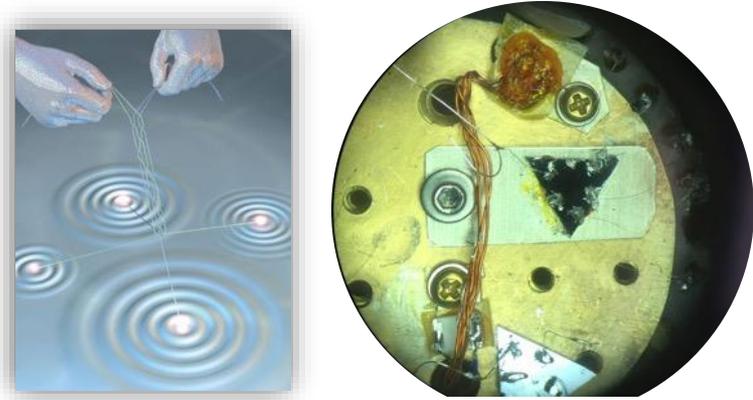
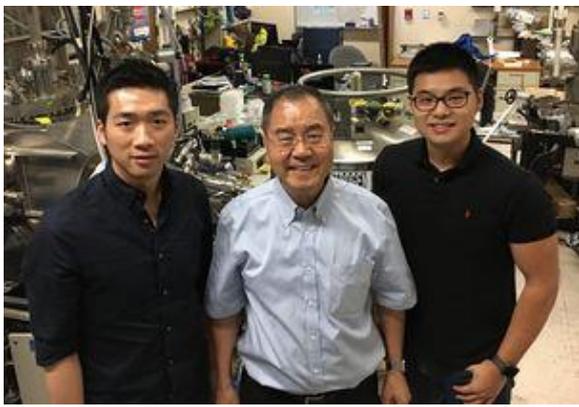


# Evidence for chiral Majorana edge modes in a topological heterostructure



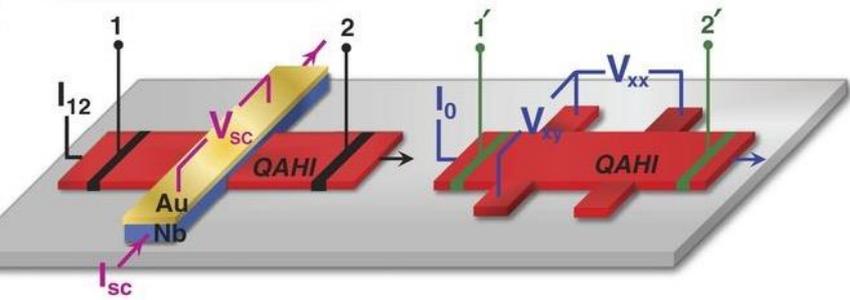
Prof. Kang L. Wang  
(UCLA) middle

Prof. S.C. Zhang  
(Stanford)



Qinling He (left)

& Kai Liu (UCD)

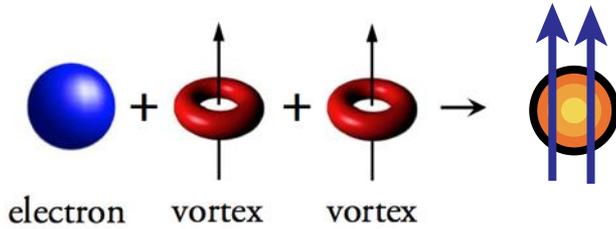


Qing Lin He, Lei Pan, Alexander L. Stern, Edward Burks, Xiaoyu Che, Gen Yin, Jing Wang, Biao Lian, Quan Zhou, Eun Sang Choi, Koichi Murata, Xufeng Kou, Tianxiao Nie, Qiming Shao, Yabin Fan, Shou-Cheng Zhang, Kai Liu, Jing Xia, Kang L. Wang

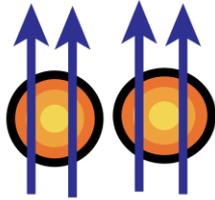
***Jing Xia, UC Irvine***  
***May 7th, 2018 @ CAS***  
***Topological Workshop***

# Lesson from $\nu = 5/2$ non-Abelian FQHE

Composite Fermion (CF) =  
 1 electron + 2 flux quanta  
 (zero effective B field at  $\nu = 5/2$ !)

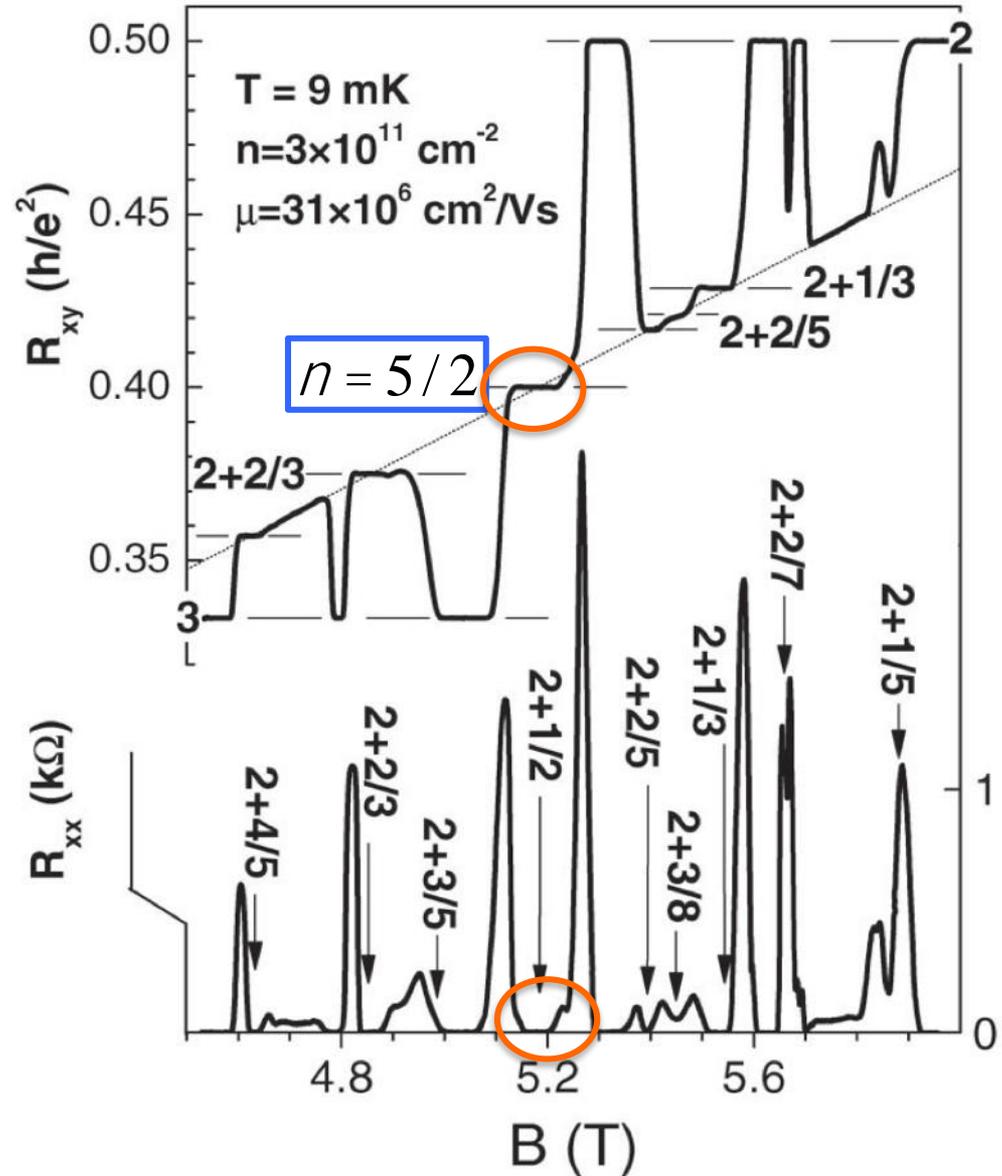


Moore-Read “Pfaffian” state

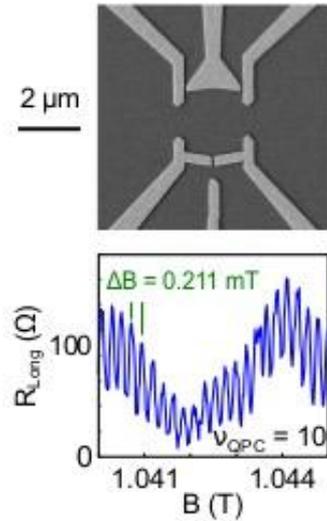


Chiral “p-wave” superconductor  
 of composite Fermions

*Can we get rid of the  
 high magnetic field?*



# “Artificial” $5/2$ state w/o magnetic field



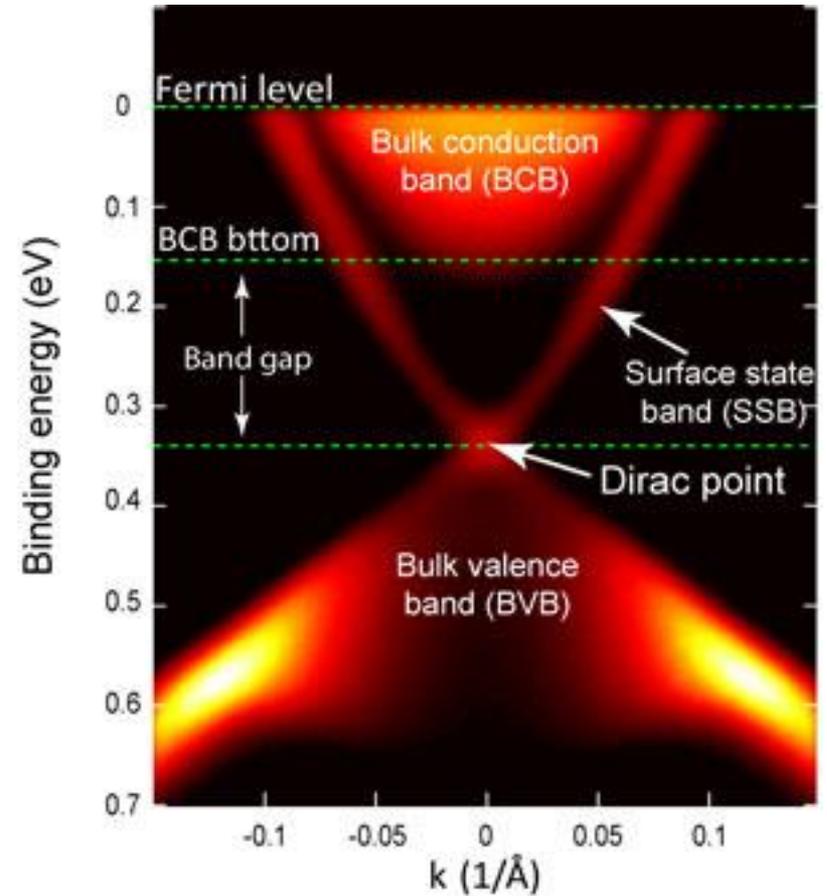
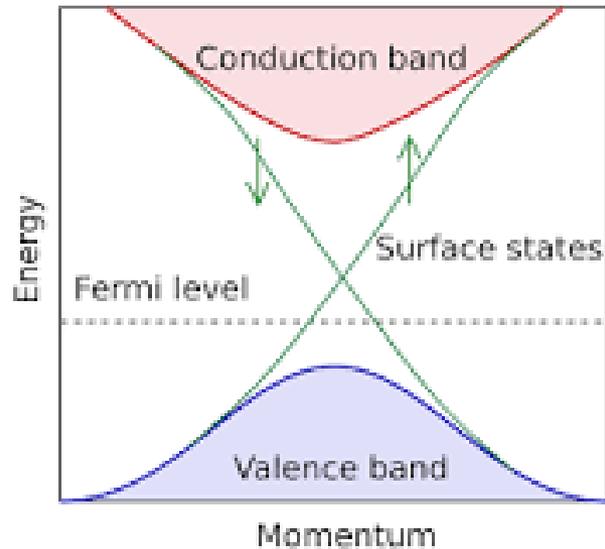
*$5/2$  FQHE state is very hard to achieve and very hard to work with.*

$5/2$  FQHE state is essentially:

