Anomalous Metals and Failed Superconductors

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Context – Two Pillars of Our Understanding of Quantum Mater

"Anderson localization" implies no metals in 2D

Small Ginzburg parameter implies there are no important superconducting fluctuations in "conventional" superconductors

Both are seemingly wrong.

"Anderson localization" implies no metals in 2D?

$$\sigma = \frac{e^2}{h} \left(k_F \ell \right) \left\{ 1 - \left(\frac{1}{2\pi k_F \ell} \right) \log \left| \frac{L_T}{\ell} \right| + \ldots \right\}$$

Extended using perturbative RG analysis

Verified numerically for non-interacting particles

No theoretical control in the presence of strong interactions or when $k_F \ 1 \ \sim 1$.

$$T^{\star} \sim E_F \exp[-\pi k_F \ell]$$

Even for weak interactions, there could be new effects at scales E_F >>> E >>> T*.

"Anderson localization" implies no metals in 2D??

Apparent Metal Insulator Transition in Clean 2DEGs with large r_s

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Quantum Hall Metal in 2DEG in large H

Quantum Superconductor to Insulator transitions in 2D

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Quantum Superconductor to Insulator transitions in 2D Quantum Superconductor to Metal transitions in 2D

$$\mathcal{N} = \rho(E_F)(\xi_0)^d \Delta_0 \qquad \qquad \mathcal{G} = 1/\mathcal{N}$$



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"Fluctuation Superconductivity" of Aslamazov-Larkin and Maki-Thomson are small (Gaussian) corrections to mean-field theory except in parametrically narrow region around T_c.

The case of the quantum transition is even worse:

$$\Delta_0 \sim \omega_0 \exp[-1/\lambda^{eff}(x)]$$
$$\lambda^{eff} > 0 \text{ for } x < x_c$$
$$\lambda^{eff} < 0 \text{ and } \Delta_0 = 0 \text{ for } x < x_c$$
$$\lambda^{eff} = 0 \text{ for } x = x_c$$

Interactions in other channels are "irrelevant."

There are no quantum critical fluctuations at all!

Quantum phase transitions from SC state to non-superconducting state

Varying gate voltage, magnetic field, film thickness ...

As T tend to zero,

Superconducting for $x < x_c$ Non superconducting for $x > x_c$

Normal state characterized by Drude conductivity:

$$\rho = h/e^2 \ (k_F \ell)^{-1} \qquad h/e^2 \approx 25k\Omega$$



Magnetic Field Driven QSMT in aMoGe films





 $h/e^2 \approx 25k\Omega$

Mason and Kapitulnik, PRL (1999)



 $e^2/h \approx 25k\Omega$

Breznay and Kapitulnik, Science Advances (2017)

Magnetic Field Driven QSMT in crystalline films of NbSe₂



 $h/e^2 \approx 25k\Omega$

Tsen et al, Nature Physics (2016)

Magnetic Field Driven QSMT in a highly crystalline ZrNCl electric double layer transistor (Ion gated)



Saito et al, Science (2015)





Gate voltage driven QSMT in a WTe₂ flake



 $h/e^2 \approx 25k\Omega$

Sajidi *et al* (D. Cobden group from U. Washington) unpublished Gate voltage Driven QSMT in a SrTiO₃-SrAlO₃ heterostructure

10⁵ 10⁴ (bs/m40) *H* 10² 10¹ 0.005 0.01 0.015 0.02 0.025 1/T(mK⁻¹)

Chen *et al* (H. Hwang's group at Stanford) submitted for publication)

 $h/e^2\approx 25k\Omega$

Gate voltage Driven QSMT

in a gated twodimensional semiconductorsuperconductor array

Bottcher et al (C. Marcus's group at Niels Bohr Institute, submitted for publication)

 $h/e^2\approx 25k\Omega$





FIG. 4. Normalized resistance as a function of temperature for SNS arrays of widely spaced islands. For spacings exceeding 700 nm, the BKT transition is interrupted by a low-temperature metallic state. The data for $d \le 690$ nm and for $d \ge 740$ nm come from different substrates, having Nb island heights of 125 nm and 145 nm, respectively.



