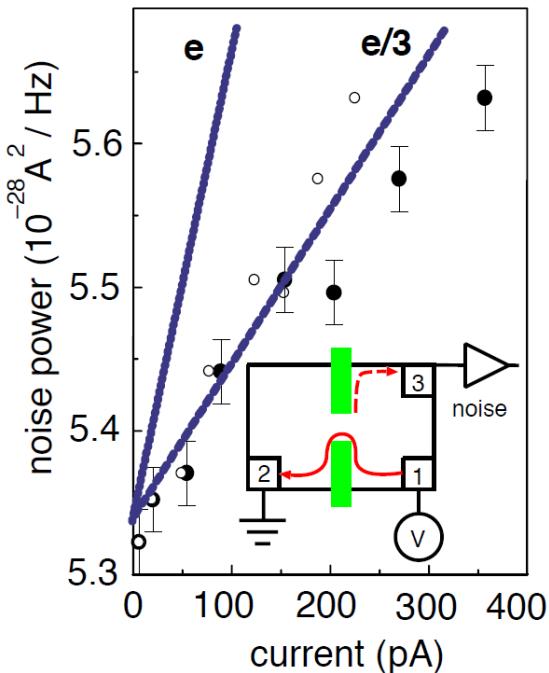


Transient  $T_c'(p)$  follows  $T^*(p)$ .



# Quantum Shot Noise & Johnson Noise

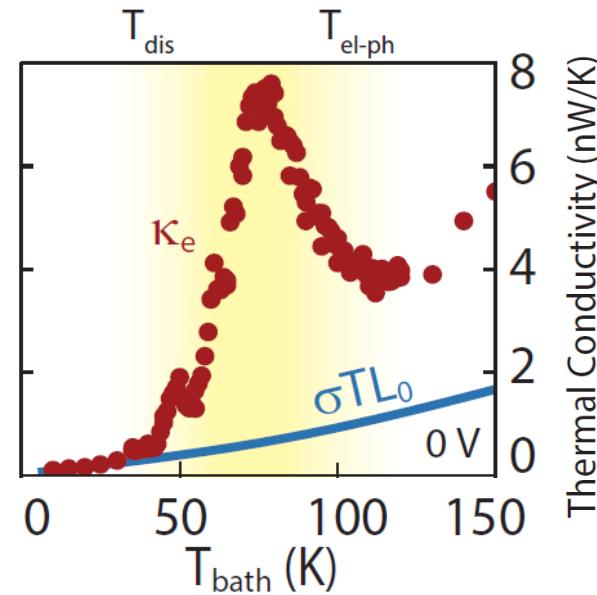
## GaAs/GaAlAs or Graphene



**Quantum shot noise** results from the discreteness of the current-carrying charges, and so is proportional to the **charge** of the quasiparticles.

V.J. Goldman, B. Su;  
Science **267**, 5200 (1995).

## Graphene



**Johnson noise** thermometry measures electronic thermal conductivity, and can test the **Wiedemann-Franz law**.

J. Crossno, P. Kim *et al.*,  
Science **351**, 1058 (2016).