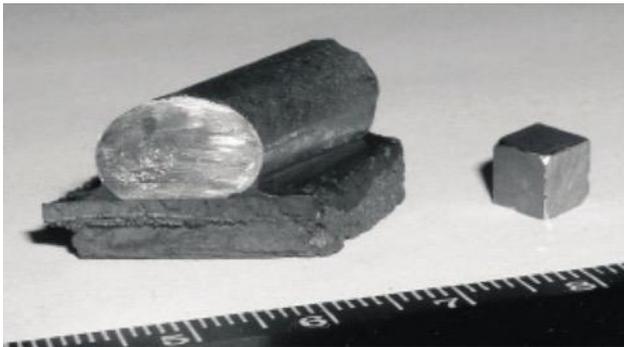
a “superconductor” of composite Fermions in

FQHE at high magnetic field

# Topological Insulator



Bismuth telluride ( $\text{Bi}_2\text{Te}_3$ )

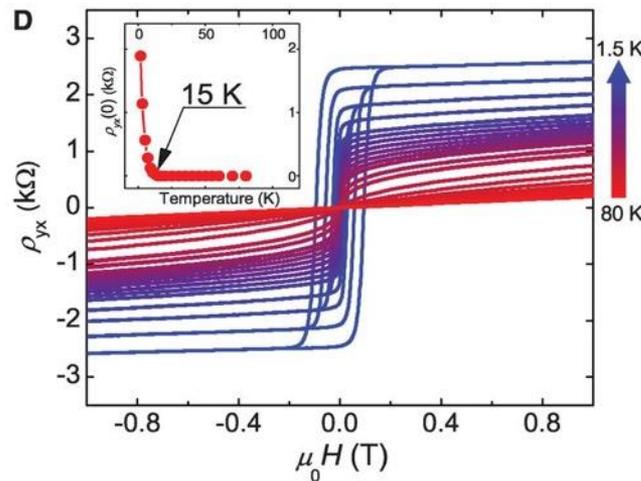
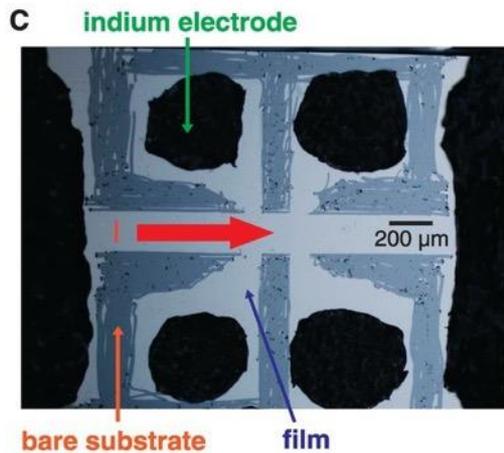
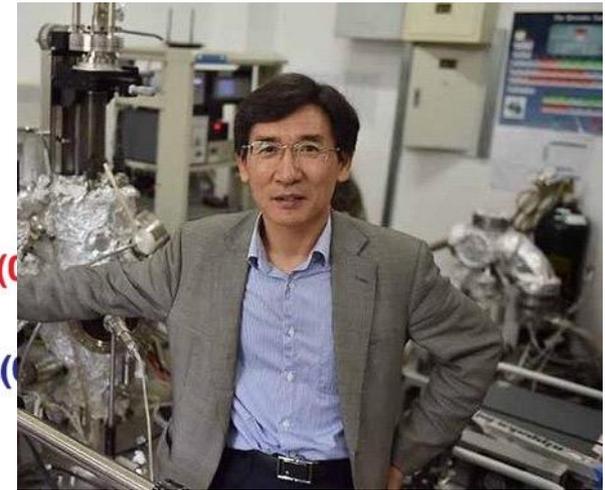
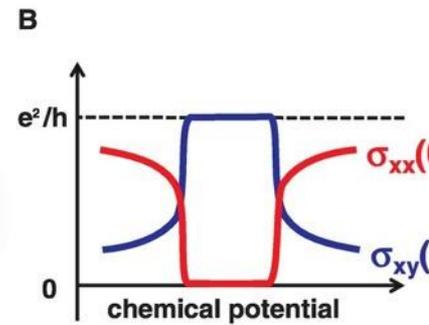
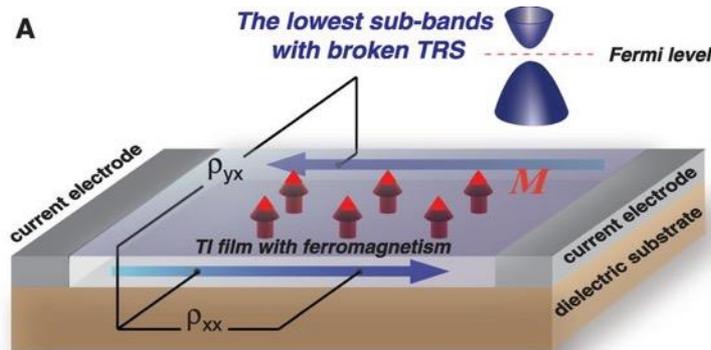


A review, see:

Xiao-Liang Qi and Shou-Cheng Zhang  
Rev. Mod. Phys. 83, 1057

# Quantum Anomalous Hall effect

Adding magnetic dopants: a “quantum Hall state” **without magnetic field!**

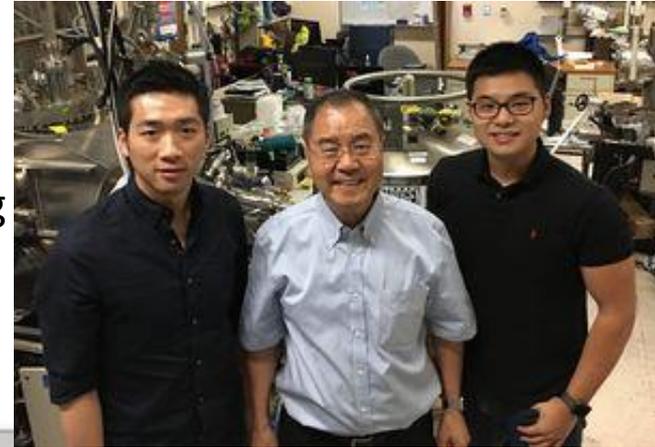
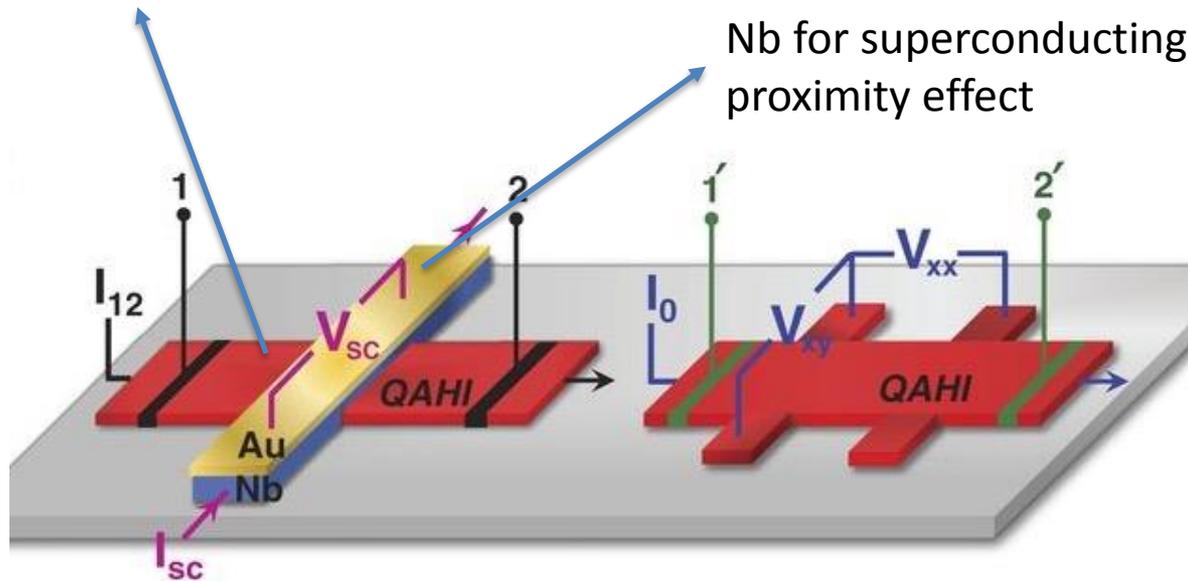


Discovery of the Quantum Anomalous Hall effect

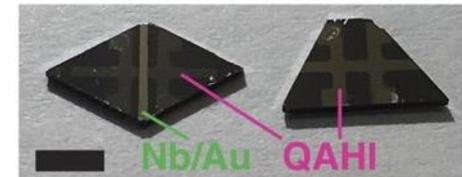
Qi-Kun Xue group,  
Science 340, 167 (2013)

# Adding “superconductor”

Quantum Anomalous Hall sample:  
(Cr<sub>0.12</sub>Bi<sub>0.26</sub>Sb<sub>0.62</sub>)<sub>2</sub>Te<sub>3</sub> (6 nm thick)



Prof. Kang L. Wang  
group, UCLA



## REPORT

# Chiral Majorana fermion modes in a quantum anomalous Hall insulator–superconductor structure

Qing Lin He<sup>1,\*</sup>, Lei Pan<sup>1,†</sup>, Alexander L. Stern<sup>3</sup>, Edward C. Burks<sup>4</sup>, Xiaoyu Che<sup>1</sup>, Gen Yin<sup>1</sup>, Jing Wang<sup>5,6</sup>, Biao Lian<sup>6</sup>, Quan Zhou<sup>6</sup>, Eun Sang Choi<sup>7</sup>, Koichi Murata<sup>1</sup>, Xufeng Kou<sup>1,8,\*</sup>, Zhijie Chen<sup>4</sup>, Tianxiao Nie<sup>1</sup>, Qiming Shao<sup>1</sup>, Yabin Fan<sup>1</sup>, Shou-Cheng Zhang<sup>6,\*</sup>, Kai Liu<sup>4</sup>, Jing Xia<sup>3</sup>, Kang L. Wang<sup>1,2,\*</sup>



Science

Vol 357, Issue 6348  
21 July 2017

[Table of Contents](#)  
[Print Table of Contents](#)  
[Advertising \(PDF\)](#)  
[Classified \(PDF\)](#)  
[Masthead \(PDF\)](#)

ARTICLE TOOLS

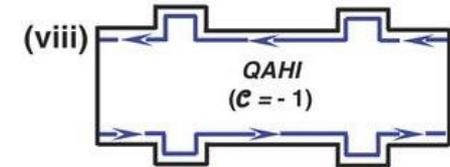
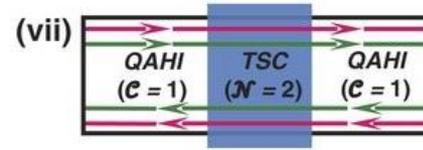
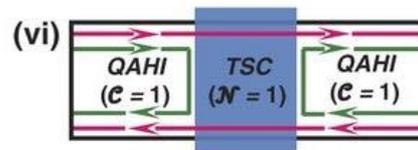
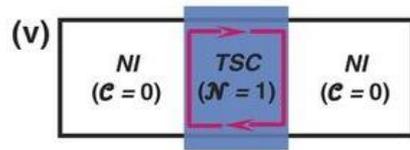
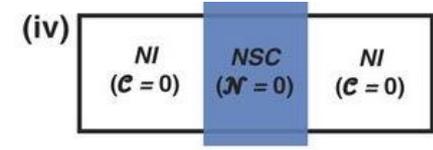
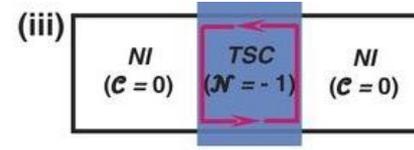
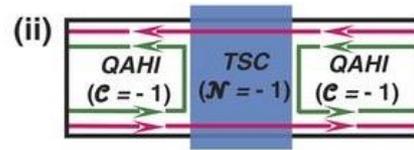
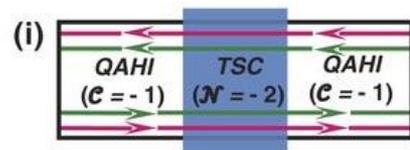
# A Chiral TSC

The quantum numbers (hence the chiral Majorana edge modes (CMEM)) of this artificially created chiral TSC (Topological Superconductor) can be tuned by a small magnetic field.