Some aspects of the theory

Consider problem of superconducting grains embedded in a metal and tune QSMT as function of concentration

 $\chi_j(T) = SC$ susceptibility of grain j

 $J_{ij}(T) =$ Josephson coupling between grain *i* and *j*

$$X_{ij}(T) \equiv \sqrt{\chi_i(T)} |J_{ij}(T)|^2 \chi_j(T)$$

Mean field estimate of T_c

$$\overline{\sum_{j} X_{ij}(T_c)} = A_c$$

B. Spivak, P. Oreto, and S. A. Kivelson, "Theory of quantum metal to superconductor transitions in highly conducting systems, Phys. Rev. B **77**, 214523 (2008).

$$\chi_j(T) = SC$$
 susceptibility of grain j

 $J_{ij}(T) =$ Josephson coupling between grain *i* and *j*

$$X_{ij}(T) \equiv \sqrt{\chi_i(T) |J_{ij}(T)|^2 \chi_j(T)}$$

Mean field estimate of $\rm T_{\rm c}$

$$\chi_j(T) < \chi_j(0) < \infty$$

$$\sum_{j} X_{ij}(T_c) = A_c$$

$$J_{ij}(T) \sim |\vec{R}_{ij}|^{-d} \text{ for } |\vec{R}_{ij}| < L_T$$
$$J_{ij}(T) \sim \exp[-|\vec{R}_{ij}|/L_T] \text{ for } |\vec{R}_{ij}| > L_T$$
$$\sum_j X_{ij}(T) \sim \log[L_T]$$

The ground state is always superconducting!

$$\chi_j(T) = SC$$
 susceptibility of grain j

 $J_{ij}(T) =$ Josephson coupling between grain *i* and *j*

$$X_{ij}(T) \equiv \sqrt{\chi_i(T)} |J_{ij}(T)|^2 \chi_j(T)$$

Mean field estimate of T_c $\chi_j(T) < \chi_j(0) < \infty$ $J_{ij}(T) \sim |\vec{R}_{ij}|^{-d} \Big[1 + \mu \log^2 |\vec{R}_{ij}| \Big]^{-1}$ for $|\vec{R}_{ij}| < L_T$ $\sum_j X_{ij}(T) \sim \chi(0) \ J_{nn}(0)$

Presence of (weak) repulsive interactions in metals result in a failed superconductor and an anomalous metal near QSMT While this is a good theory "in principle" it has problems with the broad stability of the anomalous metal

Mean field estimate of
$$T_c$$

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 $J_{ij}(T) \sim |\vec{R}_{ij}|^{-d} \left[1 + \mu \log^2 |\vec{R}_{ij}| \right]^{-1}$ for $|\vec{R}_{ij}| < L_T$
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Quantum critical regime : $A_c > \chi(0)J_{nn}(0) >$ small

$$L_T > R_{nn}$$
 $T < J_{nn}(0) \sim 1/\chi(0)$
 $\chi(0) \sim \rho(E_F)V \exp[+\sigma^{eff}/\sigma_q]$ for large grain
 $\chi(0) \sim \rho(E_F)V$ for small grain

For the most part, these are not "strongly correlated materials"

What is needed is theory beyond ADG

There are missing "small" effects which are larger than T* and larger than T_c as T_c tends to 0.

Fermi liquid "theory" Localization "theory" BCS theory

Thank you.



FIG. 7. (Color online) Sheet resistance as a function of temperature for different values of V_G and in two different magnetic fields. Panels (a) and (c) show the data taken in the R_{s1} direction with 0 T and 9 T magnetic fields, respectively, and panels (b) and (d) show the measurements obtained for the R_{s2} direction under 0 T and 9 T magnetic fields, as well. The inset of panel (a) shows a magnification of the superconducting part in a log-log scale.