Prof. S.C. Zhang  
(Stanford)

$B = B_0$



$B \sim 0$

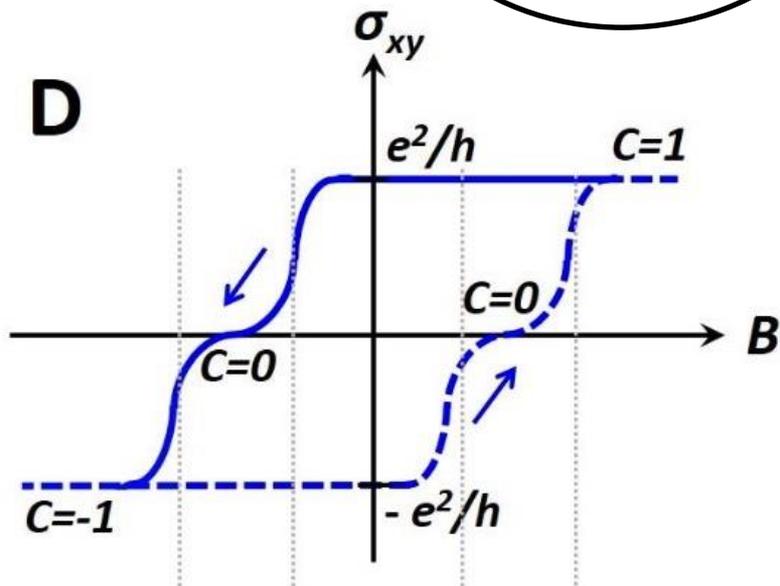
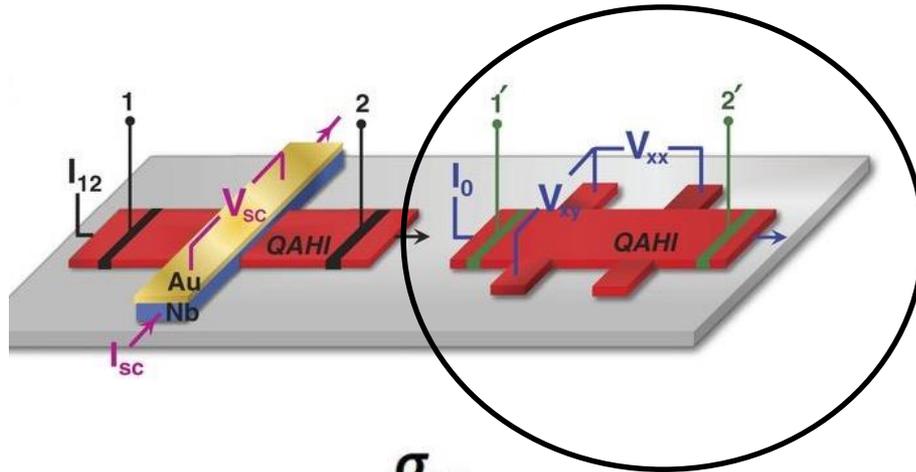
$B = -B_0$

**C:** Chern number  
QAHI: Quantum Anomalous Hall (C odd)  
NI: Normal Insulator (C = even)

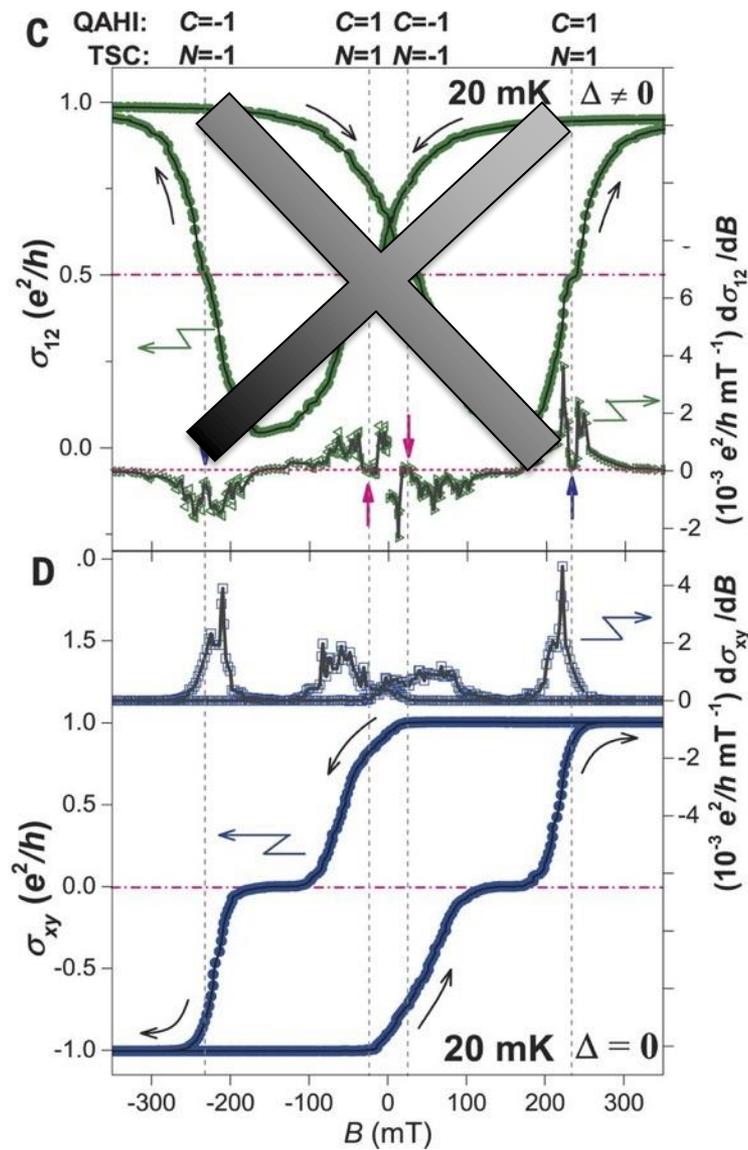
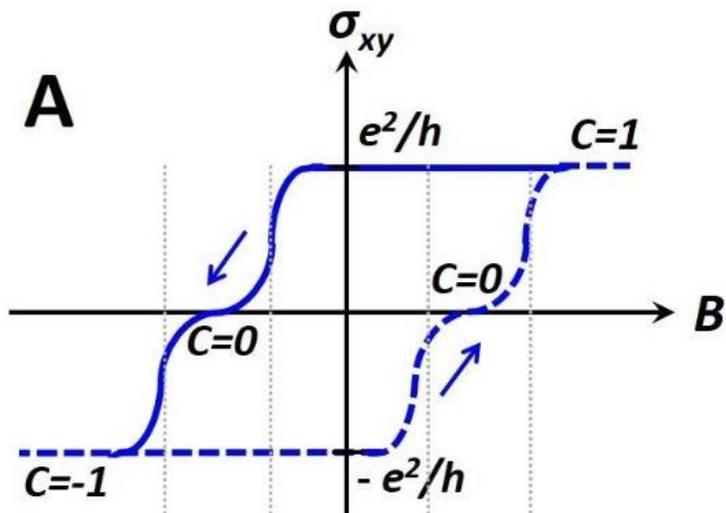
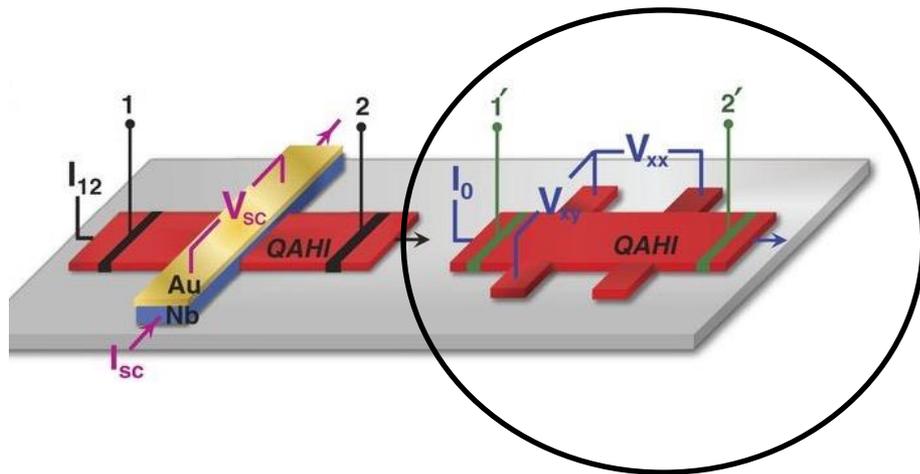
**N:** # of Chiral edge states  
TSC: Topological Superconductor (N odd)  
NSC: Normal Superconductor (N even)

# How to measure the C number?

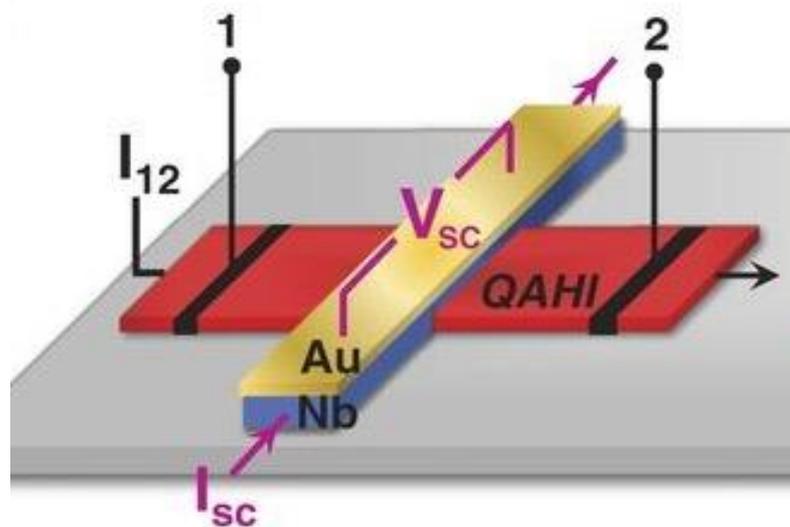
## QAHI



# Experiment



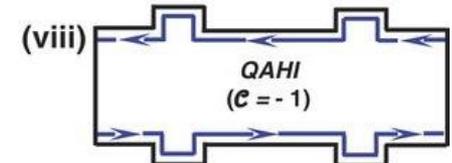
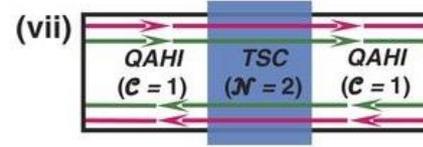
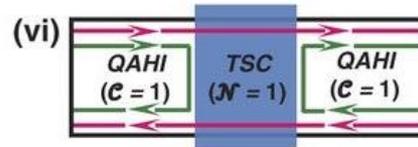
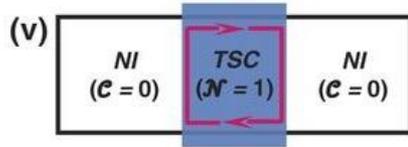
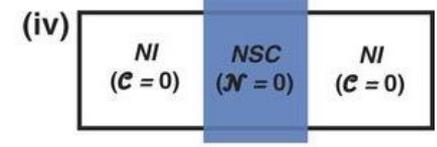
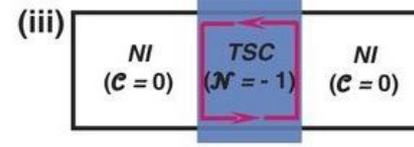
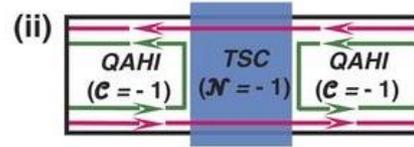
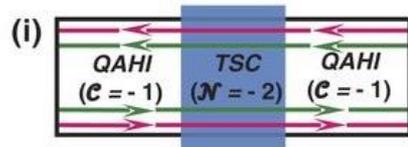
Now make the middle part SC.



# Adding superconductor

It is important to break inversion symmetry so that top and bottom SC gap are different.

$B = B_0$



$B \sim 0$

$B = -B_0$

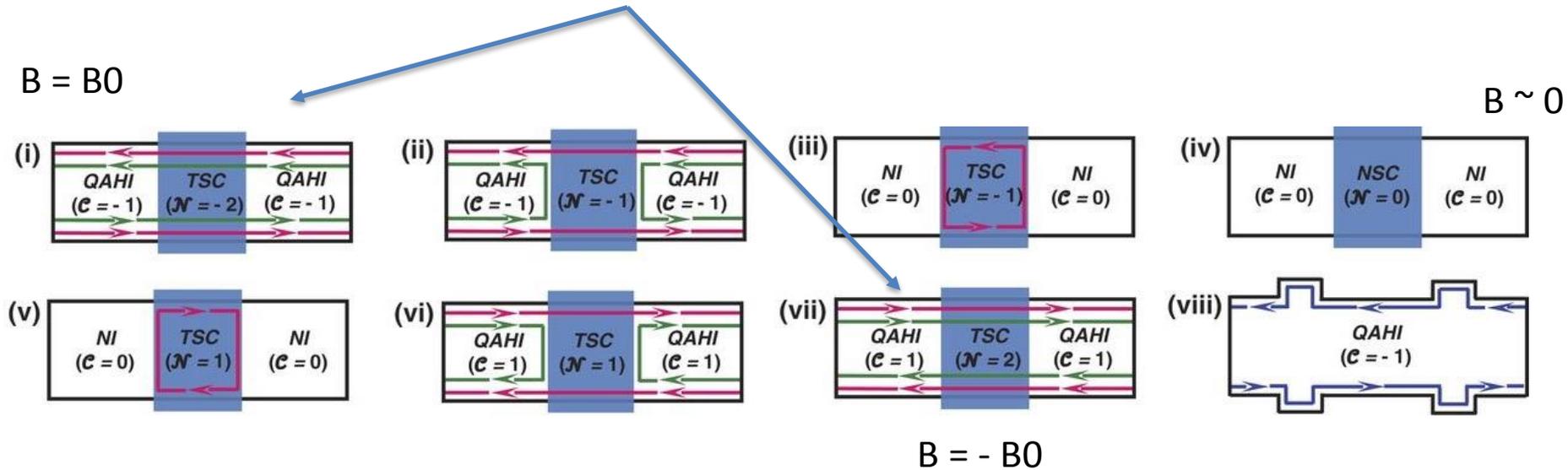
**C:** Chern number  
 QAHI: Quantum Anomalous Hall (C odd)  
 NI: Normal Insulator (C = even)

**N:** total Chern number  
 TSC: Topological Superconductor (N odd)  
 NSC: Normal Superconductor (N even)

# A Chiral TSC

It is important to break inversion symmetry so that top and bottom SC gap are different.

Two CMEM, topologically equivalent to 1 QH chiral edge



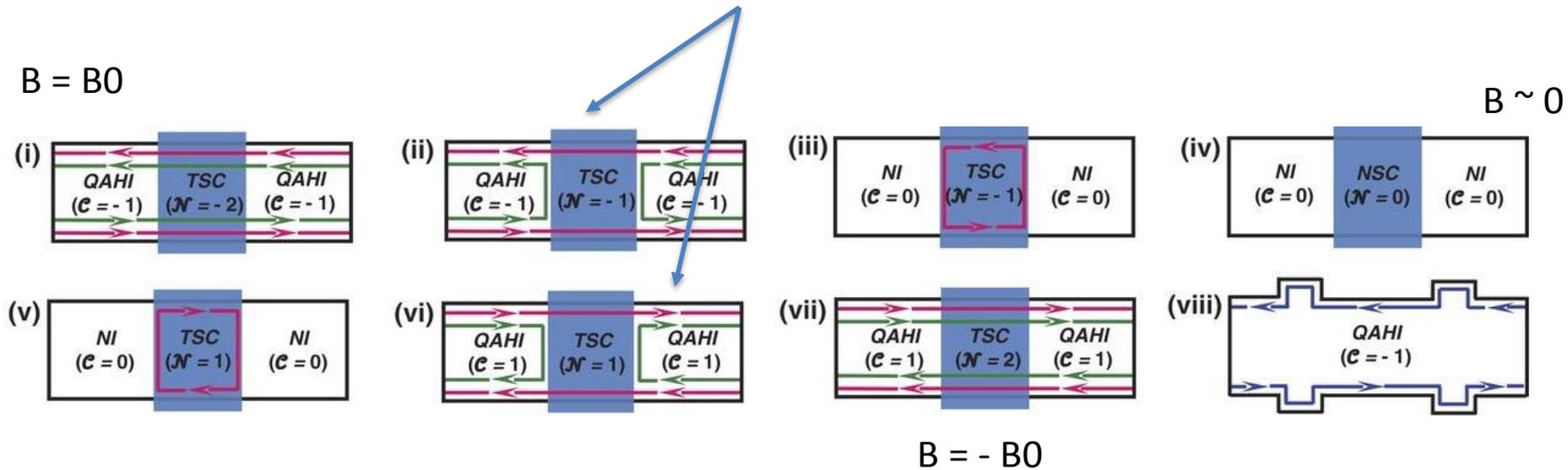
**C:** Chern number  
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**N:** total Chern number  
 TSC: Topological Superconductor ( $\mathcal{N}$  odd)  
 NSC: Normal Superconductor ( $\mathcal{N}$  even)

# A Chiral TSC

It is important to break inversion symmetry so that top and bottom SC gap are different.

One CMEM in TSC vanishes,  $N=1$ ; thus one CMEM in QAHI is reflected.



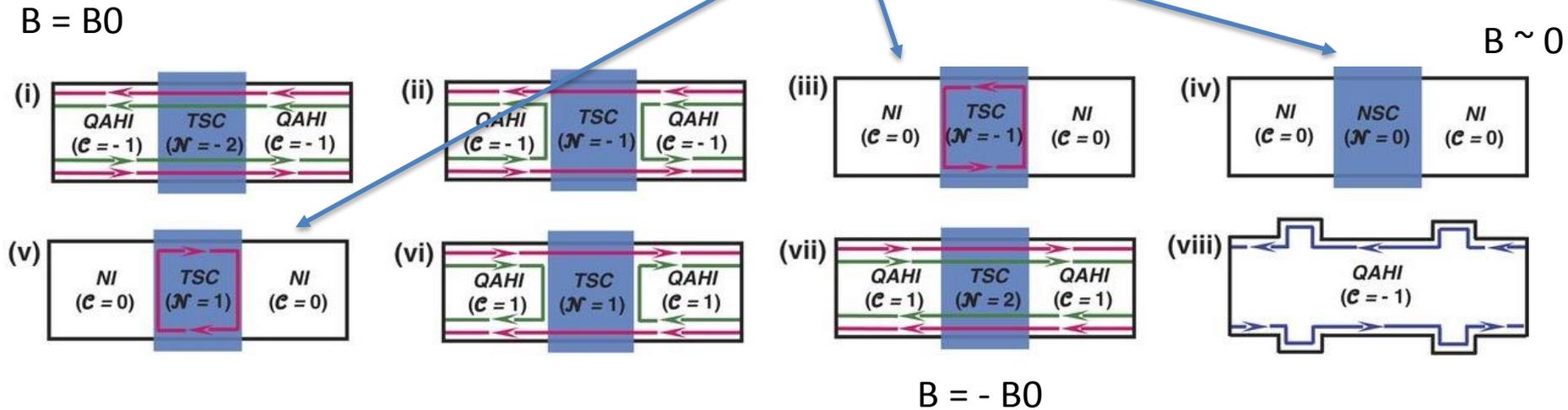
**C:** Chern number  
 QAHI: Quantum Anomalous Hall ( $C$  odd)  
 NI: Normal Insulator ( $C = \text{even}$ )

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# A Chiral TSC

It is important to break inversion symmetry so that top and bottom SC gap are different.

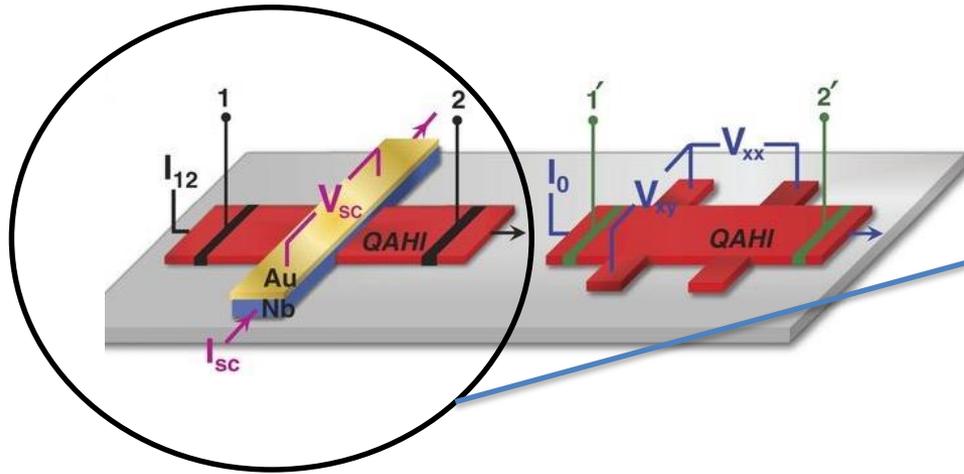
no conduction due to trivial insulating state (NI)



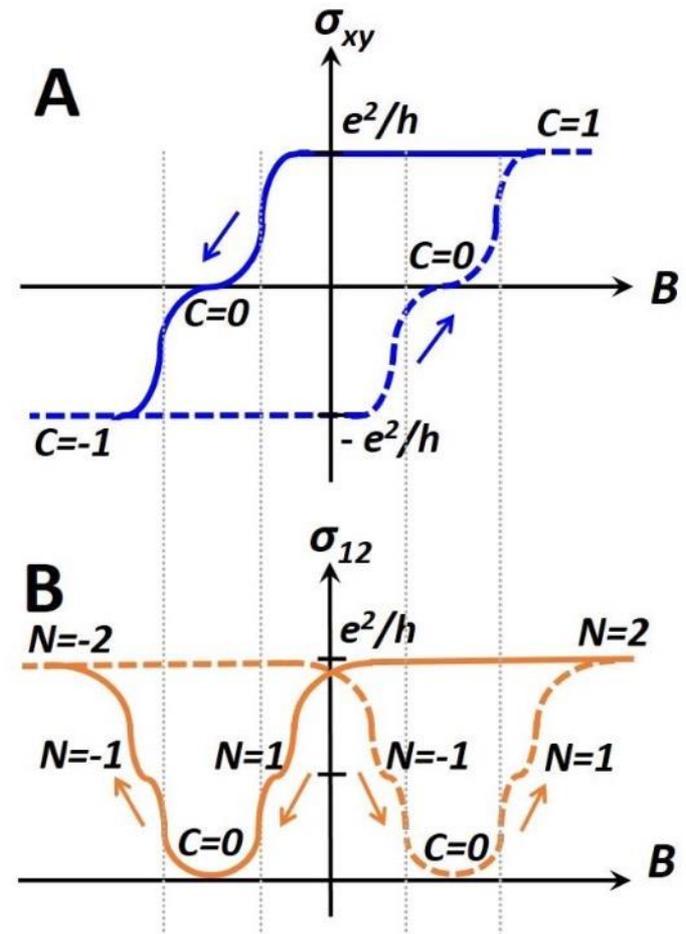
**C:** Chern number  
 QAHI: Quantum Anomalous Hall (C odd)  
 NI: Normal Insulator (C = even)

**N:** total Chern number  
 TSC: Topological Superconductor (N odd)  
 NSC: Normal Superconductor (N even)

# How do we know the N number?

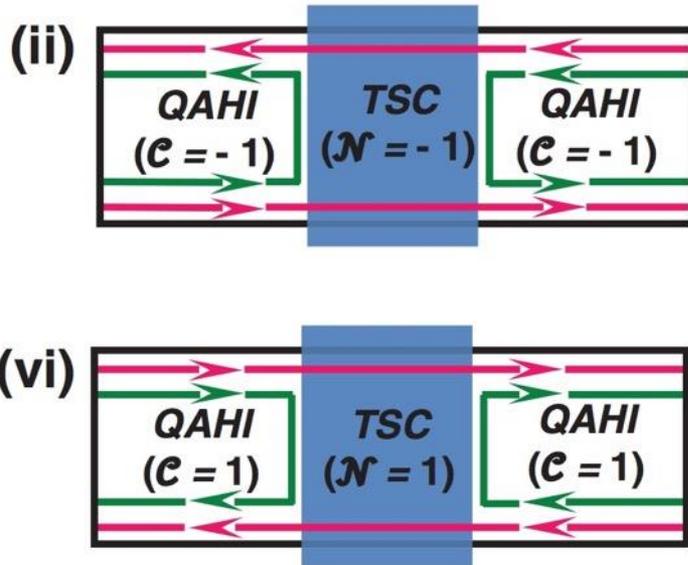


**If the middle is SC**



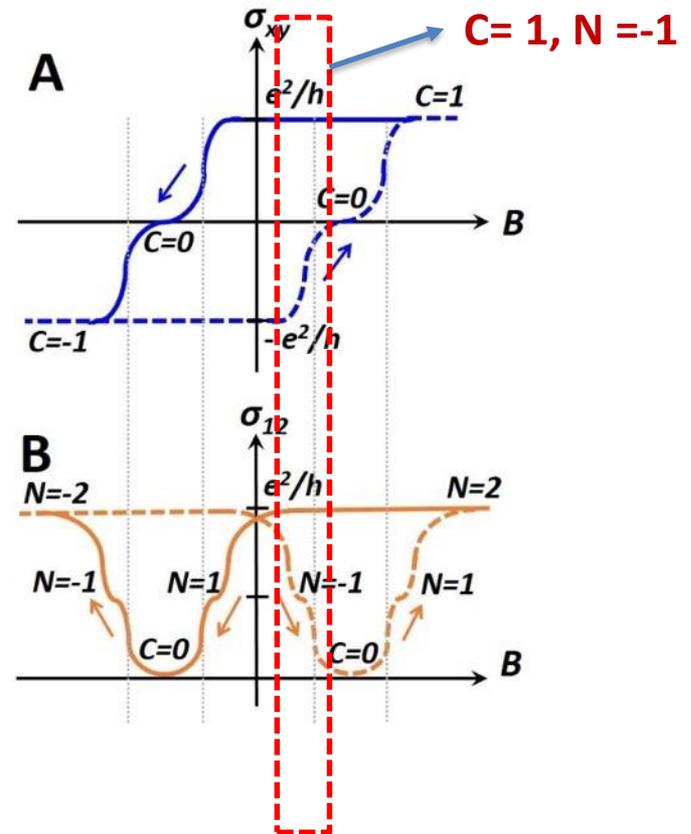
*In the middle of the QAHI bar, the proximity to an s-wave superconductor drives the QAHI into a superconducting regime, where a finite superconducting pairing amplitude is induced to the surface of the QAHI.*

# A Chiral TSC



The single **Chiral Majorana state** ( $N = \pm 1$ ) during the reversal of the magnetization (e.g. near zero magnetic field)

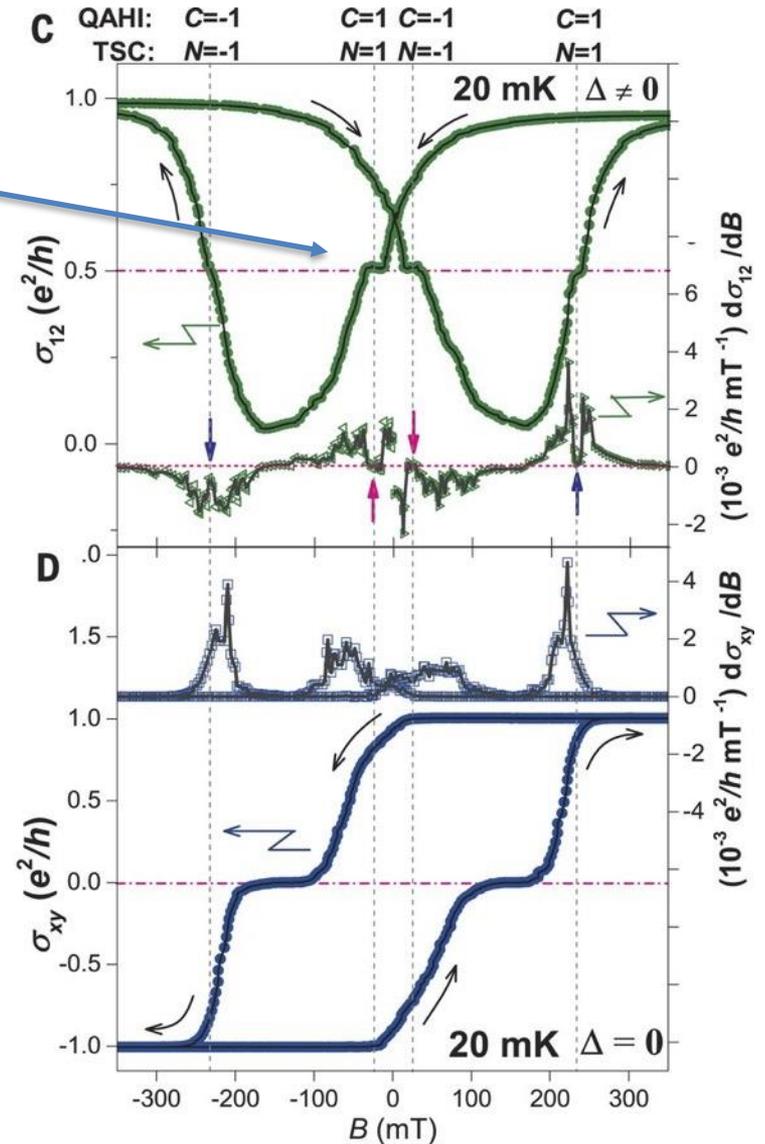
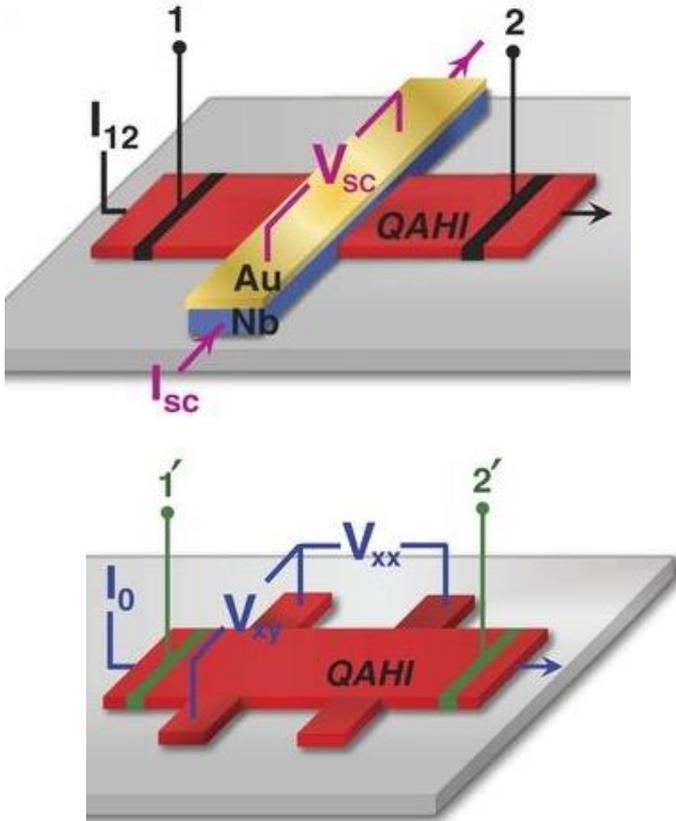
If the middle is SC



Unlike QHE or QAHE or any known topological state, it would feature a **half-integer longitudinal conductance plateau ( $0.5 e^2/h$ )**

# The “smoking gun” : 0.5 plateau

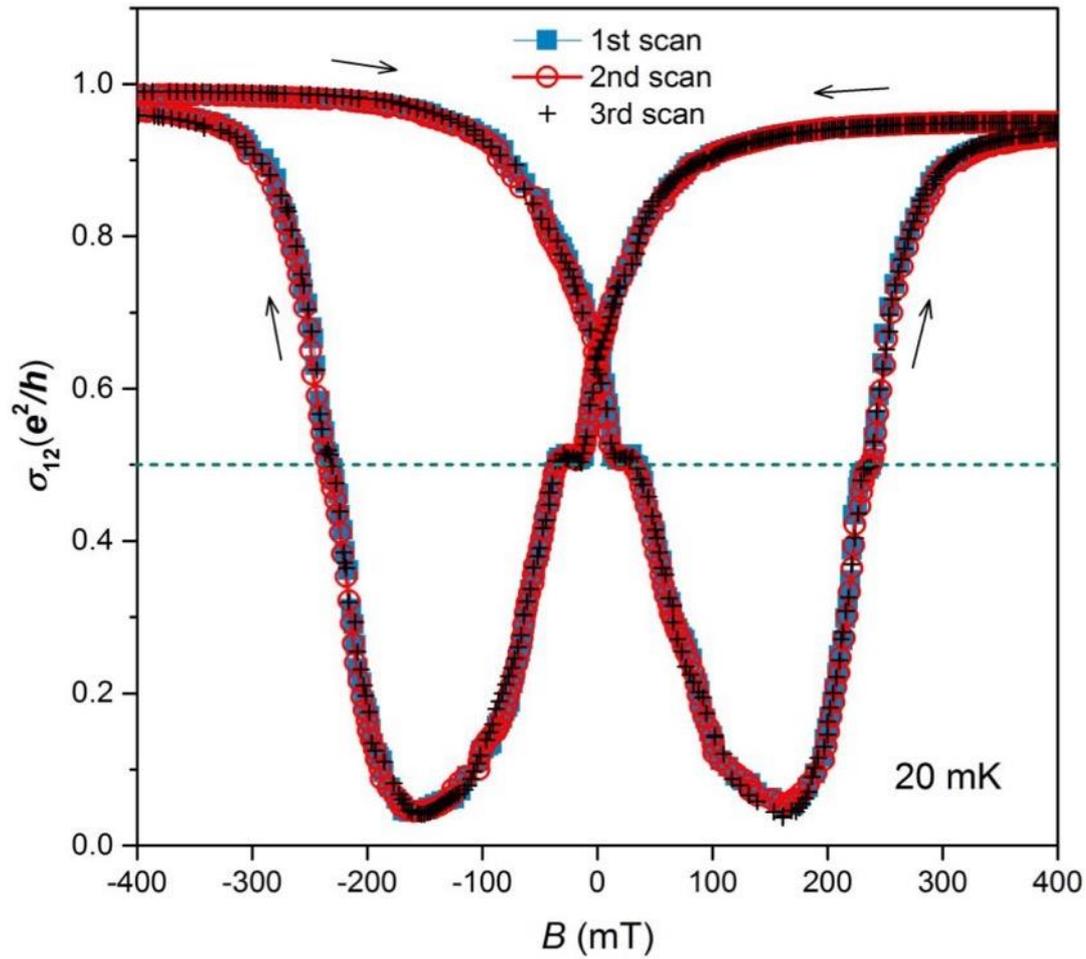
Longitudinal conductance between terminal 1 and 2 would feature a half-integer plateau ( $0.5 e^2/h$ ) near magnetic reversal.



Sigma<sub>xy</sub> of nearby QAHI sample w/o SC

# Repeatability

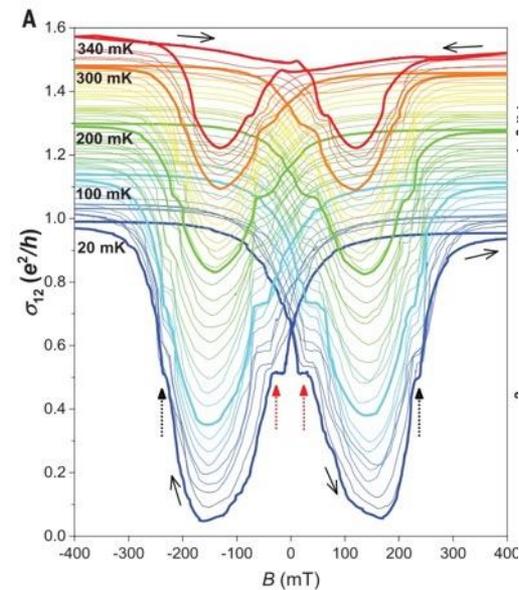
#1 device



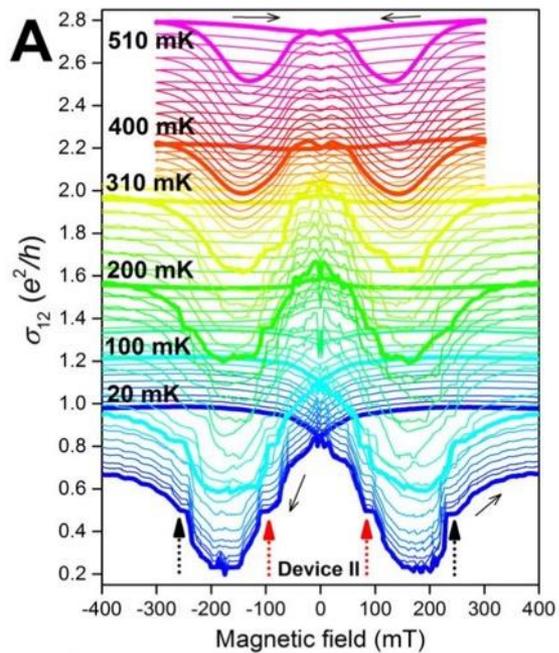
# Repeatability

3 devices separated by months.

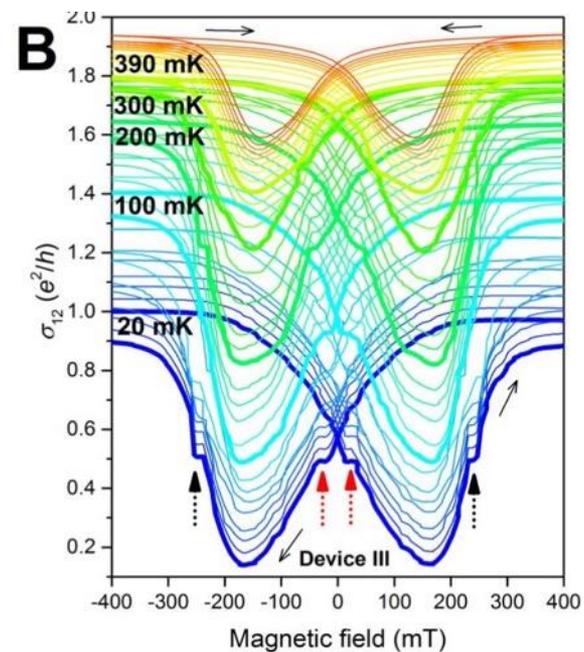
#1 device



#2 device



#3 device



- Is this directly related to topological Qubit?
- Maybe a much complicated construction is needed. However it is close to Ettore Majorana's original idea...

# Notes on Ettore Majorana (disappeared 1938)

1) This Majorana fermion propagating edge state satisfies the propagating wave equation originally proposed by Ettore Majorana, which was intended to describe neutrinos.



Dirac equation

$$\begin{aligned}(E + \mathbf{p} \cdot \boldsymbol{\sigma})\chi - m\varphi &= 0 \\ (E - \mathbf{p} \cdot \boldsymbol{\sigma})\varphi - m\chi &= 0\end{aligned}$$

Majorana equation

$$\begin{aligned}(E + \mathbf{p} \cdot \boldsymbol{\sigma})\chi - im_a \sigma_2 \chi^* &= 0 \\ (E - \mathbf{p} \cdot \boldsymbol{\sigma})\varphi - im_b \sigma_2 \varphi^* &= 0\end{aligned}$$

2) The fundamental aspects of the Majorana fermion modes and their non-Abelian braiding properties can be potentially used for topologically protected (fault-tolerant) quantum computation.

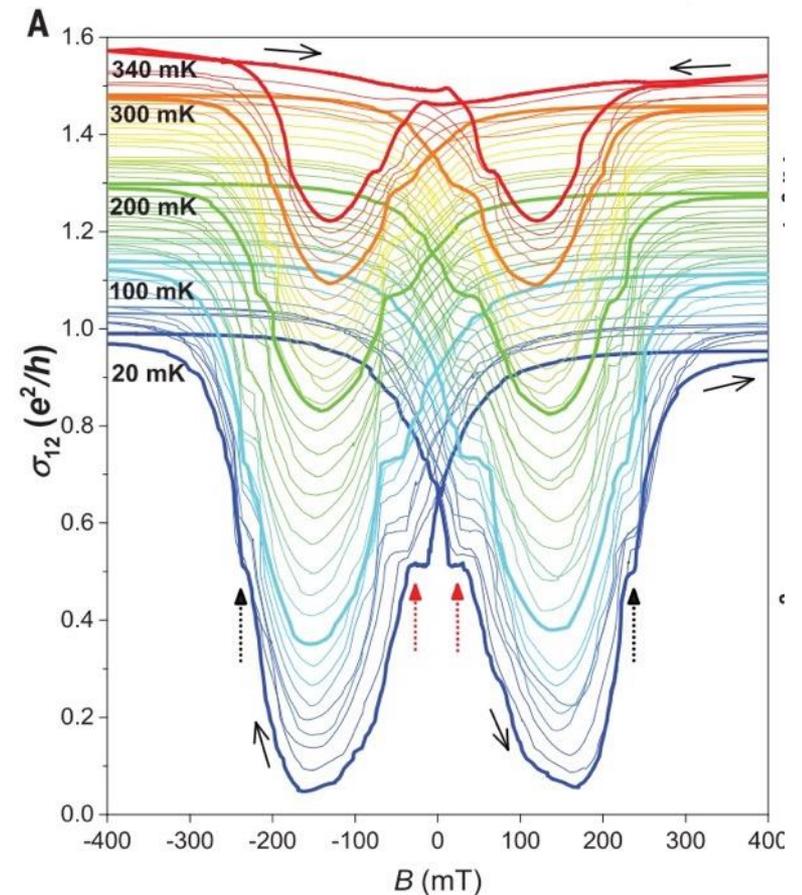
*On March 25, 1938, he disappeared under mysterious circumstances while going by ship from Palermo to Naples.*

# Why mK temperature?

$T_c$  of QAHI materials = 29 K

$T_c$  of Nb superconductor = 9 K

Why are we stuck at 20 mK?



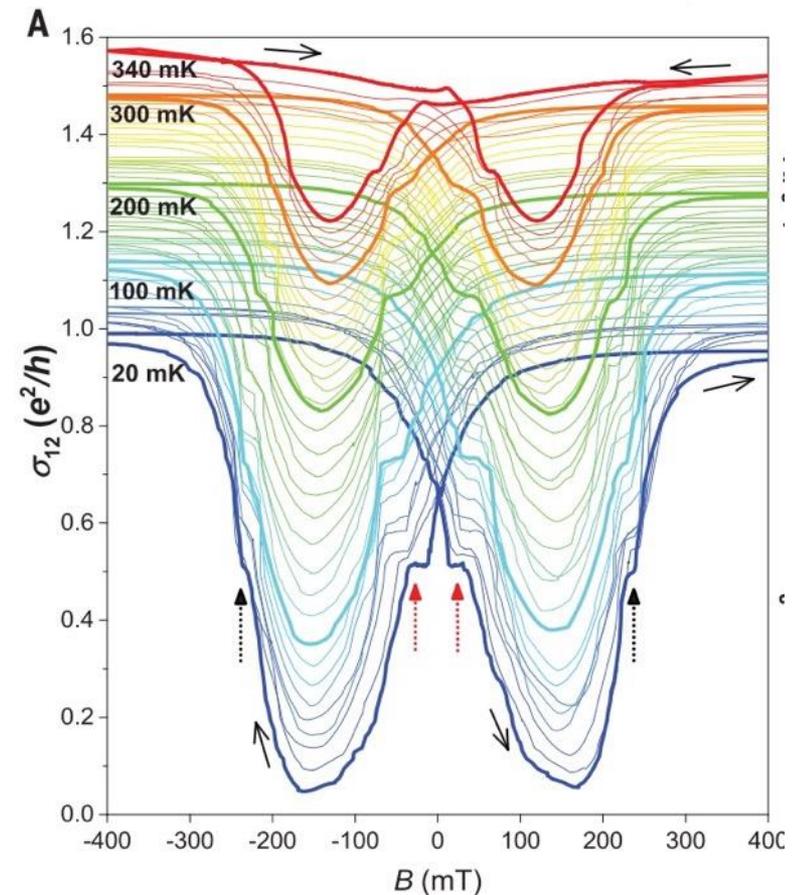
# Why mK temperature?

$T_c$  of QAHI materials = 29 K

$T_c$  of Nb superconductor = 9 K

Why are we stuck at 20 mK?

Strange magnetism in QAHI.  
We looked into this using  
combined transport and  
magnetic imaging (Sagnac  
interferometer microscope.)



# Summary

- A single Majorana edge mode is discovered in a topological superconductor structure.
- The mode is describe by the Majorana propagation equation and “maybe” useful for topological quantum computing.
- It is the instability of small FM region that kills QAHE. More uniform samples may reach QAHE at  $\sim 20$  K.

Another potential candidate for  
Majorana edge state:

Exotic Superconductivity in Bi/Ni  
bilayer

# Artificially engineered superconductor

Can we engineer some exotic superconductor?

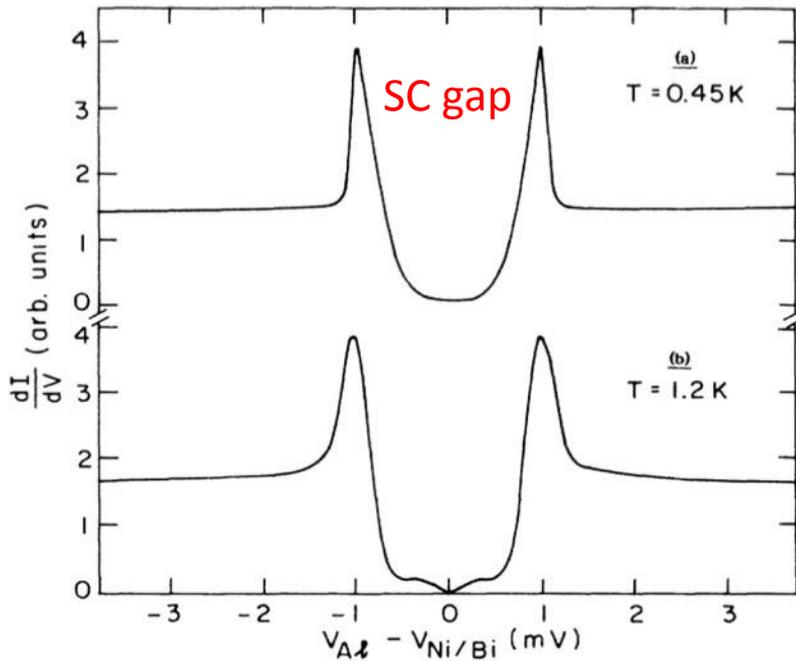


FIG. 1. Tunnel conductance plotted as a function of applied bias for two Al/Al<sub>2</sub>O<sub>3</sub>/Ni/Bi tunnel junctions with Ni/Bi of 4/800 (a) and 10/85 (b) showing superconductivity at the Ni/Bi and Al with the Al<sub>2</sub>O<sub>3</sub>.

## PHYSICAL REVIEW B

covering condensed matter and materials physics

Highlights Recent Accepted Authors Referees Search Press

Superconducting phases of Bi and Ga induced by deposition on a Ni sublayer

J. S. Moodera and R. Meservey  
Phys. Rev. B **42**, 179 – Published 1 July 1990



# The nature of Bi/Ni superconductor?

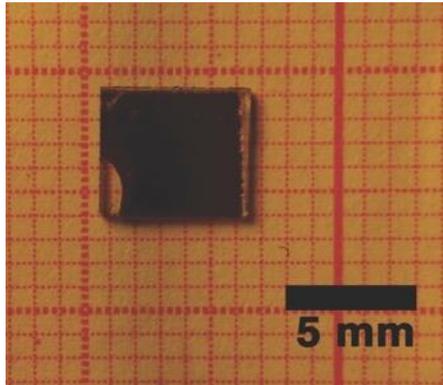


The superconductivity seems to be exotic:  
Ni is a ferromagnet  
Bi is a semimetal

Moodera sample was made by sputtering  
Uncertainties on Bi thickness, Ni thickness, Bi/Ni interface....

Need better sample and new probes to understand this  
superconducting state...

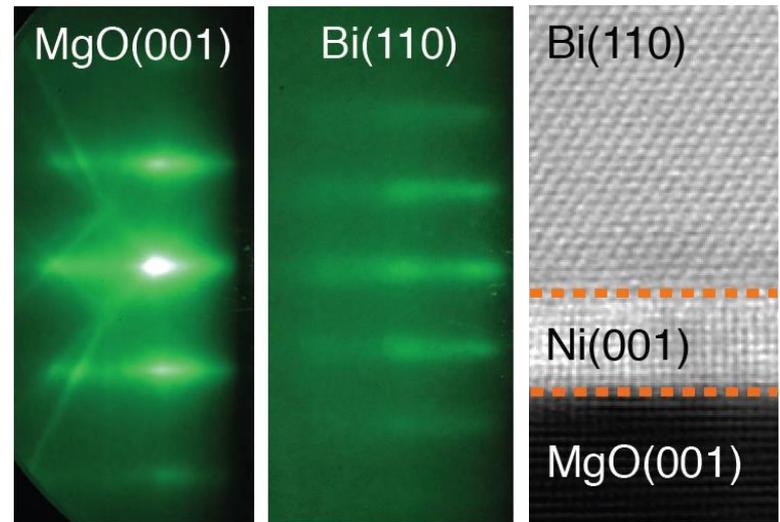
# What is the nature of SC in Bi/Ni?



Today: High quality Bi/Ni samples with MBE

**Prof. Xiaofeng Jin (Fudan)**

molecular beam epitaxy (MBE)



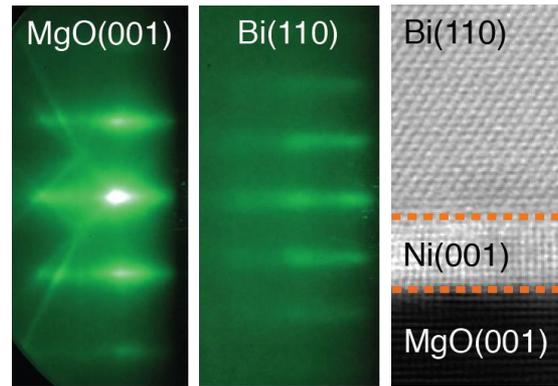
SCIENCE ADVANCES | RESEARCH ARTICLE

**SUPERCONDUCTIVITY**

## Time-reversal symmetry-breaking superconductivity in epitaxial bismuth/nickel bilayers

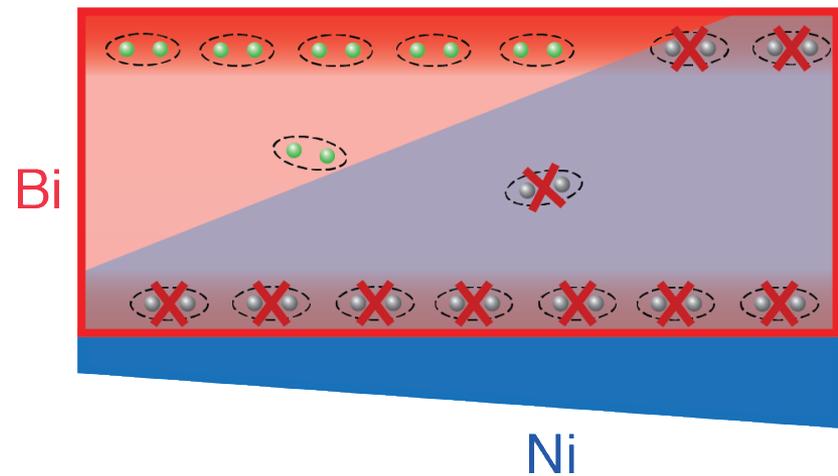
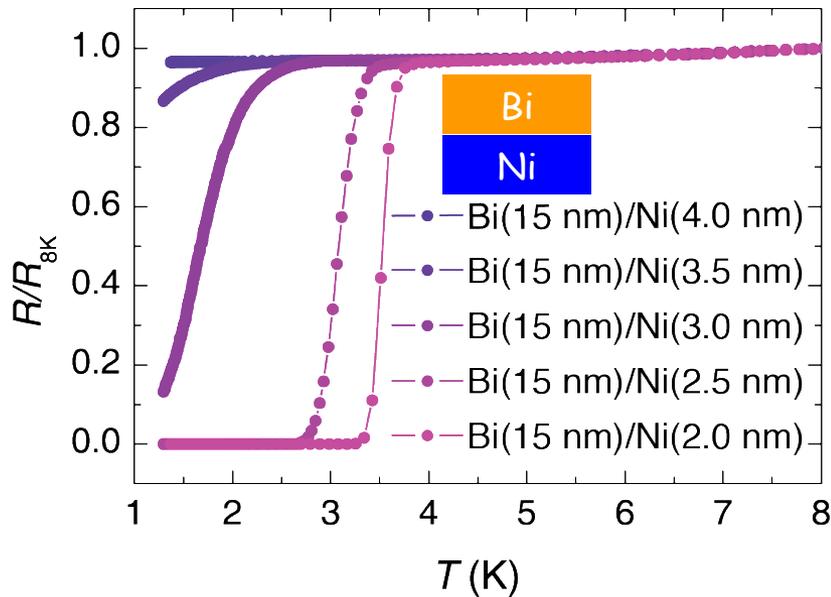
Xinxin Gong,<sup>1,2</sup> Mehdi Kargarian,<sup>3</sup> Alex Stern,<sup>1</sup> Di Yue,<sup>2</sup> Hexin Zhou,<sup>2</sup> Xiaofeng Jin,<sup>2</sup> Victor M. Galitski,<sup>3</sup> Victor M. Yakovenko,<sup>3</sup> Jing Xia<sup>1\*</sup>

# What is the nature of SC in Bi/Ni?

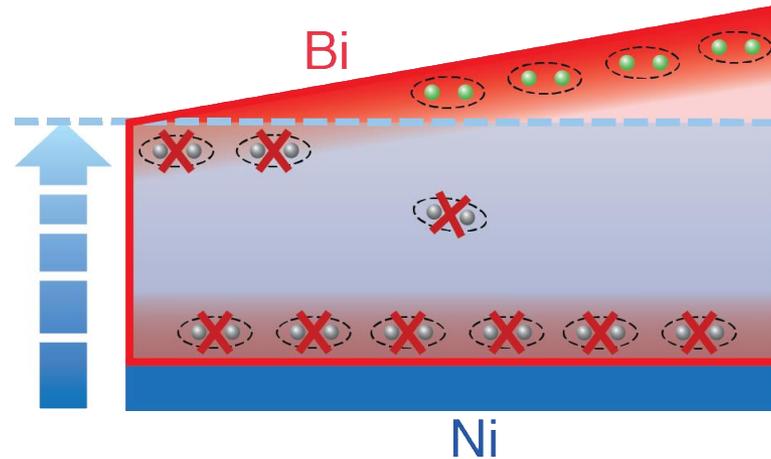
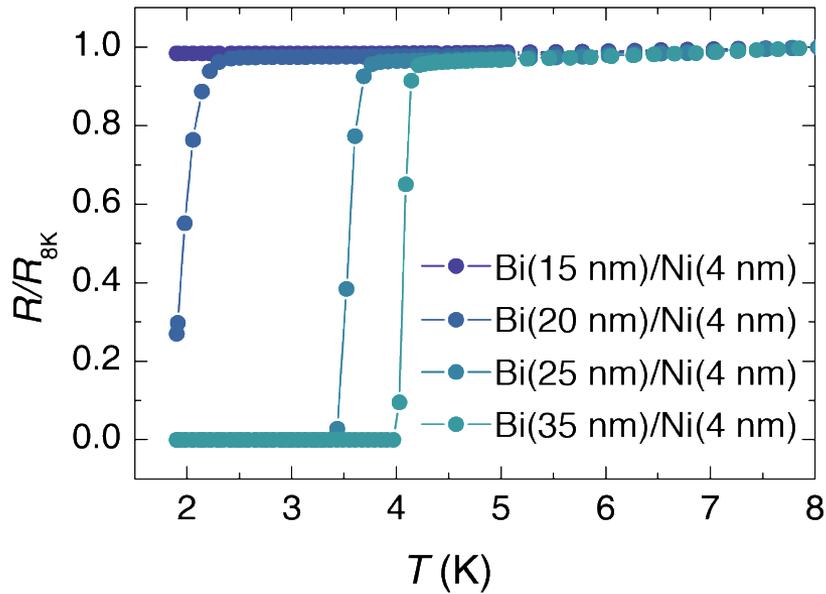


MBE High quality  
Bi/Ni samples

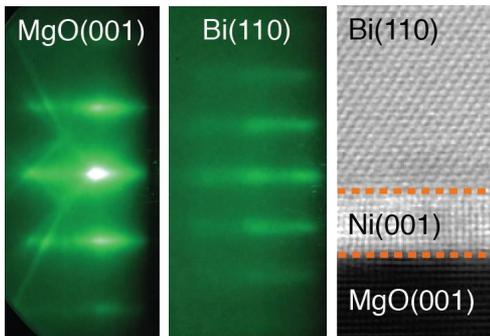
Thicker Ni layer seems to suppress superconductivity.



# What is the nature of SC in Bi/Ni?



Thicker Bi seems to strengthen superconductivity.



# The interesting case of Bi

Facts about Bi:

The heaviest nonradioactive element.

Normally a semimetal with extremely long mean free path.

Due to its extremely strong spin-orbital coupling and the broken space-inversion symmetry at the surface or interface, the spin degeneracy of surface states of Bi thin film is lifted and the energy bands split in the momentum space, resulting a helical spin structure on the Fermi surface (Rashba Effect) resembling 3D topological insulators.

One could polarize this peculiar spin texture in the in-plane direction and introduce an effective pairing interaction through the out-plane magnetic fluctuation. The spin-orbital coupling Bi and magnetic fluctuation arising from Ni can cooperatively induce pairing channels with a finite total angular momentum. As such, the superconducting order parameter would **break the TRS, and could be experimentally tested with Sagnac interferometer.**

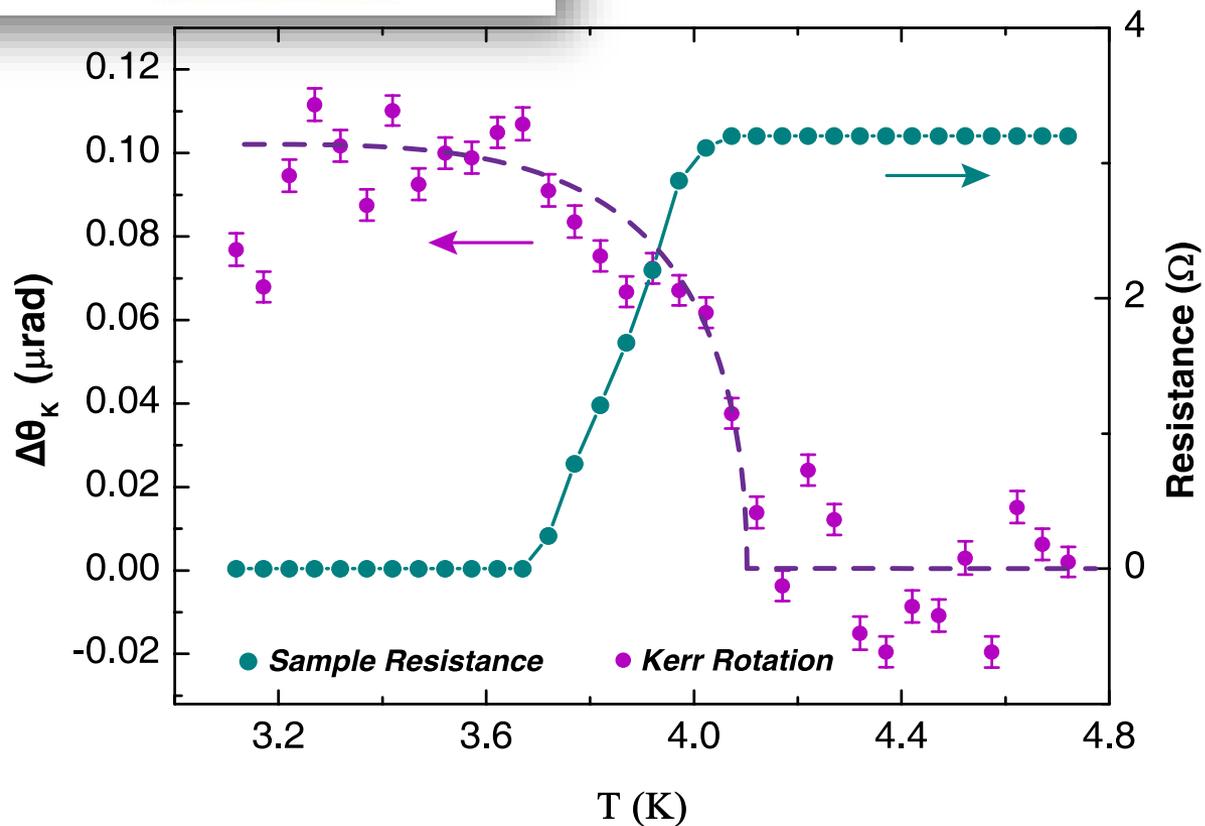
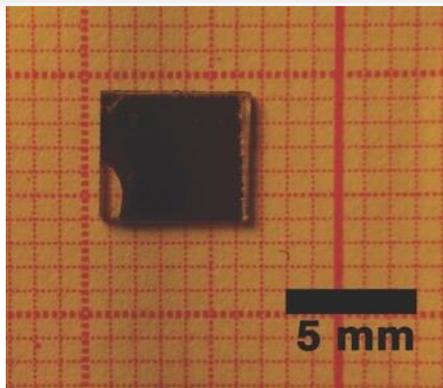
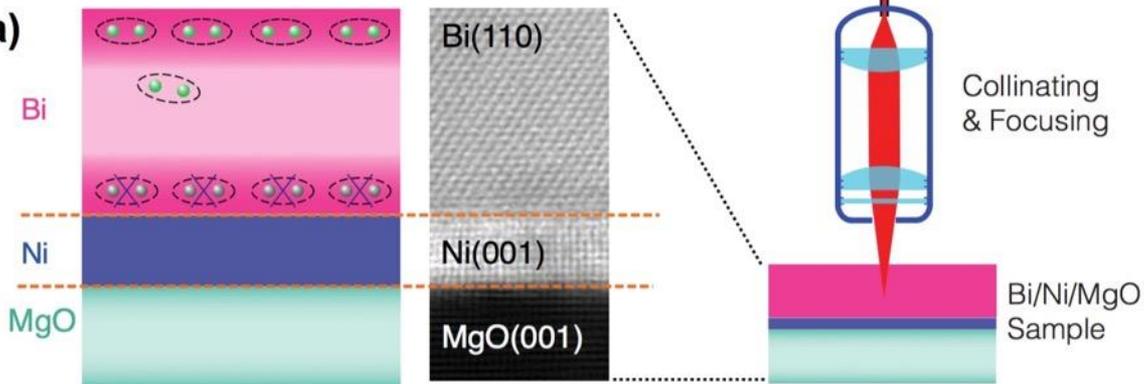
83

**Bi**

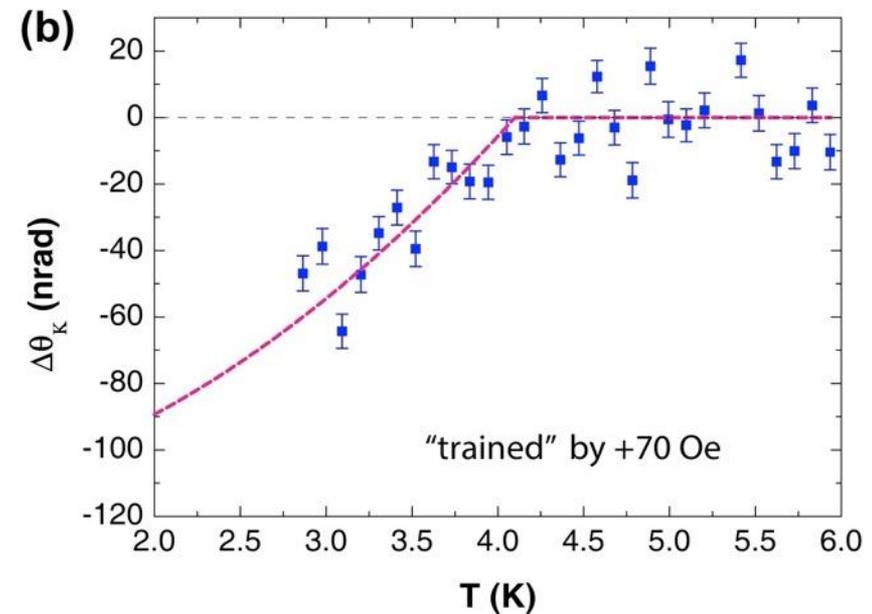
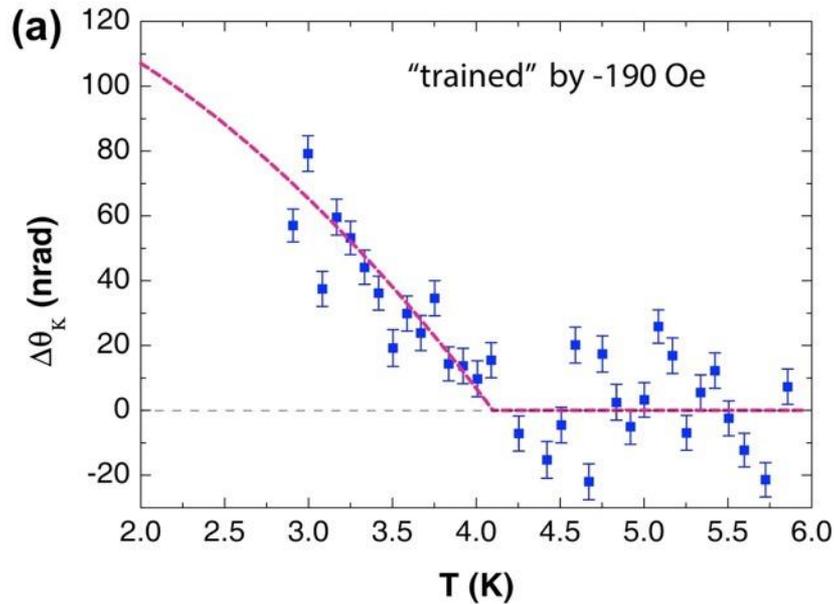
**Bismuth**  
208.980

# TRSB in Bi/Ni at $B = 0$

(a)



# Chirality can be trained by a cooling field



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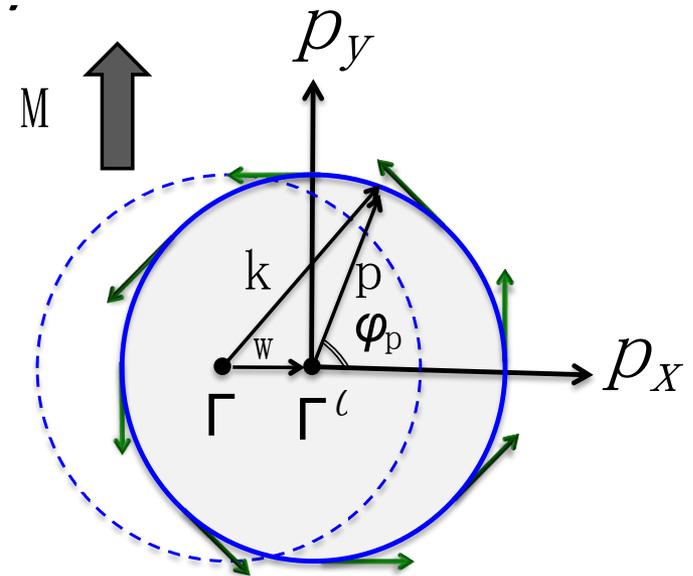
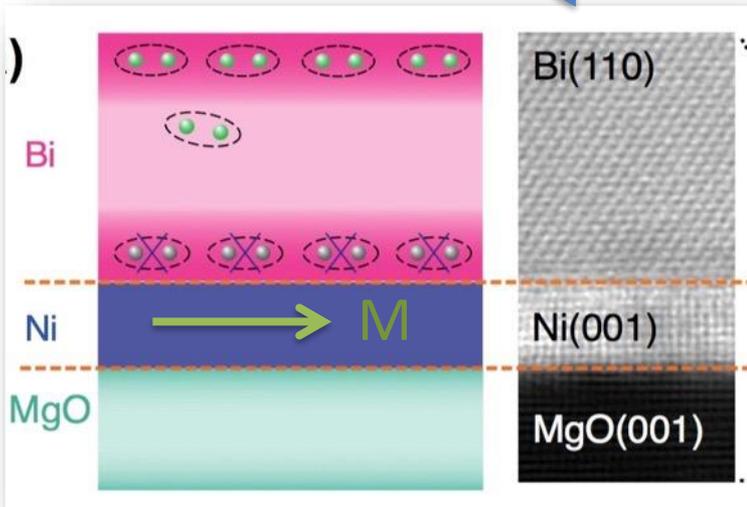
**SUPERCONDUCTIVITY**

## Time-reversal symmetry-breaking superconductivity in epitaxial bismuth/nickel bilayers

Xinxin Gong,<sup>1,2</sup> Mehdi Kargarian,<sup>3</sup> Alex Stern,<sup>1</sup> Di Yue,<sup>2</sup> Hexin Zhou,<sup>2</sup> Xiaofeng Jin,<sup>2</sup>  
Victor M. Galitski,<sup>3</sup> Victor M. Yakovenko,<sup>3</sup> Jing Xia<sup>1\*</sup>

# Do we have an understanding?

Bi(110) surface is metallic.



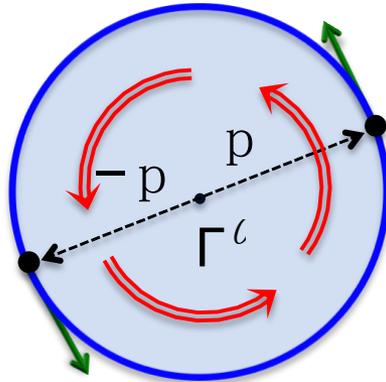
The original Fermi circle at  $\Gamma$  is shifted by the vector  $\mathbf{w}$  to the solid-blue circle centered at  $\Gamma'$  due to the in-plane magnetization  $\mathbf{M}$  from Ni.

The green arrows show spin polarization locked to the momentum direction due to strong Rashba-type spin-orbit coupling.

Theory by Victor M. Yakovenko, Mehdi Kargarian, Victor M. Galitski

# $d+id$ superconductor

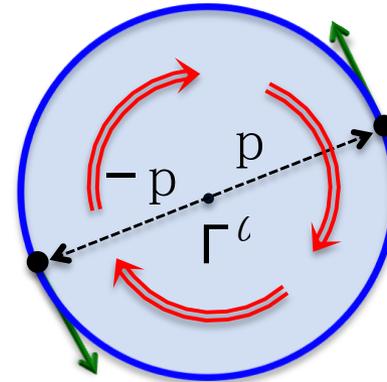
$H_{\text{training}} \odot$



$$J_z = 2$$

$d+id$

$H_{\text{training}} \otimes$



$$J_z = -2$$

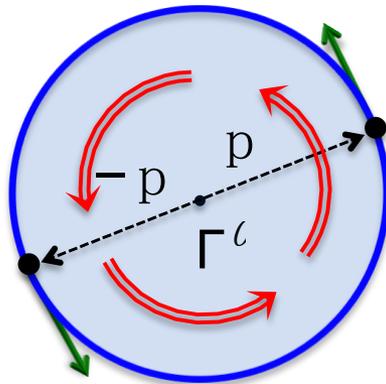
$d-id$

NOTE:  $p+ip$  is not allowed because Bi surface is non-degenerate due to large spin-orbit interaction.

Superconducting pairing of the electrons with opposite spins and opposite momenta  $\mathbf{p}$  and  $-\mathbf{p}$ . The time-reversal-breaking condensate has the total angular momentum  $J_z = \pm 2$ , corresponding to  $d \pm id$  pairing, as indicated by the double red curved arrows. A weak training magnetic field can select one of the two degenerate states.

# $d+id$ state

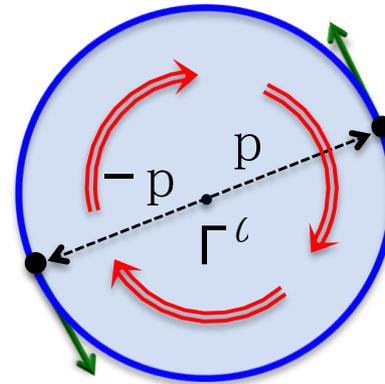
$H$  training  $\odot$



$$J_z = 2$$

$d+id$

$H$  training  $\otimes$



$$J_z = -2$$

$d-id$

Superconductivity spontaneously breaks time-reversal symmetry and is topologically non-trivial with  $J = \pm 2$ , so there are two Majorana chiral edge states moving in the same direction.